Safety, serviceability an efficiency of limit design for reinforced concrete beams and frames

Autor(en): **Cohn, M.Z. / Burnett, E.F.P. / Grierson, D.E.**

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Safety, Serviceability and Efficiency of Limit Design for Reinforced Concrete Beams and Frames

Sécurités de rupture et de service, et rendement du dimensionnement à la rupture de poutres et de portiques en béton armé

Sicherheit, Nutzbarkeit und Leistung einer Bemessung auf Bruch von Stahlbetonbalken und -rahmen

M. Z. COHN E. F. P. BURNETT D. E. GRIERSON Prof. of Civil Eng. Assist. Prof. of Civil Eng. Assist. Prof. of Civil Eng. University of Waterloo, Waterloo, Ontario, Canada

Introduction

A variety of methods is presently available for the analysis and design of reinforced concrete structures allowing for different degrees of moment redistribution $[1] \ldots [8]$.

Recently a comprehensive study was devoted to the presentation of the specific techniques, features, field of application and limitations of these methods [9].

The study was prompted by the need for providing structural engineers with an overall view of the potential applications of limit design and with some illustration of the problems involved in the available approaches. Two important results of this study [9] are noted:

- 1. A set of objective criteria for quantitatively comparing structural design solutions evolved.
- 2. Some theoretical developments in the ultimate load design [10], optimal design [11], [12], compatibility analysis [13] and computer techniques in plastic analysis [14] followed.

While the theoretical developments mentioned above are reported elsewhere, this paper elaboratores on the objective criteria first presented in [9], i.e., the collapse safety, serviceability and efficiency of limit design solutions and methods.

The paper does not attempt to recommend the application of any specific method in preference to the other. It only provides the designer with ^a set of standard criteria for evaluating various limit design methods $[2] \dots [8]$ with respect to the currently used ultimate strength design (USD) method [1].

Design Criteria and Limit Design Methods

A summary of the design criteria and basic assumptions adopted in various methods is reproduced in Table ¹ [9],

The ultimate safety is expressed by the ultimate load factor for a particular loading arrangement, which is defined as the ratio of the collapse load for the given loading arrangement to the corresponding service load, $\lambda^+ = W_u^+ / W$. The ultimate safety parameter (u.s.p.) u_i , can be introduced as a convenient measure of the structural safety, and is defined by the ratio of the ultimate to the specified load factors, i.e., $u_i = \lambda_i^+/\lambda_0$.

The serviceability is basically dependent on the safety against the first section reaching its ultimate stage. In brief, this is here referred to as yield safety, and is measured by the yield load factor. This is defined as the ratio of the load at which the ultimate moment is reached at section j (first plastic hinge load) and the service load, i.e., $\lambda_{1j} = W_{1j}/W$. A convenient measure of the yield safety of ^a critical section for ^a particular loading arrangement is the yield safety parameter (y. s.p.), which is the ratio of the yield load factor of the section to the specified overall load factor of the structure, i.e., $x_i = \lambda_{1,i}/\lambda_0$.

The compatibility condition ensures that section behaviour in the inelastic range follows the load-deformation curve of the material. For the elasticplastic material idealization it reduces to ^a limitation of the inelastic rotations, i.e., $\theta_i \leq \theta_{pj}$ [16]. This condition presupposes a limiting concrete strain which varies with different methods, as listed in line ³ of table 1.

The efficiency of a particular design solution may be considered in relation to total or initial cost, material consumption or other criteria. When geometry, concrete sections and shear reinforcement are maintained constant for various solutions, a reasonable criterion of economy is the consumption of flexural reinforcing steel. If V_e and V_k are the steel volumes required by the elastic, U.S.D. solution and by limit design respectively, the ratio $v_k = V_k/V_e$ is a measure of the relative steel consumption in limit vs. elastic design, and is referred to in this and previous studies [9], [11] as the efficiency index of the structure.

This paper suggests that ratios u_i , x_j and v_k , enable a meaningful comparison of design solutions to be made in relation to safety, serviceability and efficiency, respectively.

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The following methods are investigated:

- 1. USD: "Ultimate Strength Design" as proposed in the ACI Building Code [1], currently accepted in American design practice, and implying an elastic structural analysis and plastic sectional design.
- 2. BLD: "Bi-Linear Design" as proposed by H. A. Sawyer, Jr., [2], [3] and similar in principle to the method of imposed rotations by MACCHI [15].
- 3. SLD: "Simplified Limit Design", as proposed by A. L. L. Baker [4], [5] with amendments to include a serviceability criterion and consistency in the ultimate conditions [10].
- 4. LRD and FRD: "Limited and Full Redistribution Designs", as proposed by M. Z. COHN, [7], [8], formerly referred to as OLD 2 and OLD 1 methods respectively, [6].
- 5. OLD: "Optimum Limit Design" as proposed by M. Z. Cohn and D. E. Grierson [8], [11].

Methods 2., 3. and 4. above have been selected because they have a relatively higher potential for application, are representative of methods in the

Fig. 1. Geometry and loading of 6 examples of building structures.

"compatibility" and "serviceability" classes [7] and have been retained for consideration by the Joint ASCE-ACI Committee 428, Limit Design.

Methods 1. and 5. have been included because they represent the extreme trends in relation to the safety, serviceability and efficiency of structural designs.

The lines in table 1 are self-explanatory and summarize the basic assumpand criteria adopted in various limit design methods illustrated in the paper.

Examples of Building Structures

Design solutions based on various methods are studied by reference to six examples of building structures to which limit design may safely be applied at this time. It is believed that limit design principles are acceptable for all the examples investigated because flexural action prevails and, with proper detailing, shear, instability and other effects may be neglected. These examples are indicated in Fig. ¹ and consist of two continuous beams, two multi-storey braced frames and two single-storey, unbraced frames. The braced frames were

Fig. 2. Factored elastic moment envelopes (USD theoretical Solutions).

Example	Section $\left(\jmath\right)$	USD		BLD		SLD		LRD		\mathbf{FRD}		OLD	
		M_{pj}	x_i	M_{pj}	x_i	M_{pj}	x_i	M_{pj}	x_j	M_{pj}	x_i	$M_{\,pj}$	x_j
	$\boldsymbol{2}$ 3 4 5 6	189.4 1.000 368.7 1.000 284.3 1.000 426.4 233.1 $465.5 \quad 1.000$	1.000 1.000	175.0 335.0 247.0 385.0 235.0 385.0	0.923 0.910 0.870 0.905 1.008 0.826	270.0 0.732 297.0 1.045 331.0 265.0 1.138 331.0 0.710	143.0 0.755 0.777	310.0 256.0 210.0	$170.5 \quad 0.900$ 0.840 0.900 358.0 0.840 0.900 392.0 0.840	135.0 289.0 271.0 334.0 233.0 366.0	0.712 0.785 0.950 0.785 1.000 0.785	135.0 234.3 426.4 166.0 408.1	0.712 271.3 0.736 0.824 1.000 0.712 0.877
$\bf{4}$	1 $\overline{2}$ 3 4 5	284.0 330.0 215.0 291.0 240.5	1.000 1.000 1.000 1.000 1.000			275.5 0.970 231.0 0.700	168.0 0.782 205.0 0.704 181.5 0.756	255.5 244.5 193.3 215.5 216.5	0.900 0.740 0.900 0.740 0.900	260.5 235.0 157.0 207.0 171.0	0.916 0.712 0.732 0.712 0.712	253.0 251.0 150.3 203.0 172.3	0.889 0.760 0.700 0.700 0.726

Table 2. Design Solutions and Yield Safety: M_{pj} and x_j Values for Continuous Beam Examples ¹ and 4

Table 3. Design Solutions and Yield Safety: M_{pj} and x_j Values for Braced Frame Examples and 5

Exam- ple	Sec- tion (j)	USD	SLD	LRD	FRD	OLD	
		$M_{\,pj}$ x_i	M_{pj} x_i	M_{pj} x_i	M_{pj} x_i	$M_{\,pj}$ x_j	
$\overline{2}$	1 $\boldsymbol{2}$ 3 4 $\bf 5$ $\boldsymbol{6}$ 7 8	1.000 51.4 1.000 153.9 256.9 1.000 1.000 317.1 1.000 220.6 1.000 340.7 340.6 1.000 1.000 219.5	0.940 48.0 1.010 155.0 0.820 210.0 275.0 0.870 236.0 1.070 275.0 0.810 275.0 0.810 236.0 1.070	0.915 47.0 0.915 141.0 0.915 235.0 290.9 0.915 0.915 202.0 312.0 0.915 312.0 0.915 202.0 0.915	46.0 0.890 143.0 0.930 0.890 229.9 0.890 282.0 208.0 0.940 303.0 0.890 303.0 0.890 197.0 0.890	51.4 1.000 153.9 1.000 185.6 0.723 317.1 1.000 170.5 0.773 340.7 1.000 340.6 1.000 159.6 0.727	
$\overline{5}$	1 $\boldsymbol{2}$ 3 4 $\bf 5$ 6 7 8	1.000 70.6 157.6 1.000 1.000 241.2 1.000 230.7 1.000 126.2 213.1 1.000 216.0 1.000 133.5 1.000	0.992 70.0 169.2 1.074 0.706 170.0 0.737 170.0 0.986 124.6 0.727 155.0 155.0 0.717 132.5 0.993	63.3 0.897 0.897 141.4 216.2 0.897 0.897 207.0 113.2 0.897 0.897 191.2 0.897 193.9 119.8 0.897	56.7 0.803 155.8 0.988 0.803 194.0 185.3 0.803 102.8 0.814 171.4 0.803 173.7 0.803 107.5 0.803	70.6 1.000 0.794 125.1 241.2 1.000 230.7 1.000 89.1 0.706 153.9 0.722 183.1 0.866 94.3 0.706	

designed assuming that the requirements of articles 905 and 914 of ACI 318-63 [1] apply.

Examples 1, ² and ³ are the same as in reference [9] and represent fairly typical loads, geometries and amounts of plastic redistribution. Examples 4, 5 and 6 have been added in an attempt to explore higher limits of redistribution for the same classes of structures.

The five methods mentioned in the previous section have been successively applied to the six examples in Fig. 1. Details of the analysis and design pro-

cedures will not be reproduced here, as they have been extensively described elsewhere [9].

The factored elastic moment envelopes for all six examples, which constitute the theoretical USD Solution, are given in Fig. ² in k-ft. units.

Design Solutions based on USD, BLD, SLD, LRD, FRD and OLD are summarized in terms of plastic moments M_{pj} required at each critical section in table 2 for the beam examples ¹ and 4, in table 3 for the braced frame examples ² and 5, and in table 4 for the unbraced frame examples ³ and 6.

For the sake of undistorted comparison, the theoretical moments, as resulting from analysis, are generally assumed as design moments. A 5% overdesign of span moments has been used in SLD as an additional ultimate safety and to avoid collapse mechanism formation at the ultimate load.

The BLD method has been applied only to the first two examples, as it appears to require considerable computational effort. It is believed that the solutions obtained for these two examples and the criteria on which the method is based are sufficient to indicate probable trends in its general application.

Safety

An accurate evaluation of the actual carrying capacity of ^a given design is not possible. If plastic collapse is assumed to be an acceptable failure condition for all designs, the mechanism collapse load W_t^+ and the ultimate safety parameter $u_i = \lambda_i^+/\lambda_0$ provide a convenient measure of the relative safety of various designs.

Possible collapse modes of the six structures chosen as examples are shown in Fig. 3. For examples ³ and ⁶ only the most critical mechanisms, i.e., those resulting in lowest safety, are indicated. Values of the ultimate safety meters u_i for each critical collapse mode and for each design solution are given in table 5.

Fig. 3. Collapse modes of example structures.

Exam- ple	Mecha- nism (i)	USD	BLD	SLD	LRD	FRD	OLD
1	1 $\overline{2}$ 3	1.381 1.170 1.164	1.269 1.042 1.063	1.029 1.025 1.022	1.205 1.000 1.000	1.000 1.000 1.000	1.000 1.000 1.000
$\sqrt{2}$	1 $\overline{\mathbf{2}}$ $\overline{\mathbf{3}}$	1.095 1.100 1.122		1.028 1.022 1.022	1.000 1.008 1.028	1.000 1.000 1.000	1.000 1.000 1.000
$\bf{3}$	ı $\overline{2}$ $\overline{\bf 3}$ $\boldsymbol{4}$ $\overline{5}$ $\bf{6}$	1.285 1.292 1.975 1.170 1.160 1.170	1.150 1.116 1.810 1.130 1.100 1.118	1.052 1.045 1.618 1.030 1.012 1.025	1.028 1.055 1.542 1.000 1.000 1.000		1.075 1.000 1.396 1.020 1.000 1.000
$\bf{4}$	l $\frac{2}{3}$	1.189 1.389 1.405		1.035 1.022 1.023	1.000 1.121 1.143	1.000 1.000 1.000	1.000 1.000 1.000
$\overline{5}$	\bf{l} $\frac{2}{3}$	1.116 1.240 1.247		1.029 1.021 1.023	1.000 1.112 1.118	1.000 1.000 1.000	1.000 1.000 1.000
$\boldsymbol{6}$	1 $\frac{2}{3}$ $\frac{4}{5}$ 6 7 8	1.235 1.387 1.235 4.060 1.241 1.258 1.273 1.325		1.034 1.054 1.034 2.520 1.018 1.004 1.056 1.020	1.000 1.003 1.000 2.950 1.000 1.000 1.002 1.031		1.000 1.000 1.000 3.000 1.000 1.050 1.019 1.110

Table 5. Collapse Safety: u_i Values

It is noted that since the mechanism collapse is the most severe failure criterion considered $u_i = 1$ in methods based on such criterion, i.e., OLD, FRD and LRD, and $u_i > 1$ in SLD, BRD and USD, which adopt more conservative failure criteria. In the full redistribution design (FRD) $u_i=1$ or $\lambda_i=\lambda_0$ is postulated for a number of collapse modes equal to the number of independent limit equilibrium equations that can be written for the structure. For the optimal limit design (OLD) the same result is obtained, although this dition is not an explicit design requirement. In limited redistribution design (LRD) the condition $u_i=1$ in at least one collapse mode is imposed and is reflected in table 5. SLD Solutions are in general close to those for LRD and for beam problems may be made close to FRD Solutions if adequate safety and serviceability criteria are adopted [9], [10].

Safe SLD Solutions may be obtained only when all possible loading combinations are considered. This is essential in cases where lateral loads are significant, as the exclusive consideration of the füll loading for the structure may be unsafe in some particular loading schemes. The same aspect should be retained in calculating inelastic rotations and checking the compatibility requirements for all critical sections under the most critical loading arrangements.

BLD Solutions result in larger collapse safety than other limit design methods because the governing failure criterion is the crushing of the first, most stressed, section in the structure.

It is seen from table ¹ that the largest strength reserves against plastic collapse are provided by the USD Solutions, which imply that the structure fails when at least one of its critical section yields.

Serviceability

Normal service performance requires that deflections be within acceptable limits, cracking not be excessive, maximum stresses remain within allowable bounds and inelastic behaviour be avoided. It has been shown [17] that except for the deflection requirement all service conditions are controlled by adopting a sufficiently large margin of safety against the ultimate moment of critical sections. For the under-reinforced sections currently used in reinforced concrete design yielding of steel governs the formation of plastic hinges and the ultimate moment. Hence, the concept of yield safety is introduced, which can be measured by the yield load factor λ_{1i} for each critical section j. By definition, this is the ratio of the ultimate moment to the working moment, i.e., $\lambda_{1,i} =$ M_{pi}/M_i . Note that, for proportional loading between service and ultimate stages, this ratio also equals the ratio of corresponding first yield to service loads, or $\lambda_{1j} = M_{pj}/M_j = W_{1j}/W$ [7].

It has been shown [9] that adoption of a lower bound for $\lambda_{1,i}$ may ensure the simultaneous satisfaction of all serviceability requirements but the deflection control, and accordingly a tentative bound was suggested as $\lambda_1 = \min \lambda_{1i} =$ 1.2.

It is emphasized that further study is necessary for ^a proper assessment of the minimum values of acceptable yield load factors. Indeed, variable λ_1 values may be warranted to allow for different roles of span, support or column sections or to accomodate different serviceability requirements.

With $\lambda_1=1.2$ and λ_0 corresponding to the dead and live loads in each example, minimum values of yield safety parameters, $\min x_j=1.2/\lambda_0$, resulted as in table 6.

Example			ູ		ັ	
Λ_0	1.685	$1.700\,$	1.700	1.714	1.700	2.000
$\min x_i$	$0.712*)$	0.706	$0.706*)$	0.700	0.706	0.600

Table 6. Minimum Allowed Yield Safety Parameters for $\lambda_1 = 1.2$

*) In BLD, since $\lambda_1 = 1.39$ is adopted, min x_j for examples 1 and 3 are 0.825 and 0.818 respectively.

For the design solutions listed in tables 2, 3, and 4, it is seen that this serviceability requirement is nowhere violated. Values of $x_i = 1$ in the USD solution reflect the criterion of structural failure associated with the first section becoming a plastic hinge, i.e., $\lambda_{1,i} = \lambda_0$. Occasional values of $x_i > 1$ refer to highly conservative designs for column sections, indicating that in no loading arrangement such sections could be the first to yield.

It is seen that extreme values of x_i are used for SLD solutions, particularly for the beam and braced frame examples. This corresponds to the trend of this paper to put each method to its advantage, ensuring maximum redistribution permitted by the standard serviceability requirements adopted.

In this regard it should be mentioned that example ⁶ is identical with the frame example used in the Institution of Civil Engineers Research Committee Report [18]. In the absence of guidelines on permissible redistribution and serviceability the SLD Solution proposed in the report [18] violates drastically the serviceability requirements for the column sections.

Values of x_i in LRD solutions reflect the alternative criteria specific to the method: either equal yield safety for all critical sections or equal x_i for span sections and smaller, but also equal x_i values for support sections. The criterion of equal minimum yield safety for the largest possible number of critical sections is reflected by the FRD solutions [6].

Consistent with the design objective of minimizing the steel volume the yield safety parameters in OLD Solutions tend to be at their lowest permissible values wherever possible.

Efficiency

The efficiency index v_k for various solutions is calculated on the following assumptions:

- 1. Section sizes remain the same in each example.
- 2. The flexural steel required at each section is proportional to the sponding design plastic moment, and
- 3. the arrangement of the flexural reinforcement follows the typical schemes in Fig. 4.

The efficiency indices calculated with the formula

$$
v_k = \frac{v_k}{V_e} = \frac{\sum_j x_j \lambda_0 M_j l_j}{\sum_j \lambda_0 M_j l_j}
$$

for the examples and methods discussed are listed in table 7. In general, it is seen that with USD solutions taken as reference, v_k values decrease (i.e. the relative reductions in steel consumption are larger) as BLD, SLD, LRD, FRD and OLD Solutions are considered in turn.

Fig. 4. Typical reinforcement of example structures for the ⁶ examples.

Table 7. Structural Efficiency: v_k Values

Example	USD	BLD	SLD	LRD	$_{\rm FRD}$	OLD
$\boldsymbol{2}$ 3 4 5 6	1.000 1.000 1.000 1.000 1.000 1.000	0.907 0.926	0.877 0.948 0.934 0.793 0.897 0.772	0.868 0.927 0.790 0.831 0.909 0.757	0.850 0.922 0.768 0.866	0.825 0.890 0.760 0.766 0.829 0.756

It is noted that for the six examples presented in the paper, limit design resulted in steel savings of from 5.2% to 25% in relation to USD.

For all the examples and limit design methods considered (excluding the extreme USD and OLD solutions) an average efficiency index $v = 0.852$ is obtained, which represents a steel saving of about 15% compared to the current design practice. It may be concluded that savings of $15-20\%$ vs. USD may be expected by adopting limit design methods for the classes of structures investigated in this paper.

Conclusions

1. When compatibility considerations are not critical, the three basic criteria governing a design solution are: safety, serviceability and efficiency.

2. The parameters $u_i = \lambda_i^+/\lambda_0$, $x_j = M_{pj}/M_j\lambda_0 = \lambda_{1j}/\lambda_0$ and $v_k = V_k/V_e$ are introduced in the paper for a quantitative evaluation of design solutions in relation to the above criteria.

3. Safety and efficiency are conflicting requirements, related to the amount of allowable moment redistribution: structures designed to accomodate a large redistribution are less safe, but more efficient than those designed for small moment redistribution.

4. Various limit design methods are available for taking advantage to any desirable degree of the inelastic moment redistribution in reinforced concrete structures. Limit design methods illustrated in the examples range in the following descending order in relation to their ultimate safety: USD, BLD, SLD, LRD, FRD and OLD, with the USD and OLD having the largest and smallest reserve strength against plastic collapse respectively. The above order is preserved for the efficiency index, indicating an increase of steel savings vs. USD as one moves from BLD towards OLD.

5. Adoption of a minimum yield load factor λ_1 is a convenient and reliable approach to the control of serviceability requirements in any limit design method.

6. The examples presented in this paper indicate that steel savings of about 15% vs. USD are very likely to be obtained, regardless of the limit design method adopted.

7. Because of the small difference in efficiency of FRD and OLD Solutions, it appears that full redistribution should be a practical aim in design, which would ensure results not too far from those based on mathematical optimization.

Notation

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Summary

Safety, serviceability and efficiency of solutions based on various limit design methods, as applied to some typical reinforced concrete building structures, are compared.

Safety is considered in relation to the failure of structures as collapse mechanisms. Serviceability is evaluated in terms of the safety against first yield of critical sections. Structural efficiency for each limit design method is evaluated by the ratio of flexural steel consumption to that resulting from an elastic design.

Six examples of typical building structures (two continuous beams, two multi-storey, multi-bay braced frames and two single-storey, unbraced frames) illustate the relevant features of Solutions based on existing limit design methods.

Résumé

Une comparaison de ces trois facteurs est faite pour différentes méthodes de dimensionnement à la rupture, appliquées à quelques structures typiques en béton armé.

La sécurité de rupture se rapporte au moment de ruine par formation de mecanisme instable. La securite de Service se rapporte ^ä la plastification des premières sections critiques. Le rendement pour chaque méthode se mesure au tonnage de fer d'armature employé par rapport au dimensionnement elastique.

Six exemples typiques de structures (deux poutres continues, deux tiques à plusieurs étages renforcés, et deux portiques simples, non-renforcés) montrent les caractéristiques essentielles des solutions des diverses méthodes existantes de dimensionnement a la rupture.

Zusammenfassung

Sicherheit, Nutzbarkeit und Leistung von Berechnungen, die auf verschie-Traglastkriterien fußen, werden an einigen typischen Stahlbetonbauten miteinander verglichen.

Die Sicherheit bezieht sich dabei auf das Bruchmoment durch Bildung eines instabilen Mechanismus. Die Nutzbarkeit bedeutet die Sicherheit vor dem Nachgeben der ersten kritischen Querschnitte. Die Leistung mißt sich am Verbrauch an Armierungsstahl für die verschiedenen Methoden gegenüber einer elastischen Bemessung.

Sechs typische Beispiele (2 Durchlaufträger, zwei versteifte Stockwerkrahmen und zwei einfache, unversteifte Rahmen) zeigen die wichtigen Charakteristiken der verschiedenen existierenden Bruchbemessungsmethoden.