

Zeitschrift: Helvetica Physica Acta
Band: 54 (1981)
Heft: 3

Artikel: Vacuum polarization test and search for direct muon-hadron interaction from muonic X-rays
Autor: Aas, B. / Beer, W. / Beltrami, I.
DOI: <https://doi.org/10.5169/seals-115217>

Nutzungsbedingungen

Die ETH-Bibliothek ist die Anbieterin der digitalisierten Zeitschriften auf E-Periodica. Sie besitzt keine Urheberrechte an den Zeitschriften und ist nicht verantwortlich für deren Inhalte. Die Rechte liegen in der Regel bei den Herausgebern beziehungsweise den externen Rechteinhabern. Das Veröffentlichen von Bildern in Print- und Online-Publikationen sowie auf Social Media-Kanälen oder Webseiten ist nur mit vorheriger Genehmigung der Rechteinhaber erlaubt. [Mehr erfahren](#)

Conditions d'utilisation

L'ETH Library est le fournisseur des revues numérisées. Elle ne détient aucun droit d'auteur sur les revues et n'est pas responsable de leur contenu. En règle générale, les droits sont détenus par les éditeurs ou les détenteurs de droits externes. La reproduction d'images dans des publications imprimées ou en ligne ainsi que sur des canaux de médias sociaux ou des sites web n'est autorisée qu'avec l'accord préalable des détenteurs des droits. [En savoir plus](#)

Terms of use

The ETH Library is the provider of the digitised journals. It does not own any copyrights to the journals and is not responsible for their content. The rights usually lie with the publishers or the external rights holders. Publishing images in print and online publications, as well as on social media channels or websites, is only permitted with the prior consent of the rights holders. [Find out more](#)

Download PDF: 17.01.2026

ETH-Bibliothek Zürich, E-Periodica, <https://www.e-periodica.ch>

Vacuum polarization test and search for direct muon-hadron interaction from muonic X-rays*

by **B. Aas**,¹⁾ **W. Beer**, **I. Beltrami**, **P. Ebersold**,²⁾ **R. Eichler**,³⁾ **Th. v. Ledebur**,⁴⁾
H. J. Leisi, **W. Ruckstuhl**, **W. W. Sapp**⁵⁾ and **A. Vacchi**

Laboratory for High Energy Physics, ETHZ, c/o SIN, CH-5234 Villigen, Switzerland

and

J. Kern, **J.-A. Pinston**⁶⁾ and **R. Weber**

Physics Department, University of Fribourg, CH-1700 Fribourg, Switzerland

(12. V. 1981)

Abstract. Results are reported on wavelength measurements of $3d-2p$ X-ray transitions in muonic ^{24}Mg , ^{28}Si and ^{31}P . The experiments were performed with the bent-crystal spectrometer at SIN. The results are analysed as a QED test and, alternatively, as a search for muon-hadron interactions. The relative difference between theory and experiment for the vacuum polarization effect is $(0.6 \pm 2.4) \times 10^{-3}$.

The particular feature of muonic-atom experiments [1-4] as a test of QED is the dominance among the radiative corrections, of the vacuum polarization effect. This is because the average muonic orbit size is of similar magnitude as the spatial extension of the polarization charge around the nucleus (which is of the order of the Compton wavelength of the electron). Muonic atom experiments are therefore complementary to other high-precision QED tests [5].

Three types of QED experiments with muonic atoms have been reported:

- (i) In heavy muonic atoms X-ray energies of transitions connecting circular orbits have been measured with Ge(Li) detectors [1].
- (ii) The $2s-2p$ energy differences in muonic ^4He have been measured in a tunable-laser experiment [2].
- (iii) Crystal-spectrometer measurements of $3d-2p$ X-rays in muonic ^{28}Si [3] and ^{31}P [4].

In the present work we report on new crystal-spectrometer measurements of $3d-2p$ transitions in the same Z region with considerably improved precision [6].

An ideal system for testing the vacuum polarization effect would be an isolated muonic atom in which the muon moves in the Coulomb field of a

* Supported in part by SIN and Schweizerischer Nationalfonds. This work has been presented at the Swiss Physical Society meeting, Neuchâtel, April 9, 1981.

¹⁾ Present address: LAMPF, Los Alamos, N.M. 87545, U.S.A.

²⁾ Present address: Kantonsschule Oerlikon, CH-8050 Zürich, Switzerland.

³⁾ Present address: DESY, Notkestrasse 85, D-2000 Hamburg 52, West Germany.

⁴⁾ Present address: SIN, CH-5234 Villigen, Switzerland.

⁵⁾ Present address: Laboratory for Nuclear Science, MIT, Cambridge, Mass. 02139, U.S.A.

⁶⁾ Present address: Centre d'études nucléaires de Grenoble, 85X-38041 Grenoble, France.

point-like nucleus. In such a system the radiative corrections would be simply the difference between the measured transition energy and the well-known energy difference as calculated from the Dirac theory (with the Coulomb potential of a nuclear point charge). In reality, nuclear structure effects and electron screening shifts generally have to be included. The $3d$ - $2p$ transitions in muonic atoms with Z around 12 are of particular interest because they are very similar to an ideal, "hydrogen-like" system. In all other experiments the corrections due to one or more of the following effects are sizeable: the nuclear finite-size shift, the electron screening correction and the nuclear polarization effect. The wavelength of each of the six $3d$ - $2p$ transitions reported here can be calculated at present with a total uncertainty of 6 ppm (including nuclear structure and electron screening effects). Still further improvements in the precision of the theoretical values can be anticipated [8].

The experimental results of the present work are interesting also from a different point-of-view. Instead of interpreting the results as a QED test, one could *assume* that this theory is correct and consider the muon as a probe for an additional muon-nucleus interaction [4]. If a direct muon-nucleon interaction were mediated by a scalar, isoscalar boson of mass m , the muon would feel an additional (Yukawa) potential of the form

$$V(r) = -A \frac{g_\mu \cdot g_N e^{-rm}}{4\pi r}, \quad (1)$$

where g_μ and g_N are the boson-muon and the boson-nucleon coupling constants, respectively, and A is the atomic mass number. Potential (1) gives rise to an additional shift of the muonic energy levels. A particular example of such an interaction is the one mediated by the Higgs boson of the Weinberg-Salam theory [9, 10].

The experiments were performed with the curved-crystal spectrometer facility at the superconducting Muon Channel I of SIN [4]. All X-rays were measured relative to either the 84 keV γ -ray of ^{170}Tm or the 63 keV γ -line of ^{169}Yb , both of which have recently been calibrated to about 1 ppm [11]. Both the $3d_{5/2}$ - $2p_{3/2}$ and the $3d_{3/2}$ - $2p_{1/2}$ X-ray transition for all three atoms were measured. The weak and unresolved transitions $3d_{3/2}$ - $2p_{3/2}$ (near the $3d_{5/2}$ - $2p_{3/2}$ line) and $3s_{1/2}$ - $2p_{3/2}$ (near the $3d_{3/2}$ - $2p_{1/2}$ line) have been considered in the analysis, as well as the $3d$ - $2p$ transitions of the rare isotopes ^{29}Si and ^{30}Si in the case of μ - ^{28}Si . (The magnesium target was enriched to more than 99% ^{24}Mg .)

The measured ratios of the muonic X-ray wavelength and the γ -ray wavelength are shown in Table I. The values in column four of Table I are corrected for effects due to the vertical extension of the source and the crystals. The quoted errors include uncertainties from geometrical effects and the data analysis procedure. The dominant contribution to the error in each measured wavelength ratio comes from counting statistics.

The experimental values for the muonic X-ray wavelengths, together with the results from Refs. 3, 4, are given in the third column of Table II. They are obtained from the ratios λ_x/λ_γ by using the γ -ray wavelengths from Ref. 11:

$$84 \text{ keV } (^{170}\text{Tm}) : \lambda_\gamma = 14.715430(13) \text{ pm};$$

$$63 \text{ keV } (^{169}\text{Yb}) : \lambda_\gamma = 19.642536(26) \text{ pm}$$

Table I

Measured ratios of wavelengths between muonic X-ray and calibration γ -rays, λ_x/λ_γ . Run 15 was calibrated with the 63.12 keV line of ^{169}Yb ; in all other runs the 84.26 keV γ -line of ^{170}Tm was used.

Isotope	transition	uncorrected ^{a)}	λ_x/λ_γ corrected ^{b)}	reference
^{24}Mg	$3d_{5/2}-2p_{3/2}$	1.122824(13)	1.122813(15)	run 15
	$3d_{5/2}-2p_{3/2}$	1.498795(14)	1.498780(15)	run 18
	$3d_{3/2}-2p_{1/2}$	1.494104(22)	1.494089(24)	run 18
^{28}Si	$3d_{5/2}-2p_{3/2}$	1.099710(35)	1.099710(38)	run 11
	$3d_{5/2}-2p_{3/2}$	1.099699(16)	1.099689(18)	run 17
	$3d_{3/2}-2p_{1/2}$	1.095047(26)	1.095037(27)	run 17
^{31}P	$3d_{5/2}-2p_{3/2}$	0.957332(47)	0.957323(48)	run 19
	$3d_{3/2}-2p_{1/2}$	0.952848(80)	0.952839(85)	run 19

^{a)} Statistical errors are given.

^{b)} Corrected for source-height effect; total errors are given.

The theoretical (QED) values of the X-ray wavelengths (Ref. 8) are also given in Table II (column six). They include the nuclear structure effects (finite size and nuclear polarization) and the electron screening shift, as well as higher-order radiative corrections (see also Refs. 7, 12). The over-all uncertainty in each value of λ_{th} is 6 ppm (Ref. 8). The experimental wavelength values are compared to the QED values in the last column of Table II. Averaging the six values we obtain the final result:

$$\frac{\lambda_{exp} - \lambda_{th}}{\lambda_{th}} = (2 \pm 8) \times 10^{-6}. \quad (2)$$

Thus, we find agreement between the measured transition wavelengths and QED calculations.

The vacuum polarization contribution, averaged over the transitions measured

Table II
Experimental X-ray wavelength values and comparison with theory (QED). Earlier published results are included.

Isotope	transition	$\lambda_{exp}(\text{pm})^a)$	reference	$\lambda_{exp}(\text{pm})^b)$	$\lambda_{th}(\text{pm})^c)$	$\frac{\lambda_{exp} - \lambda_{th}}{\lambda_{th}} (\text{ppm})$
^{24}Mg	$3d_{5/2}-2p_{3/2}$	22.05490(29)	run 15	22.05507	22.05501	3 ± 10
	$3d_{5/2}-2p_{3/2}$	22.05519(24)	run 18			
	$3d_{3/2}-2p_{1/2}$	21.98616(34)	run 18	21.98616	21.98641	-11 ± 17
^{28}Si	$3d_{5/2}-2p_{3/2}$	16.18219(57)	ref. 3			
	$3d_{5/2}-2p_{3/2}$	16.18271(56)	run 11	16.18242	16.18234	5 ± 15
	$3d_{5/2}-2p_{3/2}$	16.18240(25)	run 17			
	$3d_{3/2}-2p_{1/2}$	16.11393(40)	run 17	16.11393	16.11408	9 ± 25
^{31}P	$3d_{5/2}-2p_{3/2}$	14.08630(45)	ref. 4			
	$3d_{5/2}-2p_{3/2}$	14.08742(71)	run 19	14.08662	14.08668	-5 ± 28
	$3d_{3/2}-2p_{1/2}$	14.02144(120)	run 19	14.02144	14.01861	202 ± 89

^{a)} All experimental errors included.

^{b)} Average over all experiments.

^{c)} Ref. 8, see also ref. 7.

(with appropriate weighting factors) is 3.4×10^{-3} of the average wavelength (see e.g. Ref. 7). Result (2) thus implies that the vacuum polarization effect has been measured to be correct to $(0.6 \pm 2.4) \times 10^{-3}$.

Alternatively, if we assume that QED describes the electromagnetic interaction in muonic atoms correctly, our result can be used to put a limit on an additional muon-nucleus interaction. Such an interaction can be described by potential (1). From the corresponding energy-level shift and result (2) we deduce limits for $(g_\mu \cdot g_N)/4\pi$ as a function of m . The two solid curves in Fig. 1 correspond to the mean value of $(g_\mu \cdot g_N)/4\pi$ plus and minus one standard deviation. The calculation was done separately for each element measured; the curves show an average over all elements. Also shown in Fig. 1 (broken curves) are the limits deduced from the μ - ${}^4\text{He}$ experiment (Ref. 2); the r.m.s. radius of ${}^4\text{He}$ from Ref. 13 was used in this analysis.

This experiment provides the most stringent limit to a long range interaction (zero-mass limit) between the muon and the nucleons beyond QED. For example, if the mass m of the exchanged boson were smaller than 1 MeV, the product of coupling constants is:

$$\frac{g_\mu \cdot g_N}{4\pi} = (-4 \pm 17) \times 10^{-9}. \quad (3)$$

In case of the Weinberg-Salam theory, the muon-nuclear interaction is mediated by the Higgs boson [14]. If one assumes that the coupling of the Higgs boson to

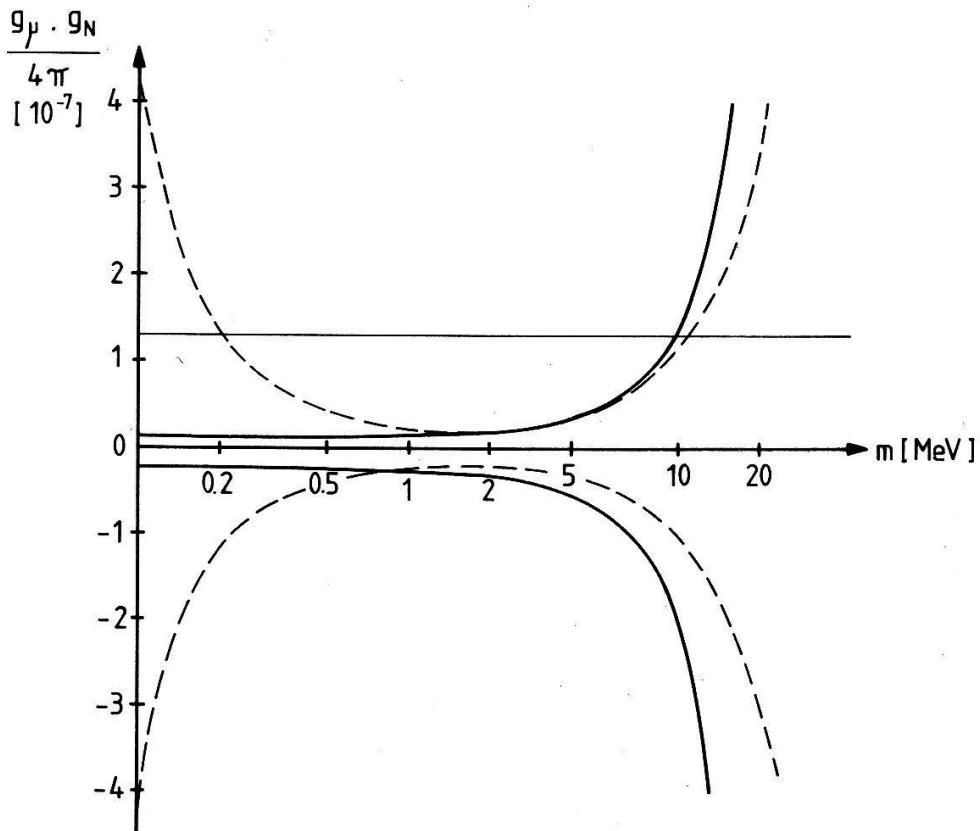


Figure 1

Limits on the product of coupling constants for a muon-nucleon interaction mediated by a boson of mass m . The solid lines are derived from equation (2). The broken curves stem from the μ - ${}^4\text{He}$ experiment [2]. The straight line is the Higgs boson interaction as predicted from the Weinberg-Salam model.

the nucleons is of the same form as the coupling to the leptons (proportional to the fermion mass), one finds [4]

$$\frac{g_\mu \cdot g_N}{4\pi} = 1.29 \times 10^{-7}, \quad (4)$$

independent of the boson mass. The value (4) corresponds to the straight line in Fig. 1. We obtain from (4) and the upper solid curve in Fig. 1 a lower limit for the mass of the Higgs boson:

$$m \geq 8.5 \text{ MeV (90% confidence level)} \quad (5)$$

This value is compatible with and similar to the results from experiments which are based on the *electron*-nucleon interaction mediated by the Higgs boson [15]. Within the framework of the Weinberg-Salam theory the above mass limit excludes a narrow mass range of heavy fermions [16, 17].

There is still another (third) interpretation of our result (2). In the calculation of the transition wavelengths (λ_{th}) the negative muon mass was assumed equal to the precisely measured positive muon mass [8]. If we now assume that QED is correct and there are no additional muon-nucleus interactions, then the null result of equation (2) establishes that the masses are in fact equal. Hence the CPT theorem for the muon is confirmed to within the quoted error of ± 8 ppm.

REFERENCES

- [1] L. TAUSCHER, G. BACKENSTOSS, K. FRANSSON, H. KOCH, A. NILSSON and J. DE RAEDT, *Z. Physik A285* (1978) 139; T. DUBLER, K. KÄSER, B. ROBERT-TISSOT, L. A. SCHALLER, L. SCHELLENBERG and H. SCHNEUWLY, *Nucl. Phys. A294* (1978) 397; C. K. HARGROVE, E. P. HINCKS, R. J. MCKEE, H. MES, A. L. CARTER, M. S. DIXIT, D. KESSLER, J. S. WADDEN, H. L. ANDERSON and A. ZEHNDER, *Phys. Rev. Lett.* 39 (1977) 307; and references cited therein.
- [2] G. CARBONI, G. GORINI, L. PALFFY, F. PALMONARI, G. TORELLI and E. ZAVATTINI, *Nucl. Phys. A278* (1977) 381; E. ZAVATTINI, Proceedings of the 7th International Conference on High-Energy Physics and Nuclear Structure, Zurich, 29 August-2 September, Birkhäuser Verlag, 1977 (Ed. M. P. LOCHER); G. CARBONI, G. GORINI, E. IACOPINI, F. PALMONARI, G. TORELLI and E. ZAVATTINI, *Phys. Lett. 73B* (1978) 229.
- [3] R. EICHLER, B. AAS, W. BEER, I. BELTRAMI, P. EBERSOLD, TH. v. LEDEBUR, H. J. LEISI, W. W. SAPP, J.-C. DOUSSE, J. KERN and W. SCHWITZ, *Phys. Lett. 76B* (1978) 231.
- [4] B. AAS, W. BEER, I. BELTRAMI, K. BONGARDT, P. EBERSOLD, R. EICHLER, TH. v. LEDEBUR, H. J. LEISI, W. W. SAPP, J.-A. PINSTON, J. KERN, R. LANNERS and W. SCHWITZ, *Nucl. Phys. A329* (1979) 450.
- [5] S. D. DRELL, SLAC-PUB-2222, October 1978; B. E. LAUTRUP, A. PETERMAN, E. DE RAFAEL, *Phys. Repts. 3C* (1972) 193.
- [6] Partial results have been communicated at the Vancouver Conference, see ref. (7). A comprehensive paper on this work has been submitted for publication to *Nuclear Physics*.
- [7] H. J. LEISI, *Nucl. Phys. A335* (1980) 3.
- [8] B. AAS, R. EICHLER and H. J. LEISI, to be published.
- [9] R. JACKIW and S. WEINBERG, *Phys. Rev. D5* (1972) 239.
- [10] S. L. ADLER, *Phys. Rev. D10* (1974) 3714.
- [11] E. G. KESSLER, JR., L. JACOBS, W. SCHWITZ and R. D. DESLATTES, *Nucl. Instr. Meth.* 160 (1979) 435.
- [12] B. AAS, Thesis No. 6541 ETHZ (1980), unpublished.
- [13] I. SICK, J. S. McCARTHY and R. R. WHITNEY, *Phys. Lett. 64B* (1976) 33.
- [14] S. WEINBERG, *Phys. Rev. Lett.* 19 (1967) 1264.
- [15] A summary of the results from the electron experiments can be found in Ref. 4.
- [16] H. D. POLITZER and S. WOLFRAM, *Phys. Lett. 82B* (1979) 242.
- [17] PHAM QUANG HUNG, *Phys. Rev. Lett.* 42 (1979) 873.