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**Autor:** Crawford, J.F. / Daum, M. / Eaton, G.H.  
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# Production of low energy pions by 590 MeV protons in nuclei

by **J. F. Crawford, M. Daum, G. H. Eaton, R. Frosch, J. Garzon<sup>1</sup>), H. Hirschmann<sup>2</sup>), P.-R. Kettle, J. W. McCulloch<sup>3</sup>) and E. Steiner**

SIN, Schweizerisches Institut für Nuklearforschung, CH-5234 Villigen, Switzerland

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**Abstract.** We have measured differential cross sections  $d^2\sigma/(d\Omega dT_\pi)$  for the production of charged pions by 590 MeV protons in beryllium, carbon and nickel at pion production angles of  $22.5^\circ$  and  $90^\circ$ , for pion energies from 6 MeV to 35 MeV. At the lowest pion energies the cross sections tend towards zero. From nickel there are more slow  $\pi^-$  than  $\pi^+$ ; this is attributed to Coulomb effects.

## 1. Introduction

Measurements of cross sections for the production of low energy pions are needed for the optimal design of new facilities such as surface muon beams [1] and pionic X-ray detection systems [2], at SIN and similar laboratories. In surface muon beams, the  $\mu^+$  from  $\pi^+$  decays at rest in the pion production target are collected. The relevant pions have typical ranges of a few millimetres in the production target, i.e., kinetic energies of a few MeV. In the new pionic X-ray facilities the experimental target is placed close to the pion production target; again the relevant  $\pi^-$  mesons are those with kinetic energies of a few MeV.

In a recent survey [3] of the literature on pion production by protons in the energy range of the "meson factories" ( $400 \text{ MeV} \leq T_p \leq 800 \text{ MeV}$ ) only a few published data for pion energies below 20 MeV were found. Measurements at low pion energies are difficult because of the large effects of ionization energy loss, multiple scattering and decay of the produced pions.

We have measured differential cross sections  $d^2\sigma/(d\Omega dT_\pi)$  for the production of charged pions by 590 MeV protons in beryllium, carbon and nickel at pion production angles of  $22.5^\circ$  and  $90^\circ$ , for pion energies from 6 MeV to 35 MeV (all quantities in the lab system). We used specially thin pion production targets in the main extracted proton beam of the SIN accelerator. As pion spectrometers we used the secondary beam transport systems  $\pi M3$  and  $\pi E3$  [4]. These systems are

<sup>1)</sup> Present address: Dto Fisica Fundamental, Universidad Autonoma, Madrid-Cantoblanco, Spain.

<sup>2)</sup> Present address: EIR, Eidgenössisches Institut für Reaktorforschung, CH-5303 Würenlingen, Switzerland.

<sup>3)</sup> Present address: Marconi Space and Defence Systems, The Grove, Warren Lane, Stanmore, Middlesex HA7 4LY, England.

suitable for our measurements because they are doubly focusing (i.e. focusing both horizontally and vertically) and thus allow a high signal-to-background ratio in the detector. Also, the channels are equipped with the vacuum system and shielding necessary for our purpose.

## 2. Experimental method

The layout of the  $\pi M3$  ( $22.5^\circ$ ) channel is shown in Fig. 1. The 590 MeV proton beam was operated at currents ranging from 6 to 102 microampères. Radiation cooled rotating wheel pion production targets [4] with thin foils were used. For the  $\pi M3$  measurements the foil thickness was 3 mm for beryllium and 0.2 mm for nickel. The angle  $\theta_1$  between the proton beam and the normal to the target foil surface was  $67.5^\circ$  and the angle  $\theta_2$  between the central pion trajectory and the normal to the target foil surface was  $45^\circ$ . For the  $\pi E3$  ( $90^\circ$ ) measurements on carbon and nickel the angles  $\theta_1$  and  $\theta_2$  as defined above were  $60^\circ$  and  $30^\circ$ , respectively. Here a 0.2 mm nickel foil and a 1 mm graphite foil were used. The  $90^\circ$ -beryllium-data were obtained with the standard SIN production target (thickness 6 mm;  $\theta_1 = 90^\circ$ ,  $\theta_2 = 0^\circ$ ).

In the  $\pi M3$  channel the vacuum systems of the production target and the pion channel are separated by two 0.4 mm thick aluminium windows at a distance of 9.5 cm from the production target. The  $\pi E3$  vacuum chamber is connected without windows to the production target vacuum; in this channel there were

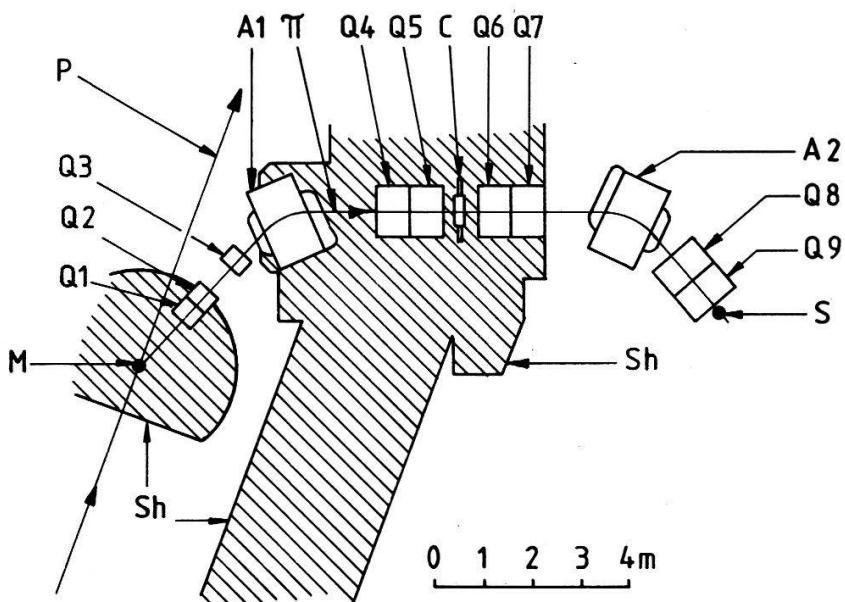


Figure 1

Layout of the  $\pi M3$  pion channel used for the measurements at a pion production angle of  $22.5^\circ$ .  $M$ : pion production target;  $p$ : 590 MeV proton beam;  $\pi$ : central pion trajectory;  $Q_i$ : quadrupole magnets;  $A_i$ : dipole magnets;  $C$ : momentum-defining collimator;  $S$ : channel end (scintillation counter);  $Sh$ : shielding (iron and concrete).

0.2 mm mylar windows upstream and downstream of the momentum defining collimator system.

The magnetic pion channels were operated at central momenta from 40 to 102 MeV/c. In  $\pi M3$  (see Fig. 1) the momentum was chosen using the bending magnet  $A_1$ . The two quadrupole doublets ( $Q_4, Q_5$ ) and ( $Q_6, Q_7$ ) were set for an achromatic beam transport from the production target (point  $M$ ) to the channel end (point  $S$ ). The triplet ( $Q_1, Q_2, Q_3$ ) imaged the target point  $M$  onto the center  $C$  of the momentum-defining colimator. Finally the bending magnet  $A_2$  and the doublet ( $Q_8, Q_9$ ) were tuned to image point  $C$  onto the channel end point  $S$ . The channel  $\pi E3$  is a similar achromatic system.

At the channel end the pions passed through a 0.1 mm thick mylar vacuum window and were detected in a plastic scintillator. The pions were identified in the large background of electrons or positrons and muons by their pulse height in the scintillator and by their time of flight (TOF) from the production target to the scintillator. The time-to-amplitude converter was started by a pulse in the scintillator and was stopped by the RF signal from the accelerator. Because the SIN proton beam consists of narrow pulses separated by 20 nanoseconds, the TOF method allows one to determine the difference between the particle flight time and an integer multiple of 20 nsec; this is sufficient for our purpose.

The incident proton beam intensity was monitored with pick-up probes [5]. The acceptance of the pion channels was determined using the Monte-Carlo program TURTLE [6], taking into account the magnet settings and apertures of the channel, the energy loss and multiple scattering of the pions in the windows and in the production target, as well as pion decay.

### 3. Results

The resulting pion production cross sections are presented in Table I and also in Figs. 2 to 6. The quoted pion energies were obtained by adding the energy corresponding to the channel momentum settings and the average energy loss in the production target and, for the  $\pi M3$  data, in the vacuum windows. The quoted uncertainties of the cross sections are estimates of the errors in the background subtraction and acceptance calculation; the number of counted pions is so large, that the statistical uncertainties are negligible in all cases. In Figs. 2 to 6 data points from Ref. 3 have been included for comparison. Our data for pion energies above 24 MeV are seen to agree with Ref. 3.

Our data have also been compared with those obtained by Batusov et al. [7]. These authors have used nuclear emulsions to measure  $\pi^\pm$  production cross sections of C, Al, Cu and Pb for  $T_p = 660$  MeV,  $\theta_\pi = 105^\circ$  and  $T_\pi$  down to 11 MeV. For pions of either sign with  $T_\pi = 11$  MeV produced in carbon the cross section values of Ref. 7 ( $T_p = 660$  MeV,  $\theta_\pi = 105^\circ$ ) are larger than the values interpolated from our data shown in Fig. 3 ( $T_p = 600$  MeV,  $\theta_\pi = 90^\circ$ ) by a factor of about 1.6. The discrepancy could at least in part be due to a rise of the cross section with both  $T_p$  and  $\theta_\pi$ . At higher pion energies the difference between our carbon data at  $90^\circ$  and those of Ref. 7 is smaller (about 10% at  $T_\pi = 35$  MeV).

Table 1

Measured nuclear differential cross sections for charged pion production by 590 MeV protons.  $\theta_\pi$ : Pion production angle.  $T_\pi$ : Pion kinetic energy. All quantities in the lab. system.

$\theta_\pi$ degrees	Target	$T_\pi$ MeV	$d^2\sigma/(d\Omega dT_\pi)$	$\mu b/(\text{sr. MeV})$
			$\pi^+$	$\pi^-$
22.5	Be	13.3	$2.11 \pm 0.46$	$0.77 \pm 0.17$
		15.8	$2.05 \pm 0.35$	$0.80 \pm 0.14$
		25.3	$4.30 \pm 0.73$	$1.46 \pm 0.25$
		31.0	$5.80 \pm 0.99$	$1.78 \pm 0.30$
90	Ni	11.3	$6.0 \pm 1.8$	$6.8 \pm 2.0$
		14.1	$6.9 \pm 1.8$	$7.5 \pm 1.9$
		24.1	$17.6 \pm 4.6$	$12.5 \pm 3.3$
		30.1	$21.4 \pm 5.6$	$11.7 \pm 3.0$
90	Be	10.9	$3.21 \pm 0.81$	$1.04 \pm 0.27$
		11.4	$2.78 \pm 0.79$	$1.28 \pm 0.30$
		11.8	$3.86 \pm 0.98$	$1.31 \pm 0.35$
		19.4	$4.9 \pm 1.2$	$1.56 \pm 0.40$
		24.6	$6.0 \pm 1.5$	$2.12 \pm 0.51$
		35.0	$10.2 \pm 2.4$	$2.80 \pm 0.67$
90	C	7.0	$2.48 \pm 0.47$	$1.09 \pm 0.13$
		7.6	$2.85 \pm 0.59$	$1.16 \pm 0.14$
		8.2	$4.06 \pm 0.50$	$1.35 \pm 0.17$
		17.2	$6.81 \pm 0.84$	$1.90 \pm 0.23$
		22.8	$9.5 \pm 1.2$	$2.26 \pm 0.28$
		33.6	$14.1 \pm 1.7$	$2.90 \pm 0.36$
90	Ni	6.4	$2.02 \pm 0.39$	$5.63 \pm 0.69$
		7.1	$3.21 \pm 0.66$	$6.59 \pm 0.81$
		7.8	$4.65 \pm 0.57$	$7.92 \pm 0.97$
		16.9	$15.4 \pm 1.9$	$9.4 \pm 1.2$
		22.6	$23.0 \pm 2.8$	$11.7 \pm 1.4$
		33.5	$38.2 \pm 4.7$	$12.4 \pm 1.5$

#### 4. Conclusions

We conclude from our data that in all three nuclei comparatively few pions are produced with small kinetic energies. For beryllium and carbon the differential  $\pi^+$  production cross section  $d^2\sigma/(d\Omega dT_\pi)$  is roughly proportional to the pion energy  $T_\pi$  for small  $T_\pi$ . This behaviour agrees with the isobar model [8] of pion production, i.e. with the assumption that the incoming proton undergoes the reaction  $p + N \rightarrow \Delta + N'$  (where  $N$  and  $N'$  are nucleons) and the pion is created in the decay of the  $\Delta$  particle. According to this model [8] the cross section  $d^2\sigma/(d\Omega dT_\pi)$  is proportional to  $T_\pi^{1/2}$  for  $T_\pi \leq 5$  MeV, then rises approximately linearly with  $T_\pi$  in agreement with our data for the light nuclei. For nickel also, the  $T_\pi$  dependence of the measured cross section is compatible with a linearly rising function of  $T_\pi$ ; however for nickel the best fit straight line crosses the



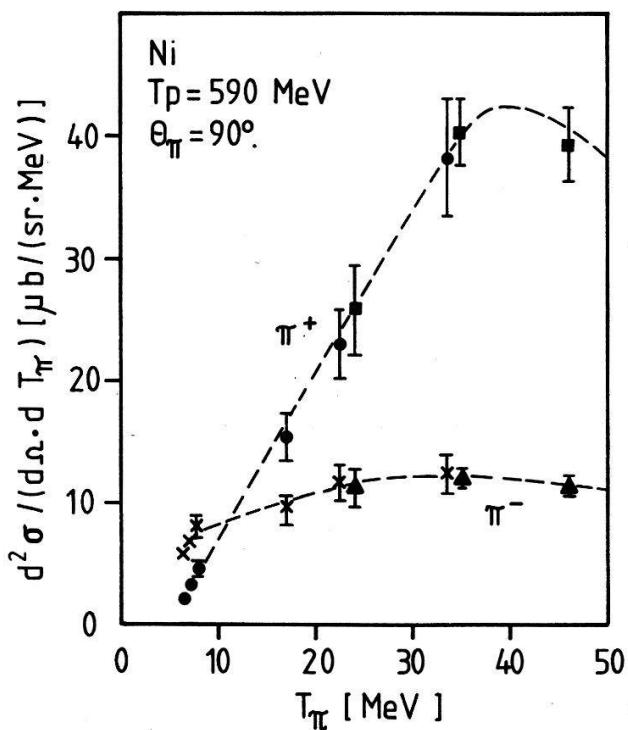


Figure 2

Measured nuclear differential cross sections for charged pion production by 590 MeV protons in nickel at a pion production angle  $\theta_\pi$  of  $90^\circ$ ;  $T_\pi$  = pion kinetic energy. There are more  $\pi^-$  than  $\pi^+$  for  $T_\pi \leq 10$  MeV. This crossover is attributed to the Coulomb force between the pion and the nuclear protons (see text). The dashed curve has been hand-drawn through the points. The cross sections measured in the present experiment are shown with full circles ( $\pi^+$ ) and crosses ( $\pi^-$ ); data from Ref. 3 are indicated with squares ( $\pi^+$ ) and triangles ( $\pi^-$ ).

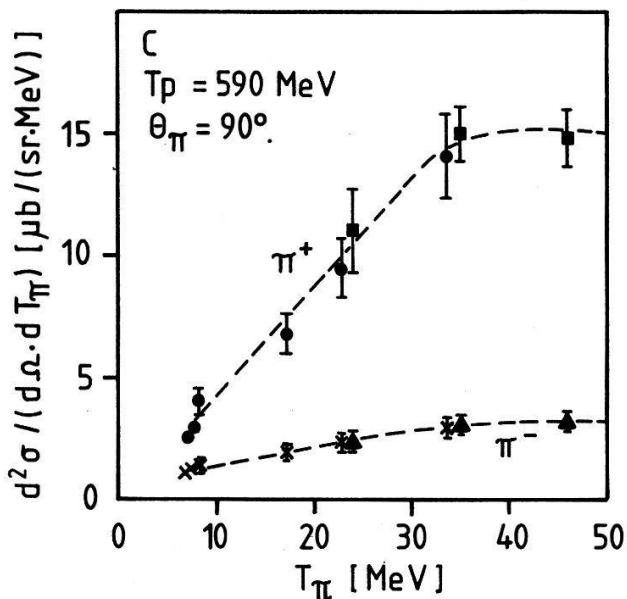


Figure 3

As Fig. 2; cross sections for carbon,  $\theta_\pi = 90^\circ$ .

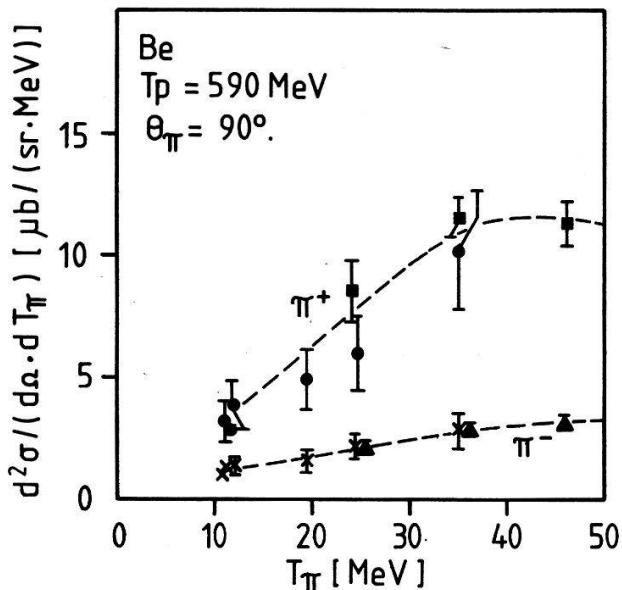


Figure 4  
As Fig. 2; cross sections for beryllium,  $\theta_\pi = 90^\circ$ .

horizontal axis at  $T_{\pi^+} \approx +5$  MeV for both production angles ( $22.5^\circ$  and  $90^\circ$ ), in disagreement with the simple isobar model, from which a slightly negative  $T_\pi$  value for the intercept is predicted. This shift in pion energy can be attributed to the Coulomb repulsion between the  $\pi^+$  meson and the protons of the residual nucleus; i.e., the  $T_\pi$  dependence of the differential cross section for  $\pi^+$  production from nickel agrees with the isobar model, as for the lighter nuclei, if the

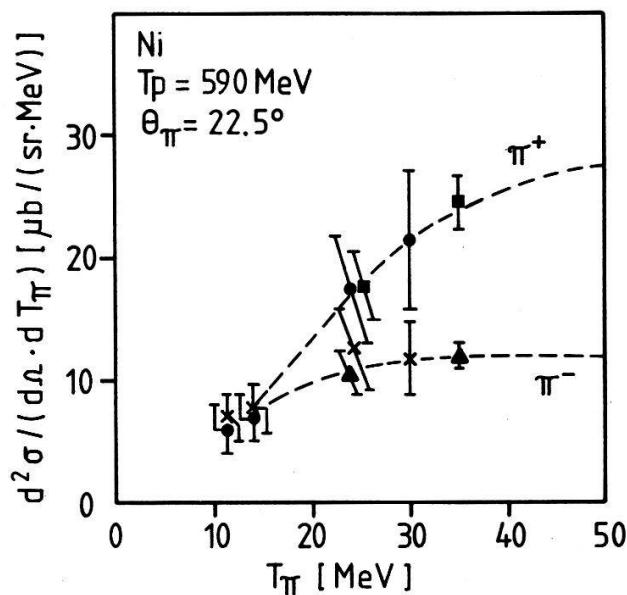


Figure 5  
As Fig. 2; cross sections for nickel,  $\theta_\pi = 22.5^\circ$ .

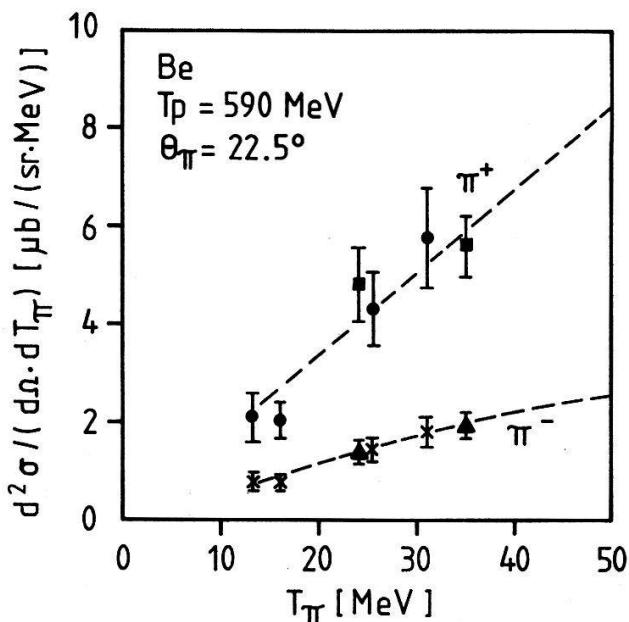


Figure 6  
As Fig. 2; cross sections for beryllium,  $\theta_\pi = 22.5^\circ$ .

estimated pion energy gain from the Coulomb repulsion (about 5 MeV for nickel) is subtracted from the measured pion energy.

The differential cross sections for  $\pi^-$  production are also consistent with a linear rise with the pion energy  $T_\pi$ . The  $\pi^-$  spectra from nickel appear shifted to lower pion energies by a few MeV if compared to the spectra from the lighter nuclei; this can again be attributed to the Coulomb force between the pion and the nuclear protons. As a consequence, at pion energies below about 10 MeV more  $\pi^-$  than  $\pi^+$  are produced from nickel, whereas for carbon and beryllium the accustomed relative abundance of  $\pi^+$  and  $\pi^-$  is observed at all pion energies.

The fact that more slow  $\pi^-$  than  $\pi^+$  are produced from heavy nuclei has been discussed before, e.g. by Kostanashvili et al. [9] who studied the energy spectra of slow  $\pi^+$  and  $\pi^-$  produced in nuclear emulsion by protons with  $T_p = 600$  MeV and 9 GeV and by  $\pi^-$  with  $T_\pi$  (incident) = 60 GeV ( $T_{\pi^+}$  from 0.5 to 20 MeV; no absolute production cross sections are given). In all cases studied in Ref. 9 the  $\pi^-$  yield is larger than the  $\pi^+$  yield, e.g. by a factor 10 at  $T_\pi \approx 5$  MeV.

The angular distributions of low energy charged pions produced by 590 MeV protons in beryllium and nickel are shown in Fig. 7. These diagrams have been obtained from smooth lines drawn through the data points of this experiment as well as those of Ref. 3. It is seen that slow  $\pi^+$  predominantly go backward, again in agreement with the isobar model. A weaker backward trend is also observed for  $\pi^-$  produced in beryllium, whereas the  $\pi^-$  from nickel are approximately isotropic. The corresponding  $\pi^+$  stop densities at the surface of a 5 cm long cylindrical beryllium production target are indicated in Fig. 8. From this figure it is evident that the initial section of a surface muon beam [1] should not be

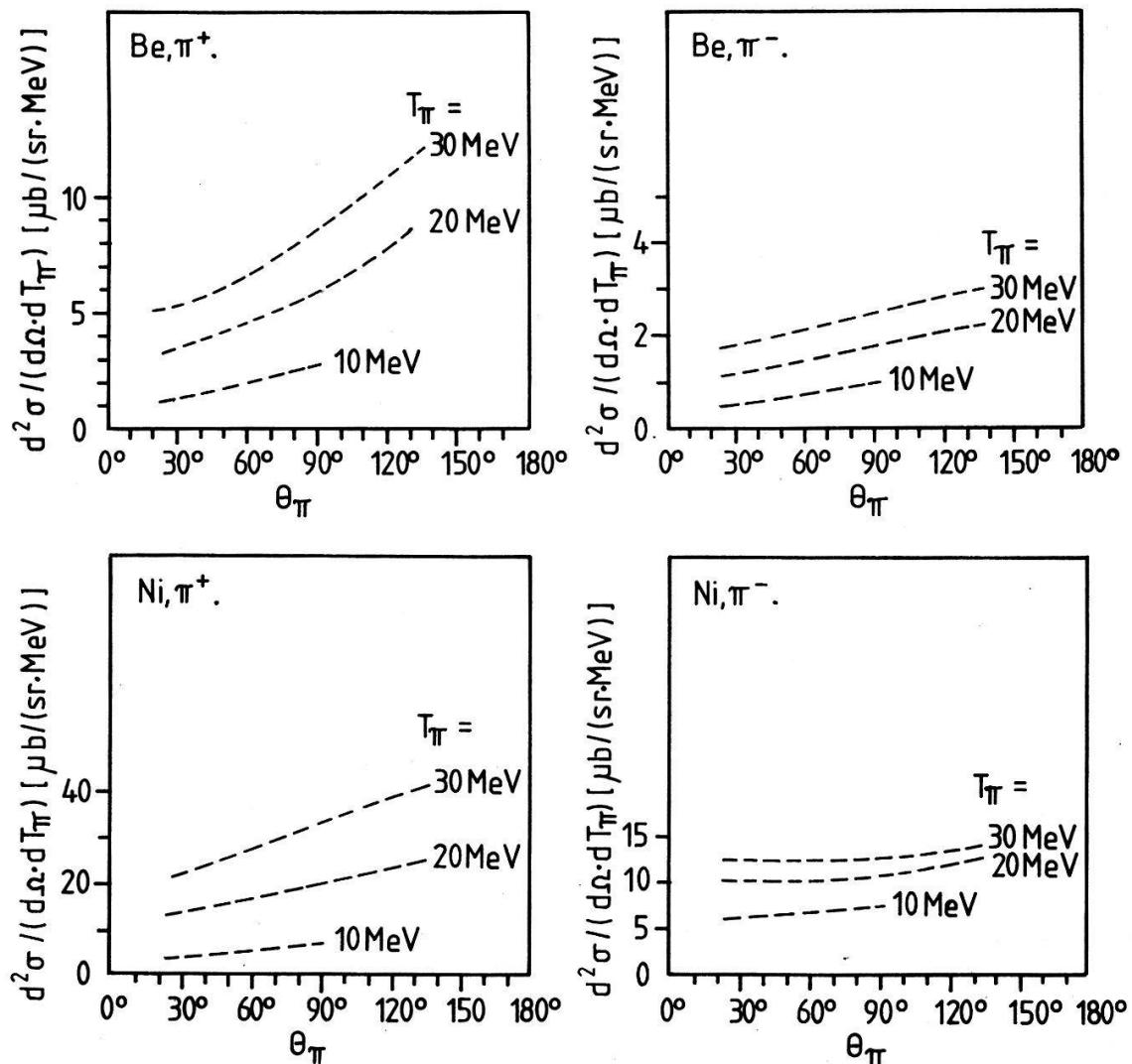


Figure 7

Angular distributions of low energy pions produced in beryllium or nickel by 590 MeV protons.  $\theta_\pi$  = pion production angle.  $T_\pi$  = kinetic energy of pion. The curves have been obtained from smooth lines drawn through the data points of Figs. 2 to 6 and through the large angle points of Ref. 3.

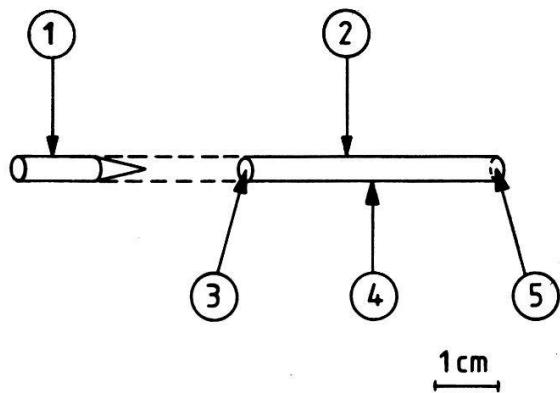


Figure 8

Positive pion stop densities at the surface of a cylindrical beryllium production target. (1) Incident proton beam;  $T_p = 590$  MeV.  $I = 100 \mu\text{A}$ ; (2) production target; (3) stop density  $3.3 \times 10^{10} \text{ g}^{-1} \text{ s}^{-1}$ ; (4) stop density  $2.5 \times 10^{10} \text{ g}^{-1} \text{ s}^{-1}$ ; (5) stop density  $1.7 \times 10^{10} \text{ g}^{-1} \text{ s}^{-1}$ . These stop densities have been calculated from the data of this experiment and from Ref. 3, under the assumption of a uniform irradiation with protons on the front face of the target. They imply that comparatively few surface muons go in the forward direction.

oriented in the forward direction. For the design of pionic X-ray facilities according to Ref. 2 it should be kept in mind that due to the Coulomb effect discussed above comparatively many slow  $\pi^-$  are produced from heavy elements.

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