

Objektyp: **ReferenceList**

Zeitschrift: **L'Enseignement Mathématique**

Band (Jahr): **33 (1987)**

Heft 1-2: **L'ENSEIGNEMENT MATHÉMATIQUE**

PDF erstellt am: **22.09.2024**

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$S \in H^0(\bar{M}, K^{-1})$ . This would imply that either  $K$  is trivial on  $M$  or  $H^0(\bar{M}, K^n) = 0$  for every  $m > 0$  and hence the Kodaira dimension of  $\bar{M}^2$  would either be  $-\infty$  or 0. This is because if  $t \in H^0(\bar{M}, K^n)$ , then  $t \cdot S^n$  is a holomorphic function on  $M$  and hence constant; since  $S$  is zero somewhere unless  $K$  is trivial, we have  $t \cdot S^n = 0$ , so that  $t = 0$  unless  $K$  is trivial on  $M$ .

Since  $M$  is Kähler and simply connected, the minimal model of  $\bar{M}$  is a Kähler surface with  $K = 0$  or  $-\infty$  and  $b_1 = 0$ . When  $K = 0$ , it is either a  $K=3$  surface or Enriques' surface. When  $K = -\infty$  it is either a rational surface or a ruled surface of genus zero,  $\bar{M}^2$  is equal the minimal model blown up successively at a finite number of points, and  $M = \bar{M} \setminus \{s=0\}$  for some  $0 \neq s \in H^0(\bar{M}, K^{-1})$ . Conversely, if  $M = \bar{M} \setminus \{s=0\}$  with  $s \in H^0(\bar{M}, K^{-1})$  and  $\bar{M}$  is as above, then  $M$  should admit a Ricci flat, complete, Kähler metric. In higher dimensions, the situation is much more complicated.

In physics, the following question has been studied. Is a Ricci flat metric with a suitable locally asymptotic property actually unique? This is the case when the metric is asymptotically flat. One would also like to know what happens when the metric is locally asymptotic to a cone. Perhaps assuming that the metric is Kähler may make this problem easier.

The existence of Ricci flat metrics has many applications. For example, using Ricci flat metrics, Siu [S1] proved that any surface  $M^2$  with  $c_1(M) = 0$  and  $H^1(M, \mathbf{R}) = 0$  must be Kähler. See also Todorov [To] for higher dimensions. One can also ask the following question: Let  $M^{2n}$  be a simply-connected, compact, complex manifold where  $n \geq 2$ . If there exists a non-degenerate 2-form  $\omega \in H^{2,0}(M)$ , is  $M$  then Kähler? Todorov claimed that  $M$  is Kähler under an additional assumption:  $\dim H^{2,0}(M) = 1$ .

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(Reçu le 6 mai 1986)

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