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7.2 THEOREM. *The centre of  $SB_n$  is all of  $SB_n$  for  $n = 2$ . But in case  $n \geq 3$  it is the same as the (infinite cyclic) centre of  $B_n \subset SB_n$ , generated by  $\Delta^2$ .  $\square$*

7.3 THEOREM. *Under the natural inclusion, the centraliser of  $SB_r$  in  $SB_n$ ,  $r \leq n$ , is generated as a monoid by the generators (see Theorem 4.4) of  $C(r, n)$ :*

$$\sigma_{r+1}, \sigma_{r+2}, \dots, \sigma_{n-1}, A_{r+1}, \dots, A_n, C,$$

*together with their inverses and the singular generators:*

$$\begin{aligned} & \tau_{r+1}, \dots, \tau_{n-1} && \text{if } r \geq 3, \text{ or} \\ & \tau_1, \tau_3, \tau_4, \dots, \tau_{n-1} && \text{if } r = 2. \end{aligned} \quad \square$$

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