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7.2 THEOREM. *The centre of SB_n is all of SB_n for $n = 2$. But in case $n \geq 3$ it is the same as the (infinite cyclic) centre of $B_n \subset SB_n$, generated by Δ^2 .* \square

7.3 THEOREM. *Under the natural inclusion, the centraliser of SB_r in SB_n , $r \leq n$, is generated as a monoid by the generators (see Theorem 4.4) of $C(r, n)$:*

$$\sigma_{r+1}, \sigma_{r+2}, \dots, \sigma_{n-1}, A_{r+1}, \dots, A_n, C,$$

together with their inverses and the singular generators:

$$\begin{aligned} \tau_{r+1}, \dots, \tau_{n-1} & \quad \text{if } r \geq 3, \text{ or} \\ \tau_1, \tau_3, \tau_4, \dots, \tau_{n-1} & \quad \text{if } r = 2. \end{aligned}$$

 \square

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