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NOTE (added in proof)

The following recent papers are intimately related to the topics discussed above:

- BELTRAMETTI, E. Recent Facts in Quantum Logic and Surroundings. Contained in the book *Recent Developments in Quantum Logic*. *Proc. Intern. Symp. Quantum Logic*, Cologne, Germany 1984, ed. P. Mittelstaedt, E.-W. Stachow, B.I.-Wissenschaftsverlag Mannheim/Wien/Zürich 1985, pp. 24-25.
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- Different orthomodular orthocomplementations on a non-modular lattice. *Submitted*.
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- KÜNZI, U.-M. A Hilbert lattice with a small automorphism group. *Submitted*.

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