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Autor: Hazewinkel, Michiel / Martin, Clyde F.

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11.11. *Remarks.* It is conceivable that the family (11.2) contains all the families of representations one needs to prove the Snapper etc. result by means of deformation arguments. Quite generally we would like to pose the question which representations occur in this family and investigate universal families (for continuous families) of homomorphisms of representations from some fixed representation space into another.

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Michiel Hazewinkel

Dept. of Mathematics
P.O. Box 1738
Erasmus Univ. Rotterdam
3000 DR, Rotterdam
The Netherlands

Clyde Martin

Dept. of Mathematics and Statistics
Case Institute of Technology
Case Western Reserve Univ.
Cleveland, OHIO 44106

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