Zeitschrift: L'Enseignement Mathématique
Herausgeber: Commission Internationale de l'Enseignement Mathématique
Band: 23 (1977)
Heft: 1-2: L'ENSEIGNEMENT MATHÉMATIQUE

Artikel: THE GELFAND-NAIMARK THEOREMS FOR C*-ALGEBRAS
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Bibliographie
DOI: https://doi.org/10.5169/seals-48924

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tion is the Gelfand-Naimark-Segal construction discussed earlier in this article.

A substantial literature has now emerged from this new algebraic point of view and a recent book by G. Emch [18] has been written with the express purpose of offering a systematic introduction to the ideas and techniques of the C*-algebra approach to physical problems. The authors recommend this book to the reader who would like to pursue this subject further. The book contains a bibliography of more than four hundred items which should aid the interested reader in his study of this new and interesting application of operator algebras.

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(Reçu le 4 février 1977)

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