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ON IMPLICIT FUNCTION THEOREMS AND THE EXISTENCE OF SOLUTIONS OF NON-LINEAR EQUATIONS *

by Hans H. Ehrmann

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1. Introduction.

This paper presents some existence theorems for the solutions of certain non-linear equations, both local and global theorems. The generality, in particular, of the local theorems is determined largely by the spaces which contain the domain and the range

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