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## Explicit imbedding of the (punctured) disc into $\mathbb{C}^2$

H. ALEXANDER

1. According to a basic result of Bishop [3] and Narasimhan [7], every  $n$ -dimensional Stein manifold can be imbedded (via a holomorphic, proper, one-to-one, non-singular mapping) as a closed complex submanifold of  $\mathbb{C}^{2n+1}$ . Forster [4] has shown that the dimension  $2n+1$  can be replaced by  $2n$  when  $n \geq 2$ . Applied to open Riemann surfaces ( $n = 1$ ), these results yield imbeddings into  $\mathbb{C}^3$ . It seems likely however that every open Riemann surface can be imbedded into  $\mathbb{C}^2$ . That this is the case for the open unit disc was proved by Kasahara and Nishino [5] by an argument that employs the well-known mapping of Fatou (and Bieberbach). Laufer [6] observed that their idea can be adapted to imbed into  $\mathbb{C}^2$  every planar annulus both of whose boundary components do not degenerate to a point; i.e., after a conformal map, annuli of the form  $\{z \in \mathbb{C} : r < |z| < 1\}$  for  $r > 0$ . The case of the punctured disc  $\Delta = \{z \in \mathbb{C} : 0 < |z| < 1\}$  was left open by Laufer and does not seem to be amenable to the technique of [5] and [6].

In this note we shall give an explicit imbedding of  $\Delta$  into  $\mathbb{C}^2$ . Namely, we write down two mapping functions, the elliptic modular function  $\lambda$  together with a simple rational expression of  $\lambda$  and its derivative  $\lambda'$  (transplanted from the Poincaré upper half plane to  $\Delta$ ) and then we verify that they do yield an imbedding. The second function will have a pole at the origin. By a minor modification, we remove this pole and get an explicit imbedding of the open unit disc  $U$  into  $\mathbb{C}^2$ . This is of interest because of the indirectness of the Kasahara–Nishino imbedding. Other proper holomorphic mappings of  $U$  into  $\mathbb{C}^2$ , in which one of the components is a universal covering map of a plane domain, were constructed in [2], but these will not generally be one-to-one.

2. We shall begin by recalling a few basic facts about the elliptic modular function  $\lambda$  [1]. Let  $\Pi = \{\tau \in \mathbb{C} : \text{Im } \tau > 0\}$  be the Poincaré upper half plane and put  $\Omega = \{\tau \in \Pi : 0 < \text{Re } \tau < 1 \text{ and } |\tau - \frac{1}{2}| > \frac{1}{2}\}$ . Let  $\lambda$  be the conformal map of  $\Omega$  onto  $\Pi$  such that  $\lambda(0) = 1$ ,  $\lambda(1) = \infty$  and  $\lambda(\infty) = 0$ . Then, by reflection,  $\lambda$  can be extended over the whole of  $\Pi$  and represents  $\Pi$  as the universal covering surface of  $\mathbb{C} \setminus \{0, 1\}$ . The group  $G$  of covering transformations is the set of linear transformations  $S(\tau) = (a\tau + b)/(c\tau + d)$  where  $a$  and  $d$  are odd integers,  $b$  and  $c$  are even

integers and  $ad - bc = 1$ . We write  $\tau_1 \equiv \tau_2 \pmod{G}$  if and only if there exists  $S \in G$  with  $S\tau_2 = \tau_1$ . Then  $\lambda(\tau_1) = \lambda(\tau_2)$  if and only if  $\tau_1 \equiv \tau_2 \pmod{G}$ . Thus  $\lambda \circ S = \lambda$  for  $S \in G$  and, differentiating, we get  $\lambda' \circ S \cdot S' = \lambda'$  for  $S \in G$ . Note, for  $S = (a\tau + b)/(c\tau + d) \in G$ , that  $S'(\tau) = 1/(c\tau + d)^2$ . We shall also use the functional equation  $\lambda(-1/\tau) = 1 - \lambda(\tau)$ . This can be seen by observing, via a reflection in the imaginary axis, that  $\tau \rightarrow \lambda(-1/\tau)$  maps  $\Omega$  to the lower half plane, hence  $\tau \rightarrow 1 - \lambda(-1/\tau)$  maps  $\Omega$  to  $\Pi$  and agrees with  $\lambda$  at the vertices of  $\Omega$ , consequently the two mappings are the same.

Let  $H = \{S \in G : S(z) \equiv z + 2n, n \in \mathbf{Z}\}$  be the subgroup of translations in  $G$ . Consider the map  $E : \Pi \rightarrow \Delta$  given by  $E(\tau) = e^{i\pi\tau}$ . Then  $E(\tau_1) = E(\tau_2)$  if and only if  $\tau_1 \equiv \tau_2 \pmod{H}$ . This allows us to identify  $\Delta$  with the quotient space  $\Pi/H$ . Observe, for  $S(\tau) = (a\tau + b)/(c\tau + d) \in G$ , that  $S \in H$  if and only if  $c = 0$  (because  $c = 0$  implies  $ad = 1$  implies  $a/d = 1$ ). If  $S \in H$ , then  $S' \equiv 1$  and so  $\lambda' \circ S \equiv \lambda'$ ; i.e.,  $\lambda$  and  $\lambda'$  are both well-defined on  $\Pi/H$ . We can now state our first result. Let  $f = \lambda'/(\lambda^2(1 - \lambda))$ .

**THEOREM 1.** *The mapping  $F = (\lambda, f)$  defines a proper, one-to-one, non-singular, holomorphic imbedding of  $\Pi/H$  into  $\mathbf{C}^2$ .*

Observe that  $F$  is non-singular because  $\lambda' \neq 0$  on  $\Pi$ . We first verify that  $F$  is one-to-one.

**LEMMA 1.** (a) *The functions  $\lambda$  and  $\lambda'$  separate the points of  $\Pi/H$ .* (b)  *$F$  is one-to-one on  $\Pi/H$ .*

*Proof.* (a). We suppose (i)  $\lambda(\tau_1) = \lambda(\tau_2)$  and (ii)  $\lambda'(\tau_1) = \lambda'(\tau_2)$  and must show that  $\tau_1 \equiv \tau_2 \pmod{H}$ . By (i), there is  $S \in G$  such that  $S(\tau_2) = \tau_1$ . In  $\lambda'(S(\tau))$   $S'(\tau) = \lambda'(\tau)$  put  $\tau = \tau_2$  and get  $\lambda'(\tau_1) S'(\tau_2) = \lambda'(\tau_2)$ . Using (ii) we conclude  $S'(\tau_2) = 1$ . Writing  $S = (a\tau + b)/(c\tau + d)$  we have  $(c\tau_2 + d)^2 = 1$ ; i.e.,  $c\tau_2 + d = \pm 1$ . Taking imaginary parts yields  $c \operatorname{Im} \tau_2 = 0$ . Hence  $c = 0$  and so  $S \in H$ ; i.e.,  $\tau_1 \equiv \tau_2 \pmod{H}$ . (b) If  $F(\tau_1) = F(\tau_2)$ , then  $\lambda(\tau_1) = \lambda(\tau_2)$  and  $\lambda'(\tau_1) = \lambda^2(\tau_1)(1 - \lambda(\tau_1))f(\tau_1) = \lambda^2(\tau_2)(1 - \lambda(\tau_2))f(\tau_2) = \lambda'(\tau_2)$ . Therefore  $\tau_1 \equiv \tau_2 \pmod{H}$ .

3. We shall collect a few elementary facts needed to verify that  $F$  is proper. For  $\tau \in \Pi$  with  $0 \leq \operatorname{Re} \tau \leq 2$ , define  $\tau^* = 2 - \bar{\tau}$ ,  $0 \leq \operatorname{Re} \tau^* \leq 2$ . By reflection of points of  $\Omega$  in the line  $\operatorname{Re} \tau = 1$  and differentiation we get

**LEMMA 2.** *For  $0 \leq \operatorname{Re} \tau \leq 2$ ,  $\lambda(\tau) = \bar{\lambda}(\tau^*)$  and  $\lambda'(\tau) = -\bar{\lambda}'(\tau^*)$ .*

LEMMA 3. ("Schwarz lemma"). For  $S \in G$  and  $\tau_1, \tau_2 \in \Pi$ , if  $S\tau_2 = \tau_1$ , then  $|S'(\tau_2)| = \text{Im } \tau_1 / \text{Im } \tau_2$ .

*Proof.* By reflection in the real axis,  $S\bar{\tau}_2 = \bar{\tau}_1$ . Hence

$$\frac{S - \tau_1}{S - \bar{\tau}_1} = k \frac{\tau - \tau_2}{\tau - \bar{\tau}_2}.$$

As  $S$  is real on the real axis we get  $|k| = 1$ . Now differentiate this relation and put  $\tau = \tau_2$ .

LEMMA 4. As  $\tau$  converges to  $\infty$  in  $\bar{\Omega}$ ,  $\lambda'/\lambda$  converges to  $i\pi$ . Consequently  $\lambda'/\lambda^2$  converges to  $\infty$ .

*Proof.* The map  $\tau \rightarrow e^{i\pi\tau}$  is a one-to-one mapping of  $\Omega$  into  $\Pi$  and the image contains  $\Pi \cap \{z \in \mathbb{C} : |z| < \varepsilon\}$  for some  $\varepsilon > 0$ . The map  $e^{i\pi\tau} \circ (\lambda|_{\Omega})^{-1}$  is defined on  $\Pi$ , is real on the real axis, and, by reflection, extends to be an analytic function  $\Psi$  defined near  $z = 0$ . By the argument principle,  $\Psi'(0) \neq 0$ . Thus we have  $(e^{i\pi\tau} \circ \lambda^{-1})(z) = \Psi(z)$  near  $z = 0$ . Putting  $z = \lambda(\tau)$ , we get  $e^{i\pi\tau} = \Psi(\lambda(\tau))$ . For the inverse  $\sigma = \Psi^{-1}$  with  $\sigma(0) = 0$  and  $\sigma'(0) = \beta \neq 0$ , we have  $\sigma(e^{i\pi\tau}) = \lambda(\tau)$ . Differentiating,  $\sigma'(e^{i\pi\tau}) e^{i\pi\tau} i\pi = \lambda'(\tau)$ . Write  $\sigma(z) = \beta z \delta(z)$  with  $\delta(0) = 1$ . Then  $(\lambda'/\lambda)(\tau) = i\pi \circ \sigma'(e^{i\pi\tau}) / (\beta \cdot \delta(e^{i\pi\tau}))$ . As  $\tau \rightarrow \infty$  in  $\bar{\Omega}$ ,  $e^{i\pi\tau} \rightarrow 0$  and so  $\sigma'(e^{i\pi\tau}) \rightarrow \beta$  and  $\delta(e^{i\pi\tau}) \rightarrow 1$ . Thus  $\lambda'/\lambda \rightarrow i\pi$ .

LEMMA 5. As  $\tau$  converges to 0 in  $\bar{\Omega}$ ,  $\tau^2 \lambda'/(1 - \lambda)$  converges to  $-i\pi$ . Consequently  $\lambda'/(1 - \lambda)$  converges to  $\infty$ .

*Proof.* Differentiating the functional equation  $\lambda(\tau) = 1 - \lambda(-\tau^{-1})$  we get  $\lambda'(\tau) = -\tau^{-2} \lambda'(-\tau^{-1})$ . Thus  $\tau^2 \lambda'(\tau)/(1 - \lambda(\tau)) = -\lambda'(-\tau^{-1})/\lambda(-\tau^{-1})$ . Reflecting in the imaginary axis gives  $\lambda(\zeta) = \bar{\lambda}(-\bar{\zeta})$  and  $\lambda'(\zeta) = -\bar{\lambda}'(-\bar{\zeta})$ . Thus, putting  $t = 1/\bar{\tau}$  we have

$$\frac{\tau^2 \lambda'(\tau)}{1 - \lambda(\tau)} = \overline{\left( \frac{\lambda'(t)}{\lambda(t)} \right)}.$$

As  $\tau \rightarrow 0$  in  $\bar{\Omega}$ ,  $t \rightarrow \infty$  in  $\bar{\Omega}$  and  $(\lambda'/\lambda)(t) \rightarrow i\pi$  by Lemma 4.

4. We can now prove that  $F = (\lambda, f)$  is a proper mapping of  $\Pi/H$  into  $\mathbb{C}^2$ . We argue by contradiction and suppose that there is a sequence  $\{z_j\} \subseteq \Pi$  with  $z_j \rightarrow \partial(\Pi/H)$  and  $M > 0$  such that (i)  $|\lambda(z_j)| \leq M$  and (ii)  $|f(z_j)| \leq M$ . Since  $F$  has period 2 we may assume that  $0 \leq \text{Re } z_j < 2$ . By Lemma 2,  $\{z_j^*\}$  is a sequence in  $\Pi$

with  $z_j^* \rightarrow \partial(\Pi/H)$  and such that (i) and (ii) hold for  $z_j^*$  in place of  $z_j$ . Thus it is no loss of generality to assume that there are  $\tau_j \in \bar{\Omega} \cap \Pi$  such that  $\tau_j \equiv z_j \pmod{G}$ . So there is  $S_j \in G$  with  $S_j(z_j) = \tau_j$ .

If  $z_j \rightarrow \infty$ , then  $z_j = \tau_j$  is in  $\bar{\Omega}$  and so  $f(z_j) \rightarrow \infty$  by Lemma 4, contradicting (ii).

Otherwise, we have  $\text{Im } z_j \rightarrow 0$ . Since  $\{\lambda(z_j)\}$  is bounded, we may pass to a subsequence and suppose that  $\lambda(z_j) \rightarrow \alpha \in \mathbb{C}$ . We consider three cases:

*Case 1.*  $\alpha \neq 0, \alpha \neq 1$ . Then, after possibly passing to a subsequence, there is a  $\tau \in \bar{\Omega} \cap \Pi$  such that  $\tau_j \rightarrow \tau$  and  $\lambda(\tau) = \alpha$ . Then  $\lambda'(z_j) = \lambda'(\tau_j) \cdot S_j'(z_j)$ . But  $|S_j'(z_j)| = \text{Im } \tau_j / \text{Im } z_j \rightarrow \infty$  since  $\text{Im } \tau_j \rightarrow \text{Im } \tau \neq 0$  and  $\text{Im } z_j \rightarrow 0$ , while  $\lambda'(\tau_j) \rightarrow \lambda'(\tau) \neq 0$ . Thus  $\lambda'(z_j) \rightarrow \infty$  which implies  $f(z_j) \rightarrow \infty$ , another contradiction.

*Case 2.*  $\alpha = 0$ . Then  $\tau_j \rightarrow \infty$  in  $\bar{\Omega}$ . We have  $(\lambda'/\lambda)(z_j) = (\lambda'/\lambda)(\tau_j) \cdot S_j'(z_j)$ . By Lemma 4,  $(\lambda'/\lambda)(\tau_j) \rightarrow i\pi$ . Also  $|S_j'(z_j)| = (\text{Im } \tau_j / \text{Im } z_j) \rightarrow \infty$ . Thus  $(\lambda'/\lambda)(z_j) \rightarrow \infty$  which implies  $f(z_j) \rightarrow \infty$ .

*Case 3.*  $\alpha = 1$ . Then  $\tau_j \rightarrow 0$ . From  $\lambda'(z_j) = \lambda'(\tau_j) \cdot S_j'(z_j)$  we get

$$\begin{aligned} \left| \frac{\lambda'(z_j)}{1 - \lambda(z_j)} \right| &= \left| \frac{\lambda'(\tau_j)}{1 - \lambda(\tau_j)} \right| \cdot \left| \frac{\text{Im } \tau_j}{\text{Im } z_j} \right| \\ &= \left| \frac{\tau_j^2 \lambda'(\tau_j)}{1 - \lambda(\tau_j)} \right| \cdot \left| \frac{\text{Im } \tau_j}{\tau_j} \right| \cdot \left| \frac{1}{\tau_j \text{Im } z_j} \right|. \end{aligned}$$

By Lemma 5, the first factor on the right converges to  $\pi$ . Since 0 is a cusp of  $\Omega$ , it is easy to check that the second factor converges to 1 as  $\tau_j \rightarrow 0$ . We conclude that  $(\lambda'/(1 - \lambda))(z_j) \rightarrow \infty$ , in contradiction to (ii). This completes the proof of Theorem 1.

5. Finally we alter our mapping in order to get an imbedding of the open unit disc  $U$ . Because  $\lambda$  and  $\lambda'$  are  $H$ -automorphic,  $G = (\lambda, \lambda'/(\lambda(1 - \lambda)))$  gives a well-defined mapping of  $\Pi/H$  into  $\mathbb{C}^2$ . Note that  $G = (\lambda, \lambda f)$  while  $F = (\lambda, f)$ . An obvious modification of the proof of Lemma 4(b) shows that  $G$  is one-to-one on  $\Pi/H$ . From  $z = e^{i\tau}$ , we get a well-defined one-to-one holomorphic map  $\tilde{G}: \Delta \rightarrow \mathbb{C}^2$  given by  $\tilde{G}(z) = G(\log z/i\pi)$ . Write  $\tilde{G} = (g_1, g_2)$ .

LEMMA 6.  $\tilde{G}$  extends to be analytic at the origin with  $\tilde{G}(0) = (0, i\pi)$ .

*Proof.* We restrict  $\tau \in \Pi$  to  $0 \leq \text{Re } \tau < 2$  and observe that this region maps onto  $\Delta$  via  $z = e^{i\tau}$ . Put  $\Omega^* = \{\tau^*: \tau \in \Omega\}$ . By Lemma 2,  $(\lambda'/\lambda) = -(\overline{\lambda'/\lambda})(\tau^*)$ . Since  $\tau^* \rightarrow \infty$  in  $\Omega$  as  $\tau \rightarrow \infty$  in  $\Omega^*$ , we conclude from Lemma 4 that  $(\lambda'/\lambda)(\tau) \rightarrow -(\overline{i\pi}) = i\pi$  as  $\tau \rightarrow \infty$  in  $\Omega^*$ . Hence  $(\lambda'/\lambda)(\tau) \rightarrow i\pi$  as  $\tau \rightarrow \infty$  in  $\bar{\Omega} \cup \Omega^*$ . Now as  $z = e^{i\tau} \rightarrow 0$

in  $\Delta$ ,  $\tau \rightarrow \infty$  in  $\bar{\Omega} \cup \Omega^*$  and so  $g_1(z) = \lambda(\tau) \rightarrow 0$  and  $g_2(z) = (\lambda'(\tau)/\lambda(\tau)) \cdot (1/(1 - \lambda(\tau))) \rightarrow i\pi \cdot 1$ , Thus  $g_1$  and  $g_2$  have removable singularities at  $z = 0$ .

Henceforth we shall consider  $\tilde{G}$  as a mapping on  $U$ .

**THEOREM 2.**  *$\tilde{G}$  is a proper, one-to-one, non-singular, holomorphic mapping of  $U$  into  $\mathbb{C}^2$ .*

**LEMMA 7.**  *$\tilde{G}$  separates the points of  $U$ .*

*Proof.* Suppose, for  $z_1$  and  $z_2$  in  $U$ , that (i)  $g_1(z_1) = g_1(z_2)$  and (ii)  $g_2(z_1) = g_2(z_2)$ . Observe that if  $g_1(z) = 0$  for  $z \in U$  then, since  $\lambda \neq 0$  on  $\Pi$ , we have  $z = 0$ . Thus if  $g_1(z_1) = 0$ , then  $g_1(z_2) = 0$  and  $z_1 = 0$ ,  $z_2 = 0$ . If  $g_1(z_1) \neq 0$ , then  $g_1(z_2) \neq 0$  and so  $z_1$  and  $z_2$  are in  $\Delta$ . Since we have already observed that  $\tilde{G}$  separates the points of  $\Delta$ , we conclude that  $z_1 = z_2$  in either case.

**LEMMA 8.**  *$\tilde{G}$  is non-singular on  $U$ .*

*Proof.* We show that  $g'_1 \neq 0$  on  $U$ . We have, for  $z \neq 0$ ,  $g_1(z) = \lambda(\log z/\pi i)$ . Hence  $g'_1(z) = (\pi iz)^{-1} \lambda'(\log z/\pi i)$  and so  $g'_1 \neq 0$  on  $\Delta$ . Putting  $z = e^{i\pi\tau}$  we have  $g'_1(z) = (i\pi e^{i\pi\tau})^{-1} \lambda'(\tau) = \sigma'(z)$  in the notation of the proof of Lemma 4. As  $z \rightarrow 0$ ,  $g'_1(z) \rightarrow \sigma'(0) \neq 0$ .

Finally we show that  $\tilde{G}$  is proper. Returning to the half plane, it is enough (because of Lemma 2) to show: If  $\{z_j\} \subseteq \Pi$ ,  $0 \leq \operatorname{Re} z_j \leq 1$ , and  $\operatorname{Im} z_j \rightarrow 0$ , then  $G(z_j) \rightarrow \infty$ . Arguing by contradiction, as before, we may suppose (a)  $\lambda(z_j) \rightarrow \alpha \in \mathbb{C}$  and (b)  $|\lambda'(z_j)/(\lambda(z_j)(1 - \lambda(z_j)))| \leq M$ .

We reconsider the proof of the properness of  $F$  with its three cases. If  $\alpha \neq 0, 1$ , we saw that  $\lambda'(z_j) \rightarrow \infty$ , if  $\alpha = 0$ , we had  $\lambda'(z_j)/\lambda(z_j) \rightarrow \infty$  and if  $\alpha = 1$ , we got  $\lambda'(z_j)/(1 - \lambda(z_j)) \rightarrow \infty$ . In every case there is a contradiction to (b). This completes the proof of Theorem 2.

As a final remark we observe that if  $V = F(\Pi/H)$  and  $W = \tilde{G}(U)$  are the two image submanifolds in  $\mathbb{C}^2$ , then the inclusion map  $\Delta \subset U$  induces a map  $V \rightarrow W$  which is the restriction to  $V$  of the Cremona transformation  $(z, w) \mapsto (z, zw)$  of  $\mathbb{C}^2$ .

## REFERENCES

- [1] AHLFORS, L. V., *Complex Analysis*, second edition, McGraw-Hill, New York, 1966.
- [2] ALEXANDER, H., On a problem of Julia, *Duke Math. J.*, 42 (1975), 327-332.

- [3] BISHOP, E., Mappings of partially analytic spaces, *Amer. J. Math.*, 83 (1961), 209–242.
- [4] FORSTER, O., Plongements des variétés de Stein, *Comm. Math. Helv.*, 45 (1970), 170–184.
- [5] KASAHARA, K. and NISHINO, T., as reported in *Math. Reviews*, 38 (1969), 4721.
- [6] LAUFER, H., Imbedding annuli in  $C^2$ , *J. d'Analyse Math.*, 26 (1973), 187–215.
- [7] NARASIMHAN, R., Imbedding of holomorphically complete complex spaces, *Amer. J. Math.*, 82 (1960), 917–934.

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