

Zeitschrift: IABSE reports = Rapports AIPC = IVBH Berichte
Band: 83 (1999)

Artikel: High strength concrete beams subject to axial compressive stress
Autor: Marinho, Adriano / Moreno, Armando Lopes Jr.
DOI: <https://doi.org/10.5169/seals-62897>

Nutzungsbedingungen

Die ETH-Bibliothek ist die Anbieterin der digitalisierten Zeitschriften auf E-Periodica. Sie besitzt keine Urheberrechte an den Zeitschriften und ist nicht verantwortlich für deren Inhalte. Die Rechte liegen in der Regel bei den Herausgebern beziehungsweise den externen Rechteinhabern. Das Veröffentlichen von Bildern in Print- und Online-Publikationen sowie auf Social Media-Kanälen oder Webseiten ist nur mit vorheriger Genehmigung der Rechteinhaber erlaubt. [Mehr erfahren](#)

Conditions d'utilisation

L'ETH Library est le fournisseur des revues numérisées. Elle ne détient aucun droit d'auteur sur les revues et n'est pas responsable de leur contenu. En règle générale, les droits sont détenus par les éditeurs ou les détenteurs de droits externes. La reproduction d'images dans des publications imprimées ou en ligne ainsi que sur des canaux de médias sociaux ou des sites web n'est autorisée qu'avec l'accord préalable des détenteurs des droits. [En savoir plus](#)

Terms of use

The ETH Library is the provider of the digitised journals. It does not own any copyrights to the journals and is not responsible for their content. The rights usually lie with the publishers or the external rights holders. Publishing images in print and online publications, as well as on social media channels or websites, is only permitted with the prior consent of the rights holders. [Find out more](#)

Download PDF: 22.07.2025

ETH-Bibliothek Zürich, E-Periodica, <https://www.e-periodica.ch>



High Strength Concrete Beams Subject to Axial Compressive Stress

Adriano MARINHO

Civil Engineer

Univ. Estadual de Campinas
Campinas, SP, Brazil

Adriano Marinho, Structural Engineer
that obtained his MS from the Civil
Engineering at Campinas State
University. Scholar Ship by FAPESP

Armando Lopes MORENO JR

Professor

Univ. Estadual de Campinas
Campinas, SP, Brazil

Armando L. Moreno Jr, Doctor Professor Assistant
of Civil Engineering at Campinas State University –
UNICAMP, Campinas – São Paulo, Brazil.

This paper forms part of a comprehensive investigation of the shear behaviour of high strength concrete beams submitted to axial compressive stress and attempts to search the basis for the development of simple design procedures for these structural elements, particularly the study of the shear force portion absorbed by the concrete, V_c .

Most current building codes express the shear strength of beams in terms of the shear force portion carried by transverse reinforcement, V_s , and the shear force portion “carried by the concrete”, V_c . This “concrete contribution” can be assumed as:

$$V_{C,ACI} = 1.4\sqrt{f'_c} + 17.2\rho_w \frac{V_{ud}}{M_u - N_u} \frac{(4h-d)}{8} \sqrt[3]{b_w d} \text{ [kN]}, \text{ to ACI 318-86(1)} \quad (1)$$

$$V_{C,NBR} = 0.15 * b_w * d * \sqrt{f_{ck}} * \sqrt[3]{1 + \frac{M_0}{M_{sd}}} \text{ [kN]}, \text{ according to NBR 6118(2).} \quad (2)$$

$$V_{C,REV} = 0.6 * f_{ctd} * b_w * d * \sqrt[3]{1 + \frac{M_0}{M_{sd}}} \text{ [kN]}, \text{ according to NBR 6118 review.} \quad (3)$$

$$V_{C,CEB} = V_\theta - V_{45} \text{ [kN]}, \text{ according to CEB FIP-1990 (4)} \quad (4)$$

$$V_\theta = \frac{-A_{sw} * f_{yd}}{s} \sqrt[3]{z * (\cot g\theta + \cot g90) * \sin 90} \quad (5)$$

considering V_{45} and V_θ the total shear force ($V_c + V_s$) according to the “plasticity truss model” with the angle of inclination of the diagonal concrete struts, θ , equal to 45 degrees for V_{45} and variable from 18.4 up to 45 degrees for V_θ .

Based on the research’s results herein presented, a new equation is proposed for predicting the ultimate shear force portion “carried by the concrete”, V_c :

$$V_{C,PROP} = 0.6 * f_{ctd} * b_w * d * (1 + \kappa)^2 \text{ [kN]}, \text{ with } (1 + \kappa)^2 \leq 2 \quad (6)$$

with the compression degree, k , assumed as:

$$K = \frac{N}{N_{nec}} \quad (7)$$

where N is the compressive axial load applied in the beam and N_{nec} is the service compressive axial load necessary to avoid tension stresses in required cross section of the beam, assumed as:

A total amount of seven beams, with a concrete compressive strength around 85 N/mm^2 , were analysed. All of them had identical geometry and reinforcement, longitudinal and transversal. The only variables were the intensity of the compressive axial load applied and its application point through out the beam's height.

The loading on the beams was made up of a concentrated load, applied at the midspan of the beams, and of a compressive axial load, applied at their external faces.

A web reinforcement ratio, ρ_w , of 0.252% was adopted for all the beams. Logically this value was chosen in order to be inferior to the web reinforcement ratio, which was calculated according to the classical truss model - $\rho_{w,45}$, once the shear failure by yielding of the web reinforcement was required. Strains in the longitudinal bars and shear reinforcement were measures by strain gages.

The intensity and position difference point application of the compressive axial load resulted in a variability of the compression degree, k , in the investigated beams.

All the tested beams have reached the ultimate shear capacity by the yielding of the web reinforcement as it was expected.

Failure was sudden and complete, particularly in beams with high compression degree, k .

Results of the tests conducted here have shown that the truss model can be extended to high-strength concrete beams subjected to axial compressive stress, on the shear design. At least the ones which have been made of concrete with a compressive strength until 85 N/mm^2 .

The shear force portion "absorbed by the concrete", V_c , calculated according ACI code equation, NBR code equation and CEB code equation, were compared with the experimental data obtained in this work and it could be noticed that the all code equations were very conservative for high strength concrete beams herein tested, underestimating the influence of shear force portion "absorbed by the concrete", V_c , at the shear strength design.

It was possible to notice for this research's beams, as it was already observed by Leonhardt for the usual strength concrete beams subject to axial compressive stress, the possibility of a bigger reduction shear load portion, V_c , due to the compression degree increased, k , within the beams). This reduction possibility may be explained due to the fact that the longitudinal compression stresses delay the crack beginning of the beams and, therefore, they delay the mobilised of the web reinforcement too.

The new proposal, presented in this paper, eq. (6), has provided satisfactory values of "shear force portion absorbed by the concrete", V_c , for high strength concrete beams submitted to axial compressive stress.