

**Zeitschrift:** IABSE reports = Rapports AIPC = IVBH Berichte  
**Band:** 59 (1990)  
  
**Artikel:** Fatigue of cross-beam connections in plate-girder highway bridges  
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**DOI:** <https://doi.org/10.5169/seals-45714>

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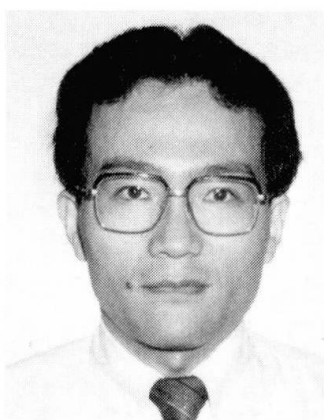
## Fatigue of Cross-Beam Connections in Plate-Girder Highway Bridges

Fatigue dans les attaches des entretoises de ponts-routes à section ouverte

Ermüdung der Querträger-Anschlüsse in Strassenbrücken  
mit offenen Querschnitten

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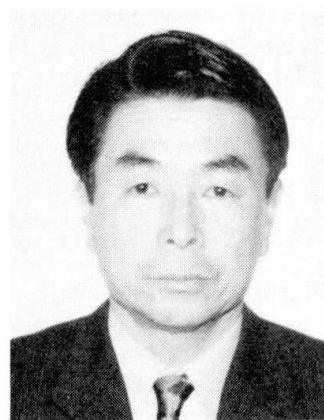
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### SUMMARY

Fatigue cracks often grow from connections of cross beams to main girders in plate-girder highway bridges. The structural parameters which govern cracking at cross-beam connections are examined based on the overall behaviour of the bridges. Cracking patterns at cross-beam connections are determined from fatigue tests. A recommendation is given for connection details between concrete slabs and main girder flanges.

### RÉSUMÉ

Les fissures de fatigue prennent souvent naissance à la liaison entre les entretoises et les poutres maîtresses des ponts-routes à section ouverte. Les paramètres structuraux qui régissent la fissuration aux liaisons avec les entretoises sont examinés en se basant sur le comportement global des ponts. Des modèles de fissuration des liaisons avec les entretoises sont déterminés à partir d'essais de fatigue. Une recommandation est donnée pour des détails de liaison entre la dalle de béton et les ailes des poutres maîtresses.

### ZUSAMMENFASSUNG

Ermüdungsrisse in Strassenbrücken mit offenen Querschnitten gehen oft von den Verbindungen zwischen Quer- und Hauptträgern aus. Die Einflussfaktoren, die den Rissverlauf an den Verbindungsstellen bestimmen, werden unter Berücksichtigung des Gesamtverhaltens der Brücke untersucht. Das Rissverhalten an den Verbindungsstellen wird anhand von Ermüdungsversuchen betrachtet. Es werden Empfehlungen gemacht zur Gestaltung der Konstruktionsdetails bei der Verbindung zwischen Betonfahrbahnplatte und Hauptträgerflansch.



## 1. INTRODUCTION

In many plate girder highway bridges in the urban area of Japan, fatigue cracks are often observed at the connections of main girders with secondary members such as cross beams, sway bracings and lateral bracings. At the connections of cross beams to main girders in the plate girder bridges of the Hanshin Expressway in Osaka, four types of fatigue cracks are detected, as shown in Fig.1.

-Type 1 crack is initiated either on the bead or at the toe at the end of the fillet weld between the connection plate and the top flange of the main girder.

-Type 2 crack is initiated at the upper scallop of the connection plate, and grows diagonally through the connection plate itself.

-Type 3 crack is initiated at the toe at the end of the fillet weld connecting the connection plate to the main girder web, and grows downward along the toe on the connection plate side.

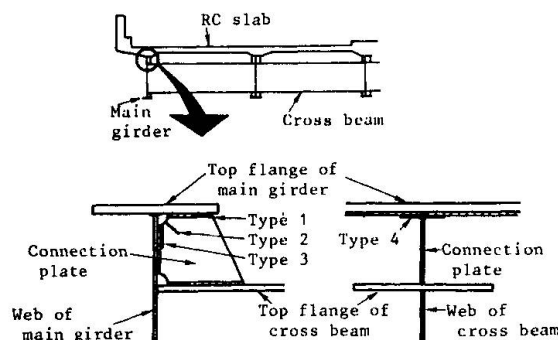
-Type 4 crack is initiated and grows along the toe on the web side of the fillet weld between the top flange and the web of the main girder.

Investigation of the causes of the crack initiation and the development of repair methods have been under way at various research institutions. However satisfactory results are not yet available.

In 1985 the authors carried out the field stress measurement of an existing plate girder bridge of the Hanshin Expressway to make clear the local stresses causing the cracking at the cross-beam connections[1,2]. They then formulated the relationship between the local stresses and the three-dimensional behavior of the bridge under traffic loading[3].

The objectives of this paper are:

- to present the parameters introduced from the structural behavior of a plate girder bridge, which govern the cracking at the cross-beam connections,
- to show the patterns of the cracking at the cross-beam connections from fatigue tests, and
- to give a recommendation to the connection details between concrete slab and main girder flange.



**Fig.1** Fatigue cracks at cross-beam connections of plate girder bridge

## 2. STRUCTURAL PARAMETERS AFFECTING CRACK INITIATION

### 2.1 Relationship between Local Stresses and Rotations of Concrete Slab and of Cross Beam

As shown in Fig.2, the membrane stress  $\sigma_{my}$  in the vertical direction in the connection plate and the plate-bending stress  $\sigma_{by}$  in the main girder web are main factors to cause Types 1 and 4 fatigue cracks, respectively[1,2]. The relationship between those local stresses and the rotations of concrete slab and of cross beam is given by[3]

$$\begin{bmatrix} \sigma_{my} \\ \sigma_{by} \end{bmatrix} = \begin{bmatrix} k_{m1} & k_{m3}(\nu - k_{m123}) \\ k_{b1} & k_{b3}(\nu - k_{b123}) \end{bmatrix} \begin{bmatrix} \theta_{s0} \\ \theta_g \end{bmatrix} \quad (1)$$

where  $\theta_{s0}$ =rotation of concrete slab due to the slab-deformation caused by wheel loads(see Fig.3),  $\theta_g$ =rotation of cross beam due to the vertical displacements of main girders(see Fig.3),  $\nu$ =coefficient depending on the position of a vehicle in the direction of the roadway width, and  $k_{m1}$ ,  $k_{m3}$ ,  $k_{m123}$ ,  $k_{b1}$ ,  $k_{b3}$  and  $k_{b123}$ =constants which relate the local stresses to the rotations of concrete slab and of cross beam.

### 2.2 Structural Parameter for Concrete-Slab Rotation

Referring to Fig.4, the rotation  $\theta_{s0}$  of concrete slab at the position (a, 0) where a main girder is located, is expressed by[3]

$$\theta_{s0} = (a/D_c) \{P/(2\pi^2)\} \phi_p(x/a) \phi(x/a) \left[ \sum_{m=1}^{\infty} \{(-1)^m/m^2\} \sin(m\pi x/a) \right. \\ \left. (1+m\pi|y|/a) \exp(-m\pi|y|/a) \right] \quad (2)$$

where  $a$ =spacing between main girders,  $D_c$ =flexural rigidity of concrete slab,  $P$ =a concentrated load,  $\phi_p(x/a)$ =correction factor for the wall parapets on both sides of the roadway, and  $\phi(x/a)$ =correction factor to treat the concrete slab as a continuous plate.

Equation(2) implies that the concrete-slab rotation  $\theta_{s0}$  varies with values of  $a/D_c$ . The values of  $a/D_c$  are determined by the dimensions of concrete slab. Hence the reciprocal of  $a/D_c$ , namely,  $D_c/a$  is chosen as a structural parameter for  $\theta_{s0}$ . The bridges with smaller values for  $D_c/a$  are more susceptible to cracking, since the decrease of  $D_c/a$  increases  $\theta_{s0}$  and then results in the

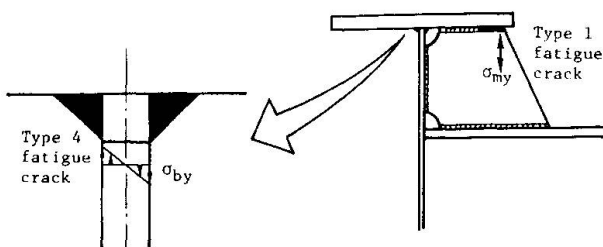


Fig.2 Local stresses  $\sigma_{my}$  and  $\sigma_{by}$

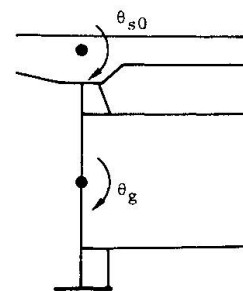


Fig.3 Rotations  $\theta_{s0}$  and  $\theta_g$

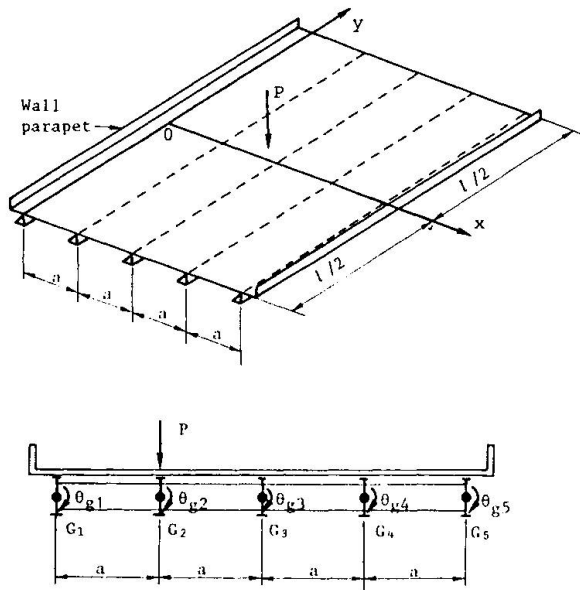


Fig. 5 Cross-beam rotation  $\theta_{gi}$

increase of the local stresses of  $\sigma_{my}$  and  $\sigma_{by}$ .

### 2.3 Structural Parameters for Cross-Beam Rotation

In a plate girder bridge with five main girders as shown in Fig. 5, the rotation  $\theta_{gi}$  of the cross beam at the main girder  $G_i$  is given by [3]:

$$\theta_{gi} = \mathbf{A}_i \mathbf{v} / (56a) \quad (3)$$

where  $\mathbf{v} = (v_1, v_2, v_3, v_4, v_5)^T$ ,  $v_i$  = vertical displacement of the girder  $G_i$  at the cross-beam connection, T = symbol representing transpose, and  $\mathbf{A}_i$  = row vector consisting of constants which correspond to  $\theta_{gi}$ . When a concentrated load  $P$  is applied to the girder  $G_j$ , the vertical displacement  $v_i$  of the girder  $G_i$  is provided with

$$v_i = P q_{ij} l^3 / (48 E_s r_i I_g) \quad (4)$$

where  $q_{ij}$  = load-distribution-coefficient from the girder  $G_j$  to  $G_i$ ,  $l$  = span length of main girders,  $E_s$  = Young's modulus of steel,  $r_i = I_{gi} / I_g$ ,  $I_{gi}$  = moment-of-inertia of the main girder  $G_i$ , and  $I_g$  = moment-of-inertia of any girder arbitrarily selected among the five main girders. The load-distribution-coefficient  $q_{ij}$  is expressed by a function of  $r_i$  and  $Z$  defined by

$$Z = (I_Q / I_g) \{l / (2a)\}^3 \quad (5)$$

where  $I_Q$  = moment-of-inertia of a cross beam. Substitution of Eq. (4) into Eq. (3) provides

$$\theta_{gi} = \{P / (2688 E_s)\} \{l^3 / (a I_g)\} \mathbf{A}_i \mathbf{q} \quad (6)$$

where  $\mathbf{q} = (q_{1j}/r_1, q_{2j}/r_2, q_{3j}/r_3, q_{4j}/r_4, q_{5j}/r_5)^T$ .

Figure 6 shows the relationship between  $\mathbf{A}_i \mathbf{q}$  which corresponds to

Fig. 4 Concrete slab under concentrated load  $P$

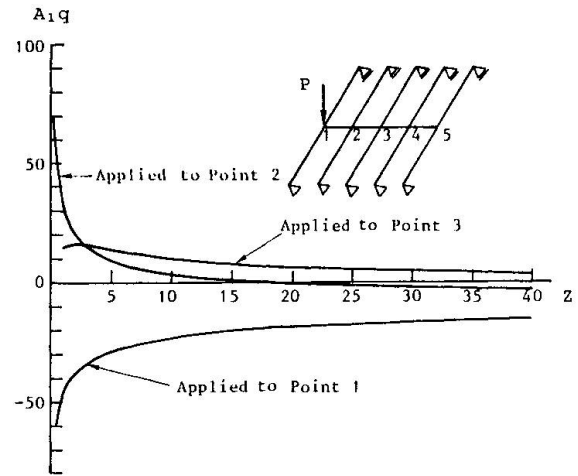


Fig. 6 Relationship between  $\mathbf{A}_i \mathbf{q}$  and  $z$

the cross-beam rotation  $\theta_{g1}$ , and  $Z$ . The calculation of  $A_1q$  is carried out for all  $r_i=1$ . Except for the case of a concentrated load  $P$  applied to the girder  $G_3$  above which a center divider exists on the roadway,  $A_1q$  is approximately inversely-proportional to  $Z$  for  $Z \leq 10$ . Accordingly, when  $Z \leq 10$ , the term  $\{I^3/(aI_g)\}A_1q$  in Eq.(6) is proportional to  $\{I^3/(aI_g)\}/Z$ , and then considering Eq.(5),  $\{I^3/(aI_g)\}/Z$  is changed into  $8a^2/I_0$ . On the other hand, when  $Z > 10$ , only the term  $I^3/(aI_g)$  is variable in Eq.(6), since  $A_1q$  takes almost constant values for  $Z > 10$ .

From the above, the following structural parameters are chosen for the cross-beam rotation  $\theta_{gi}$ :

$$I_0/a^2 \text{ for } Z \leq 10 \quad (7)$$

$$aI_g/l^3 \text{ for } Z > 10 \quad (8)$$

The bridges with smaller values for these structural parameters suffer more chances of cracking, since the decrease of the parameters increases  $\theta_g$ , which leads to the increase of the local stresses of  $\sigma_{my}$  and  $\sigma_{by}$ .

#### 2.4 Relationship between Structural Parameters and Cracking

The relationship between  $I_0/a^2$  and initiation of Types 1 and 4 cracks is investigated for 158 plate girder bridges on a route of the Hanshin Expressway[4]. The structural parameter  $D_c/a$  is found to be almost invariable on this route.

Figure 7 shows the relationship between  $I_0/a^2$  and the number of bridges in which Type 1 cracks were detected. As shown in Ref.[4], the influence of  $\theta_g$  on the local stress  $\sigma_{my}$  which causes Type 1 cracks is very small in the bridge with  $I_0/a^2=3.1 \text{ cm}^2$ . In Fig.7, however, Type 1 cracks occur in the bridges for  $I_0/a^2 > 3.0 \text{ cm}^2$ . This indicates that Type 1 cracks can be initiated by the

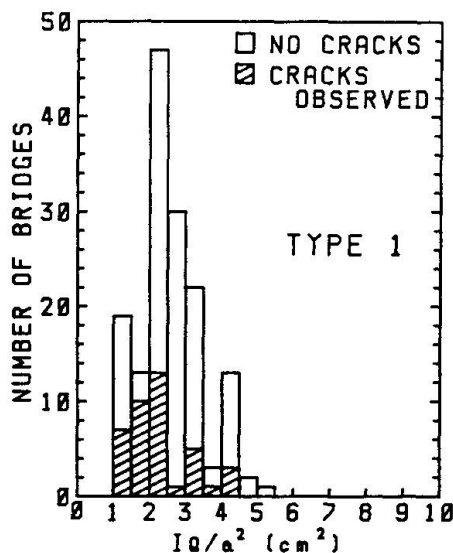


Fig.7 Relationship between  $I_0/a^2$  and the number of bridges in which Type 1 cracks were observed

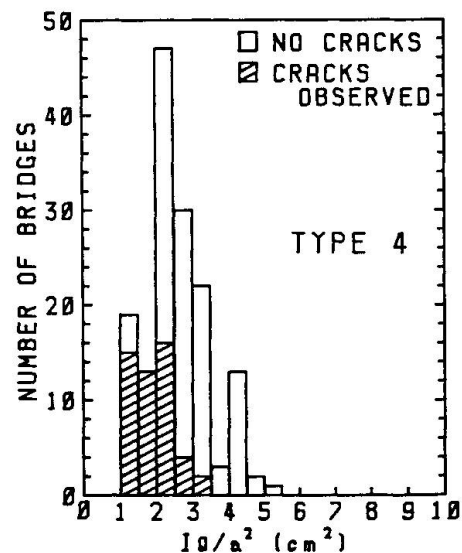


Fig.8 Relationship between  $I_0/a^2$  and the number of bridges in which Type 4 cracks were observed



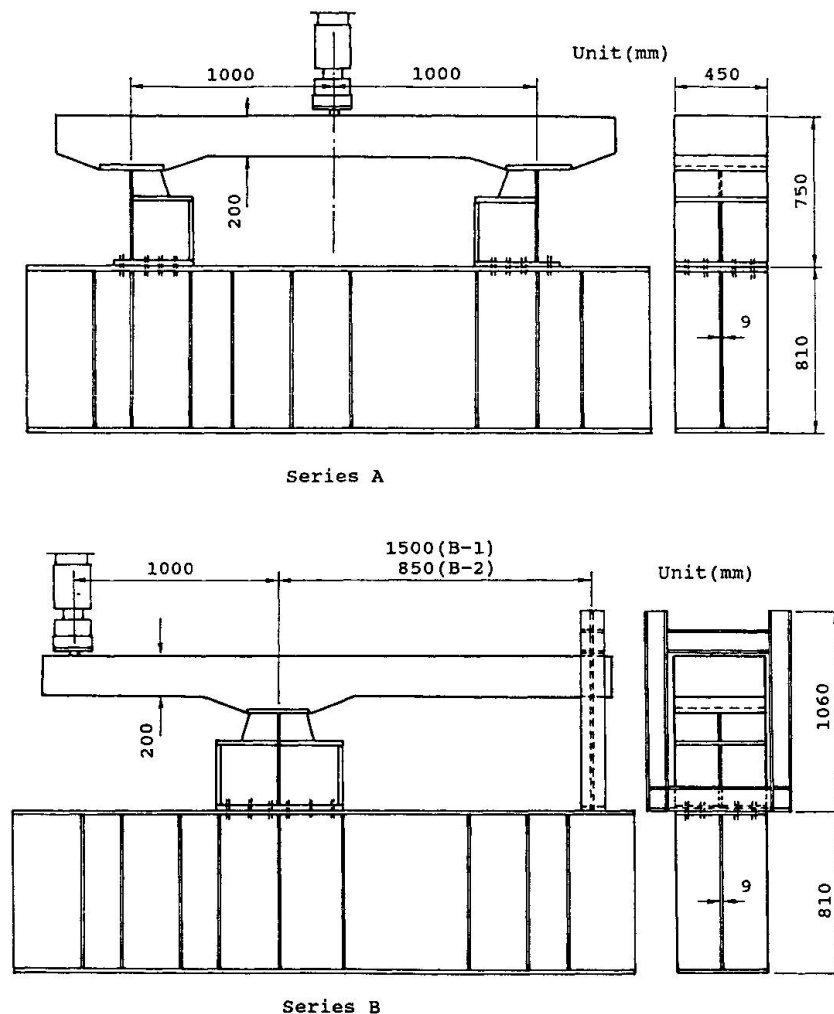
concrete-slab rotation only.

Figure 8 shows the relationship between  $I_Q/a^2$  and the number of bridges in which Type 4 cracks were observed. With the increase in  $I_Q/a^2$ , the number of bridges suffering from cracking gradually decreases, since the influence of  $\theta_g$  on the local stress  $\sigma_{by}$  which causes Type 4 cracks becomes small. No cracks occur in the bridges for  $I_Q/a^2 > 3.5 \text{ cm}^2$ .

### 3. FATIGUE TESTS OF CROSS-BEAM CONNECTIONS

#### 3.1 Fatigue Test Specimens

As can be seen from Eq.(1), the local stresses  $\sigma_{my}$  and  $\sigma_{by}$  are provided with the sum of stress components due to the rotations of concrete slab and of cross beam. This implies that effects of concrete-slab rotation and of cross-beam rotation on the local stresses can be divided. Then in order to clarify the influence of the concrete-slab rotation on the cracking at cross-beam connections, fatigue tests are carried out on the specimens as shown in Fig.9. The specimens consist of cross-beam connections and of



**Fig.9** Fatigue test specimens

a concrete slab in a stripped form. The series A corresponds to the cross-beam connections of exterior main girders. The series B does for interior main girders. In the series B, negative moment is created in the concrete slab above the cross-beam connection.

### 3.2 Connection Details between Girder Flange and Concrete Slab

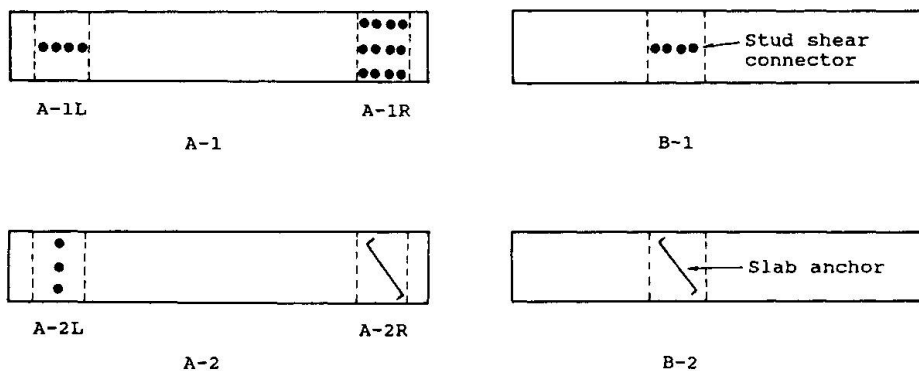
In order to examine the effects of connection details between girder flange and concrete slab on the cracking, the number of stud shear connectors and their arrangement are changed at each cross-beam connection, as shown in Fig.10. In the right side of Specimen A-2 and in Specimen B-2, a slab anchor is used.

### 3.3 Results of Fatigue Tests

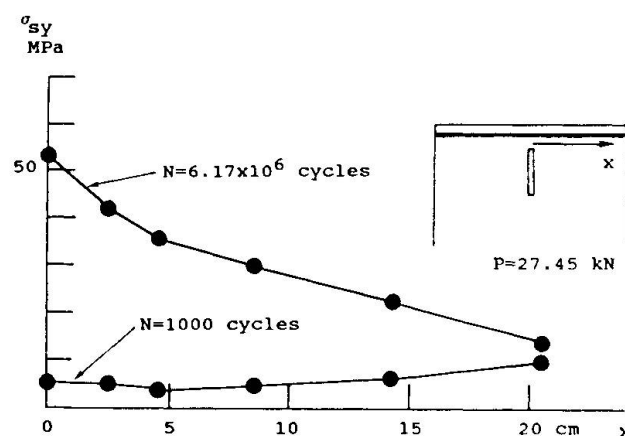
The following observations are drawn from the fatigue tests:

-The similar cracks as shown in Fig.1 occur at all the cross-beam connections, not depending on the connection details between girder flange and concrete slab.

-In the series A corresponding to the cross-beam connections of exterior main girders, there exists no order in initiation of Types 1 and 4 cracks, while in the series B corresponding to the



**Fig.10** Connection details between girder flange and concrete slab



**Fig.11** Distribution of web surface stress  $\sigma_{sy}$  along the flange-to-web fillet weld (Specimen B-1)





cross-beam connections of interior main girders, Type 4 crack follows Type 1 crack.

The distribution along the flange-to-web fillet welds of the stress  $\sigma_{sy}$  on the surface of the web plate is shown in Fig.11 for Specimen B-1. In the figure, at  $N=1000$  cycles  $\sigma_{sy}$  is very small and Type 1 crack does not occur, while at  $N=6.17 \times 10^6$  cycles  $\sigma_{sy}$  becomes large and Type 1 crack is initiated and grows. Therefore in the series B the propagation of Type 1 crack makes the local stress  $\sigma_{by}$  increase, and then results in Type 4 crack initiation.

### 3.4 Characteristics of Occurrence of Local Stresses

In order to make clear the occurrence of the local stresses  $\sigma_{my}$  and  $\sigma_{by}$ , a finite element analysis is carried out for a model as shown in Fig.12. It consists of a girder flange, girder web and connection plate, and a half of them is divided into finite elements from symmetry. The bottom edges of the girder web and connection plate are fixed. The forces which are determined by the measurements of displacement of the concrete slab and by the measurements of strain of the stud shear connectors are applied to the girder flange of the F.E.M. model, as shown in Fig.13. The vertical forces on the girder flange are produced by the pull-out action of stud shear connectors and by the contact action between concrete slab and girder flange. The horizontal forces on the girder flange are created by the shear resistance of stud shear connectors.

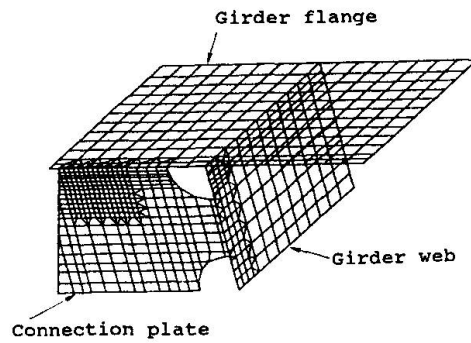
Comparison of F.E.M. values with the measured ones is shown in Fig.14 for  $\sigma_{my}$  and  $\sigma_{by}$ . As for  $\sigma_{my}$ , F.E.M. values are close to the measured ones. As for  $\sigma_{by}$ , the distribution of F.E.M. values shows the same tendency as that of the measured ones, though the former shifts slightly from the latter.

The local stresses  $\sigma_{my}$  and  $\sigma_{by}$  can be correlated with the forces  $Q$  and  $S$ . Here  $Q$  is, as shown in Fig.13, the total of the vertical forces on the girder flange, while  $S$  is the total of the horizontal forces on the girder flange. The stress components of  $\sigma_{my}$  and  $\sigma_{by}$  against  $Q$  and  $S$  are listed in Table 1 for the series A. The stress values in the table are obtained at the points of the strain gauges nearest to the crack initiation in the fatigue tests. Connection A-0, which is just a model for the F.E.M. analysis, corresponds to the cross-beam connections in which neither stud shear connectors nor slab anchors are used between concrete slab and girder flange. In this model, the concentrated load of 49.0 kN is applied vertically to the edge of the girder flange just above the connection plate.

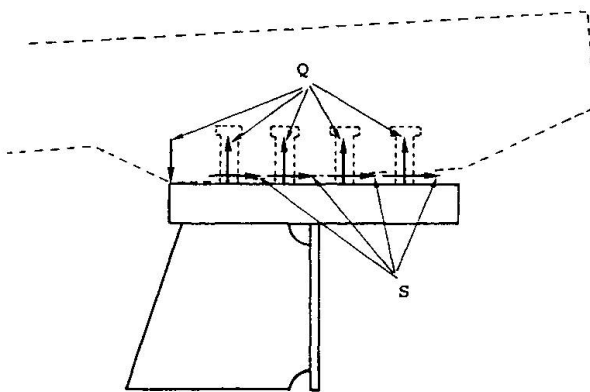
The following are pointed out from Table 1:

- The local stress  $\sigma_{my}$  is mostly produced by the vertical force  $Q$ , while the local stress  $\sigma_{by}$  is produced by both  $Q$  and  $S$ .
- The stress values of Connection A-0 are much smaller than those of any other connection model.

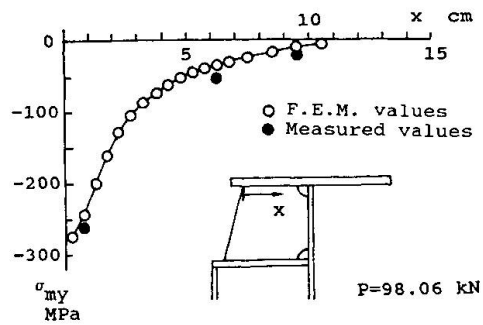
In order to reduce the local stresses and thus to prevent cracking, it is recommended that neither stud shear connectors nor slab



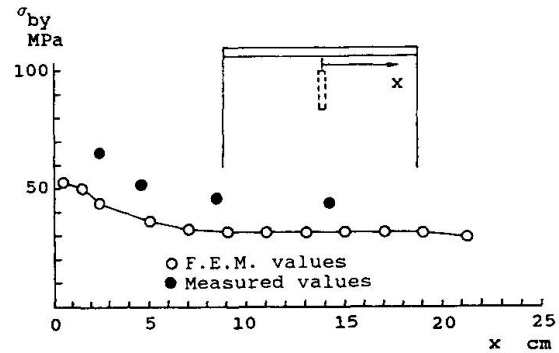
**Fig.12** Mesh division



**Fig.13** Forces acting on F.E.M. model



(a)  $\sigma_{my}$  at connection plate



(b)  $\sigma_{by}$  at girder web

**Fig.14** Comparison of F.E.M. values with measurement values (Connection A-1L)

**Table 1** Comparison of stress components against Q and S

Connection	Q (kN)	S (kN)	$\sigma_{my}$ (MPa)	$\sigma_{mQ}$ (MPa)	$\sigma_{mS}$ (MPa)	$\sigma_{by}$ (MPa)	$\sigma_{bQ}$ (MPa)	$\sigma_{bS}$ (MPa)
A-1L	48.88	41.45	-237.9	-240.8	2.9	43.2	8.6	34.6
A-1R	49.17	56.43	-292.3	-296.2	3.9	96.3	49.2	47.1
A-2L	56.03	66.08	-275.4	-279.8	4.4	77.1	21.1	55.9
A-2R	42.02	44.32	-295.9	-298.9	2.9	26.5	-11.9	38.5
A-0	49.03	0.0	-184.0	-184.0	0.0	-9.7	-9.7	0.0

Note:  $\sigma_{my} = \sigma_{mQ} + \sigma_{mS}$   
 $\sigma_{by} = \sigma_{bQ} + \sigma_{bS}$   
 $\sigma_{mQ}$  = membrane stress component produced by Q  
 $\sigma_{mS}$  = membrane stress component produced by S  
 $\sigma_{bQ}$  = plate-bending stress component produced by Q  
 $\sigma_{bS}$  = plate-bending stress component produced by S

anchors be placed above the connections of cross beams to main girders.

#### 4. CONCLUSIONS

(1) The structural parameters governing the fatigue cracking at the connections of cross beams to main girders in plate girder highway bridges were specified as follows according to the rotations of



concrete slab and of cross beam:

- a) For the concrete-slab rotation,  $D_c/a$ .
- b) For the cross-beam rotation,  $I_Q/a^2$  when  $Z \leq 10$ , and  $aI_g/l^3$  when  $Z > 10$ . Here  $Z = (I_Q/I_g) \{1/(2a)\}^3$ .

The bridges with smaller values of the above structural parameters become more susceptible to cracking. Type 1 cracks at the connection plates can be initiated by the concrete-slab rotation only.

(2) From the fatigue tests to investigate the influence of the concrete-slab rotation on the cracking, it was revealed that cracks are initiated at the cross-beam connections with stud shear connectors regardless of the number of them and their arrangement, and that they are also initiated at the cross-beam connections with slab anchors.

(3) To reduce the local stresses and thus to prevent cracking, it was recommended from a F.E.M. analysis that neither stud shear connectors nor slab anchors be placed above the connections of cross beams to main girders.

#### ACKNOWLEDGMENT

The authors would like to thank Mr. H. Inoue, graduate student of Osaka University, and Mr. Y. Yamada, Takadakiko Co., Ltd. for their help in carrying out the fatigue tests. The first author would also like to acknowledge the Kajima Foundation, Japan, who offered him the traveling expenses for his presentation in EPFL, Switzerland.

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