

**Zeitschrift:** IABSE reports of the working commissions = Rapports des commissions de travail AIPC = IVBH Berichte der Arbeitskommissionen

**Band:** 16 (1974)

**Artikel:** On the extreme compressive strain of concrete for calculating the ultimate strength of reinforced concrete section

**Autor:** Muguruma, Hiroshi / Tanaka, Shinzo

**DOI:** <https://doi.org/10.5169/seals-15716>

#### **Nutzungsbedingungen**

Die ETH-Bibliothek ist die Anbieterin der digitalisierten Zeitschriften auf E-Periodica. Sie besitzt keine Urheberrechte an den Zeitschriften und ist nicht verantwortlich für deren Inhalte. Die Rechte liegen in der Regel bei den Herausgebern beziehungsweise den externen Rechteinhabern. Das Veröffentlichen von Bildern in Print- und Online-Publikationen sowie auf Social Media-Kanälen oder Webseiten ist nur mit vorheriger Genehmigung der Rechteinhaber erlaubt. [Mehr erfahren](#)

#### **Conditions d'utilisation**

L'ETH Library est le fournisseur des revues numérisées. Elle ne détient aucun droit d'auteur sur les revues et n'est pas responsable de leur contenu. En règle générale, les droits sont détenus par les éditeurs ou les détenteurs de droits externes. La reproduction d'images dans des publications imprimées ou en ligne ainsi que sur des canaux de médias sociaux ou des sites web n'est autorisée qu'avec l'accord préalable des détenteurs des droits. [En savoir plus](#)

#### **Terms of use**

The ETH Library is the provider of the digitised journals. It does not own any copyrights to the journals and is not responsible for their content. The rights usually lie with the publishers or the external rights holders. Publishing images in print and online publications, as well as on social media channels or websites, is only permitted with the prior consent of the rights holders. [Find out more](#)

**Download PDF:** 21.01.2026

**ETH-Bibliothek Zürich, E-Periodica, <https://www.e-periodica.ch>**

# On the Extreme Compressive Strain of Concrete for Calculating the Ultimate Strength of Reinforced Concrete Section

Raccourcissement ultime du béton et calcul de la sollicitation ultime d'une section en béton armé

Über den Grenzwert der Druckstauchung von Beton bei der Berechnung der Traglast von Stahlbetonquerschnitten

Hiroshi MUGURUMA      Shinzo TANAKA  
Prof., Doctor of Engineering      Graduate Student  
Kyoto University  
Kyoto, Japan

## 1. Introduction

The failure of reinforced concrete section subjected to the flexural moment, axial load or combined flexural and axial loads is generally caused by crushing of concrete at the compression zone. For the calculation of ultimate strength it is necessary to assume the extreme compressive fiber strain of concrete,  $\epsilon_{cu}$ , induced in the section at the ultimate strength. Usually, the values of  $\epsilon_{cu}$  empirically or semi-empirically determined are adopted in the calculation.<sup>1)</sup> For instance,  $\epsilon_{cu} = 0.15 - 0.2\%$  is assumed for pure axial loading failure and  $\epsilon_{cu} = 0.25-0.35\%$  for flexural failure under the action of pure flexural load or combined flexural and axial loads.

However, the extreme compressive fiber strain of concrete,  $\epsilon_{cu}$ , at the ultimate strength is not always defined clearly from the theoretical view-point. The value of  $\epsilon_{cu}$  seems to be affected by many factors such as the combination of applied axial and flexural forces, the characteristics of stress-strain curve of concrete, especially the falling branch of it after compressive strength, and the percentage of reinforcements etc. In this paper, numerical estimations are made on the value of  $\epsilon_{cu}$  for ultimate strength calculation by using the typical stress-strain curves of concrete, and the effects of these factors upon the value of  $\epsilon_{cu}$  are discussed.

## 2. Definition of concrete fiber strain, $\epsilon_{cu}$ , at ultimate strength

The ultimate loading capacity of reinforced concrete section subjected to combined axial and bending forces can be represented by the ultimate axial load-moment interaction curve. This can be calculated from the equilibrium of forces acting on the section under the consideration of stress and strain compatibility, where the compressive fiber strain of concrete,  $\epsilon_{cu}$ , at ultimate strength should be assumed. While the collapse of reinforced concrete section is generally caused by crushing of concrete in compression zone, the applied load shows its' maximum value before the crushing of concrete. Fig. 1 shows such phenomenon by load-deflection curve of typical member. Thus, generally the maximum of applied

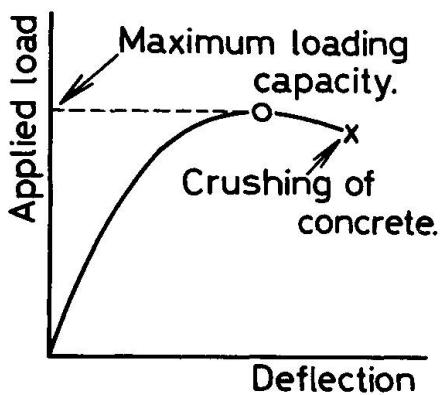


Fig. 1 Load-deflection curve of reinforced concrete member

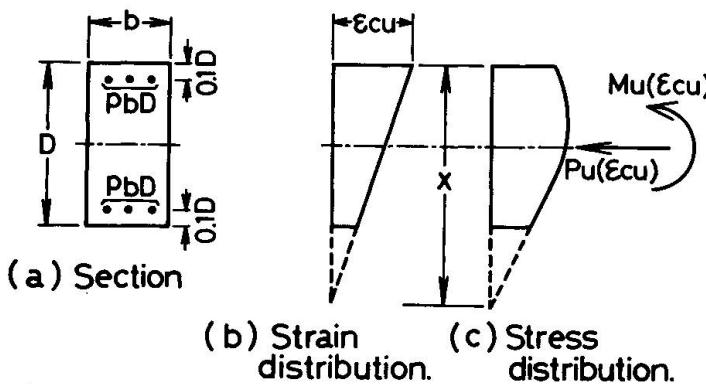


Fig. 2 Stress and strain distributions overall the rectangular column section.

generally expressed as the function of  $\epsilon_c$  and  $x$ . However, considering that loads,  $P(\epsilon_c)$  and  $M(\epsilon_c)$ , are so applied as the eccentricity,

$$e = M(\epsilon_c)/P(\epsilon_c) \quad (1),$$

becomes constant without regard to their magnitude, the distance of neutral axis,  $x$ , can also be expressed as a function of  $\epsilon_c$ . Thus, in other words, a set of combined loads,  $P(\epsilon_c)$  and  $M(\epsilon_c)$ , can be obtained numerically for a given value of  $\epsilon_c$  under the consideration of constant eccentricity,  $e$ .

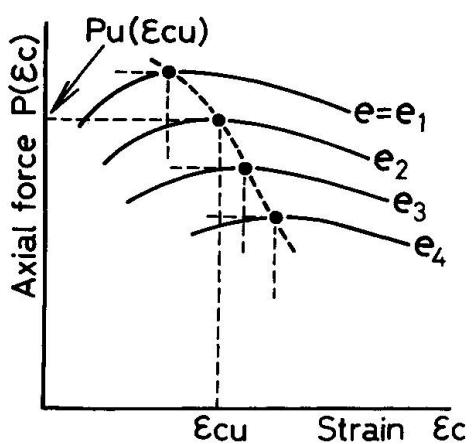


Fig. 3  $\epsilon_c - P(\epsilon_c)$  or  $M(\epsilon_c)$  relation

load recorded until the collapse of section takes place by crushing of concrete is so defined as the ultimate loading capacity or the ultimate strength,<sup>2), 3)</sup> And also the corresponding compressive fiber strain of concrete,  $\epsilon_{cu}$ , is defined as the strain which should be used in the calculation of ultimate strength.

### 3. Method of numerical estimation of $\epsilon_{cu}$

The purpose of this study is to obtain numerically the compressive fiber strain of concrete,  $\epsilon_{cu}$ , at maximum loading capacity of reinforced concrete column section subjected to various combinations of applied axial load and flexural moment. To explain the procedure of numerical estimation, the rectangular column section shown in Fig. 2(a) is considered. The stress and strain distributions overall the section are shown in Fig. 2(b) and 2(c), respectively, in general form. The stress distribution shown in Fig. 2(c) is obtained in correspondence to the strain distribution in Fig. 2(b) by using the stress-strain relations of component materials. The compressive fiber strain of concrete,  $\epsilon_c$ , and the distance of neutral axis,  $x$ , from compressive fiber of section are determined so as to satisfy the equilibrium equations for given combined loads,  $P(\epsilon_c)$  and  $M(\epsilon_c)$ . That is, the applied combined loads,  $P(\epsilon_c)$  and  $M(\epsilon_c)$ , are

Fig. 3 shows  $\epsilon_c - P(\epsilon_c)$  or  $M(\epsilon_c)$  relation for various values of eccentricity,  $e = e_1, e_2, e_3, \dots$ , where the concrete fiber strain,  $\epsilon_{cu}$ , corresponding to the peak value of  $P(\epsilon_c)$  coincides with that of  $M(\epsilon_c)$  because of the linear relation between  $P(\epsilon_c)$  and  $M(\epsilon_c)$ . From the definition of ultimate strength described in 2 the peak values,  $Pu(\epsilon_{cu})$  and  $Mu(\epsilon_{cu})$ , in  $\epsilon_c - P(\epsilon_c)$  and  $\epsilon_c - M(\epsilon_c)$  curves are defined as the maximum loading capacity for a given loading condition,  $e = M(\epsilon_c)/P(\epsilon_c)$ , and the corresponding compressive fiber strain,  $\epsilon_c = \epsilon_{cu}$ , is the strain to be used in the theoretical calculation of ultimate strength. In this paper using  $\epsilon_c - P(\epsilon_c)$  or  $\epsilon_c - M(\epsilon_c)$  relation as shown in Fig. 3, the ultimate strengths,  $Pu(\epsilon_{cu})$

and  $M_u(\epsilon_{cu})$ , as well as corresponding compressive fiber strain of concrete,  $\epsilon_{cu}$ , is estimated graphically for rectangular column section shown in Fig. 2(a).

Moreover, the ultimate strengths,  $P_u(\epsilon_{cu})$  and  $M_u(\epsilon_{cu})$ , and corresponding concrete fiber strain,  $\epsilon_{cu}$ , can be obtained as the values satisfying following mathematical conditions.<sup>3)</sup>

$$\frac{dP(\epsilon_c)}{d\epsilon_c} = 0 \quad \text{or} \quad \frac{dM(\epsilon_c)}{d\epsilon_c} = 0 \quad (2).$$

Of course, a set of values,  $\epsilon_{cu}$ ,  $P_u(\epsilon_{cu})$  and  $M_u(\epsilon_{cu})$ , obtained from first equation in Eq. (2) satisfies the second condition in Eq. (2) simultaneously.

#### 4. Stress-strain curves of component materials for numerical calculation

For numerical calculation of compressive fiber strain of concrete,  $\epsilon_{cu}$ , at the ultimate strength of reinforced concrete column section, the stress-strain curves of component materials should be assumed.

To simplifying the numerical calculation, the ideal elastic-plastic relation shown in Fig. 4 is assumed for reinforcement, where the elastic modulus of  $E_s = 2,100,000 \text{ kg/cm}^2$  is taken without respect to the yield strength of reinforcement.

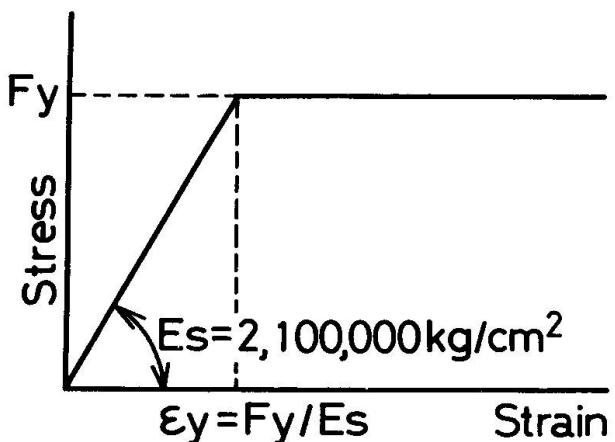


Fig. 4 Stress-strain curve of reinforcement

To simplifying the numerical calculation, the ideal elastic-plastic relation shown in Fig. 4 is assumed for reinforcement, where the elastic modulus of  $E_s = 2,100,000 \text{ kg/cm}^2$  is taken without respect to the yield strength of reinforcement.

Fig. 5 shows three different types of typical stress-strain curve of plain concrete obtained from compressive tests on cylinder specimens of various kinds of concrete.<sup>4),5)</sup> The ordinate in Fig. 5 is expressed as the ratio of applied stress to the compressive strength. Curve I represents the stress-strain relation for ordinary aggregate concrete having 28-day compressive strength up to  $350 \text{ kg/cm}^2$ . Curve II is that of light-weight aggregate structural concrete. The strain at the peak stress (that is, at the compressive strength) as well as the negative inclination of strain softening region in Curve II is greater than that in Curve I. Curve III in Fig. 5 is identical one modified from Curve I for investigating the effect of the negative inclination of strain softening region upon the compressive fiber strain of concrete,  $\epsilon_{cu}$ , at the ultimate strength. For convenience of the numerical calculation of  $\epsilon_{cu}$ , the area surrounded by each stress-strain curve shown in Fig. 5 and its' center of gravity were calculated in correspondence to an arbitrary strain. The results are also shown in Fig. 5 in the coefficients,  $k_1k_3$  and  $k_2$ , versus compressive strain,  $\epsilon_c$ , relations, where  $k_1k_3$  and  $k_2$  denote the ratio of average stress of stress-strain curve until an arbitrary strain,  $\epsilon_c$ , to the compressive strength,  $F_c$ , and the ratio of the location of center of gravity of corresponding area from an arbitrary strain,  $\epsilon_c$ , to the strain  $\epsilon_c$ , respectively. That is, coefficients,  $k_1k_3$  and  $k_2$ , can be considered as the generalized stress block

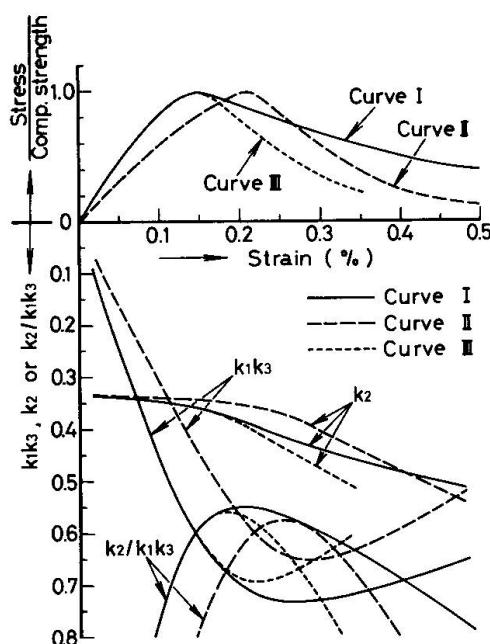


Fig. 5 Typical stress-strain curves of concrete and corresponding values of  $k_1k_3$ ,  $k_2$  and  $k_2/k_1k_3$

coefficients of concrete in flexural compression zone of reinforced concrete section.

### 5. Effects of the eccentricity of applied axial load and the percentage of reinforcements upon $\epsilon_{cu}$

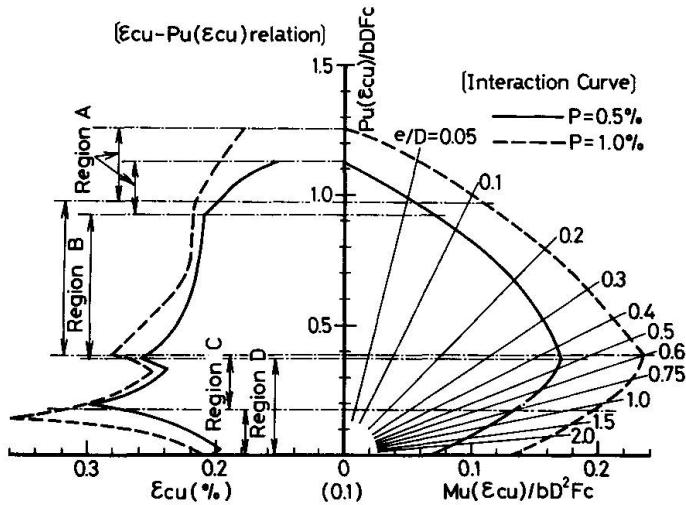


Fig. 6  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  -  $M_u(\epsilon_{cu})$  relations for rectangular column section (Curve I concrete stress-strain relation and  $F_y = 4000$  kg/cm<sup>2</sup> are used in calculation)

The numerical calculations of compressive fiber strain,  $\epsilon_{cu}$ , at ultimate strength were performed on the percentage of reinforcements,  $p = 0.5\%$  and  $p = 1\%$ , of rectangular column section shown in Fig. 2. The stress-strain relation of concrete as well as the yield strength of reinforcement adopted in calculation are Curve I in Fig. 5 and  $F_y = 4000$  kg/cm<sup>2</sup>, respectively. The results are shown by  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  relation with  $P_u(\epsilon_{cu})$  -  $M_u(\epsilon_{cu})$  interaction curve as in Fig. 6.  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  relations shown in Fig. 6 can be divided into following four regions.

Region A : Range that applied combined loads reach at their maximum without yielding of whole reinforcements.

Region B : Range that applied combined loads reach at their maximum after yielding of reinforcements in compression zone, where the stress in reinforcements in tensile zone still remains in elastic range.

Region C : Range that applied combined loads reach at their maximum after yielding of whole reinforcements.

Region D : Range that applied combined loads reach at their maximum after yielding of reinforcements in tensile zone, where the stress in reinforcements in compression zone still remains in elastic range.

In  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  relation for the section of  $p = 0.5\%$ , Region C disappears and is expressed border line between B and D.

It can be seen from Fig. 6 that the compressive fiber strain  $\epsilon_{cu}$  is much influenced by the combination of applied axial and flexural loads. In Fig. 6 the pure axial loading column section shows the minimum value of  $\epsilon_{cu}$ . These are listed in Table 1, which are a little larger than the strain,  $\epsilon_{cu} = 0.15\%$ , corresponding to the peak stress in concrete stress-strain curve. In Region A and B in Fig. 6, the compressive fiber strain  $\epsilon_{cu}$  increases gradually with increase of the relative degree of applied moment  $M(\epsilon_c)$  to applied axial force  $P(\epsilon_c)$ , that is, with increase of the eccentricity  $e = M(\epsilon_c)/P(\epsilon_c)$ . On the lower bound of Region B, the strain  $\epsilon_{cu}$  reaches at a peak value, where the corresponding ultimate flexural moment  $M_u(\epsilon_{cu})$  becomes maximum in the interaction curve. In Table 1, the values of  $\epsilon_{cu}$  on the lower bound of Region B are also listed. In Region C and D, considerable increase of  $\epsilon_{cu}$  is recognized after a little decrease near the upper bound of Region C or D, and the maximum value of  $\epsilon_{cu}$  is obtained at the middle portion of these range. After that, the value of  $\epsilon_{cu}$  decreases rapidly to the value of about 0.21%, which corresponds to the value for pure flexure. The maximum values of  $\epsilon_{cu}$  are also summarized in Table 1.

From such observation, it can be stated that for the exact calculation

Table 1 The values of  $\epsilon_{cu}$  for critical point in  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  relation (Curve I concrete stress-strain relation and  $F_y = 4000 \text{ kg/cm}^2$  are used in the calculation)

| Percentage of reinforcement  | $P$ (%)                      | 0.5   | 1     |
|--|------------------------------|-------|-------|
| For pure axial loading   | $\epsilon_{cu}$ (%)          | 0.152 | 0.180 |
|  | $P_u(\epsilon_{cu})/bDF_c$   | 1.125 | 1.250 |
|  | $M_u(\epsilon_{cu})/bD^2F_c$ | 0     | 0     |
| On the lower bound of Region A                                       | $\epsilon_{cu}$ (%)          | 0.211 | 0.217 |
|  | $P_u(\epsilon_{cu})/bDF_c$   | 0.920 | 0.970 |
|  | $M_u(\epsilon_{cu})/bD^2F_c$ | 0.070 | 0.107 |
| On the lower bound of Region B                                       | $\epsilon_{cu}$ (%)          | 0.267 | 0.281 |
|  | $P_u(\epsilon_{cu})/bDF_c$   | 0.370 | 0.390 |
|  | $M_u(\epsilon_{cu})/bD^2F_c$ | 0.171 | 0.233 |
| At the peak value in $\epsilon_{cu}$ - $P_u(\epsilon_{cu})$ relation | $\epsilon_{cu}$ (%)          | 0.300 | 0.360 |
|  | $P_u(\epsilon_{cu})/bDF_c$   | 0.195 | 0.140 |
|  | $M_u(\epsilon_{cu})/bD^2F_c$ | 0.139 | 0.185 |
| For pure flexure   | $\epsilon_{cu}$ (%)          | 0.204 | 0.210 |
|  | $P_u(\epsilon_{cu})/bDF_c$   | 0     | 0     |
|  | $M_u(\epsilon_{cu})/bD^2F_c$ | 0.068 | 0.132 |

\*  $F_c$  denotes the compressive strength of concrete.

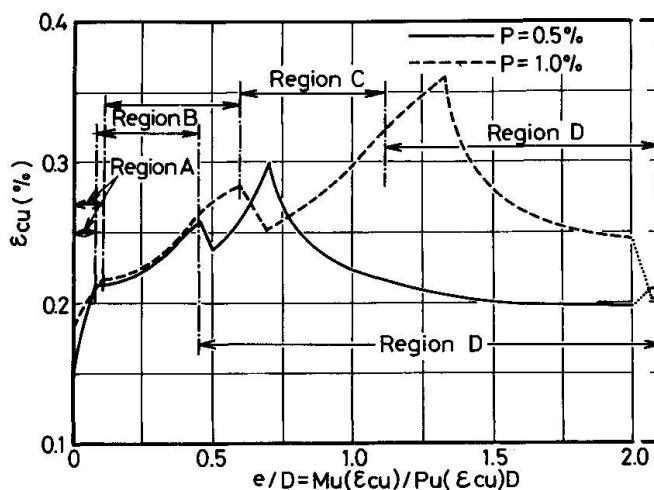


Fig. 7  $e$  -  $\epsilon_{cu}$  relations for rectangular column section of  $p = 0.5\%$  and  $1\%$  (Curve I concrete stress-strain relation and  $F_y = 4000 \text{ kg/cm}^2$  are used in calculation)

#### 6. Effects of the shape of stress-strain curve of concrete upon the compressive fiber strain $\epsilon_{cu}$

Using three different types of stress-strain curve of plain concrete shown in Fig. 5, the compressive fiber strain,  $\epsilon_{cu}$ , at ultimate strength was calculated on the rectangular column section having  $p = 0.5\%$ . The yield strength of reinforcement was assumed as  $4000 \text{ kg/cm}^2$  in the calculation. The results are illustrated in Fig. 8. While three interaction curves are very closed with each other, much difference can be seen in three results on  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  relation. Comparison between the results for concrete stress-strain Curve I and II shows that the larger compressive strain at the peak stress in stress-strain curve of

of maximum loading capacity, especially that of corresponding deflection of reinforced concrete member the change of compressive fiber strain,  $\epsilon_{cu}$ , as shown in Fig. 6 may be considered in correspondence to the combination of applied axial and flexural loads.

The effects of the percentage of reinforcement,  $p$ , upon the compressive fiber strain,  $\epsilon_{cu}$ , can be observed from  $e$  -  $\epsilon_{cu}$  relations shown in Fig. 7, which is rewritten from the results of Fig. 6. It seems from Fig. 7 that the effects of  $p$  is so small as negligible in Region A and B, while much difference of  $\epsilon_{cu}$  between  $p = 0.5\%$  and  $p = 1\%$  is observed in Region C and D.

Table 2 Effects of the type of concrete stress-strain curve upon  $\epsilon_{cu}$  for pure axial loading section of  $p = 5\%$  ( $F_y = 4000 \text{ kg/cm}^2$ )

| Type of stress-strain curve of concrete used in calculation | Ultimate axial load $P_u(\epsilon_{cu})/bDF_c$ | The value of $\epsilon_{cu}$ in % |
|---|--|-----------------------------------|
| Curve I   | 1.125  | 0.152                             |
| Curve II  | 1.160  | 0.208                             |
| Curve III   | 1.125  | 1.151                             |

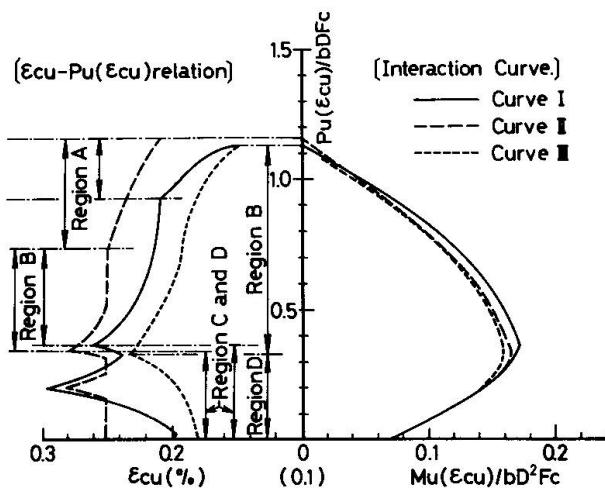


Fig. 8 Effects of the type of concrete stress-strain curve upon the compressive fiber strain,  $\epsilon_{cu}$ , at ultimate strength ( $p = 0.5\%$ ,  $F_y = 4000 \text{ kg/cm}^2$ )

concrete results in the larger values of  $\epsilon_{cu}$  within Region A and B in  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  relation. The difference between the compressive fiber strains for Curve I and II becomes maximum in the case of pure axial loading. As a reference, the values of  $\epsilon_{cu}$  obtained for pure axial loading are summarized in Table 2. On the contrary it appears from the comparison of the results for concrete stress-strain Curve III with that for Curve I that the increase of negative inclination in strain softening region of concrete stress-strain relation reduces the compressive fiber strain at ultimate strength of reinforced concrete section, while no obvious effect is recognized on the section subjected to pure axial force.

### 7. Effects of the yield strength of reinforcement, $F_y$ , upon $\epsilon_{cu}$

Fig. 9 shows the results of numerical calculation on the ultimate strengths,  $P_u(\epsilon_{cu})$  and  $M_u(\epsilon_{cu})$ , and corresponding compressive fiber strain,  $\epsilon_{cu}$ , for rectangular column section of  $p = 0.5\%$  having various yield strengths of reinforcement. The stress-strain relation of concrete used in calculation is Curve I in Fig. 5.

Comparison between the results for  $F_y = 4000 \text{ kg/cm}^2$  and  $F_y = 5000 \text{ kg/cm}^2$  shows that Region A in  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  relation becomes larger with increase of the yield strength of reinforcement, which results in the considerable increase of compressive fiber strain,  $\epsilon_{cu}$ , in Region B. In Fig. 9, the strain  $\epsilon_{cu}$  in Region B for  $F_y = 5000 \text{ kg/cm}^2$  is about 0.05% larger than that for  $F_y = 4000 \text{ kg/cm}^2$ .

The use of reinforcement having smaller yield strength provides the decrease of Region A in  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  curve. In Fig. 9, Region A disappears in  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  relation for  $F_y = 2400 \text{ kg/cm}^2$  because the yield strain of reinforcement is smaller than the strain corresponding to the peak stress in stress-strain curve of concrete. In such case, the strain  $\epsilon_{cu}$  for pure axial loading just coincides with the strain at peak stress in concrete stress-strain relation.

### 8. Conclusions

Based on the general concept that the ultimate loading capacity of reinforced concrete section is defined as the loads satisfying the equation  $dP(\epsilon_c)/d\epsilon_c = 0$  or  $dM(\epsilon_c)/d\epsilon_c = 0$ , corresponding compressive fiber strain of concrete,  $\epsilon_{cu}$ , was calculated numerically on the rectangular column section and the effects of the combination of applied axial and flexural loads, the percentage of reinforcement, the shape of stress-strain curve of concrete and the yield strength of reinforce-

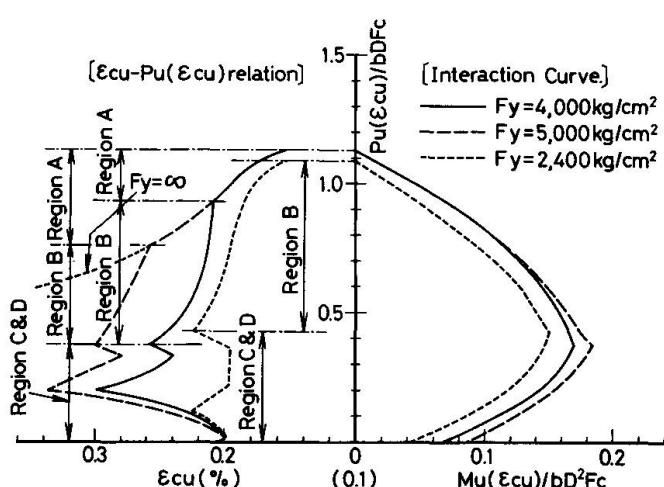


Fig. 9 Effects of the yield strength of reinforcement upon  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  relations of rectangular column section of  $p = 0.5\%$  (Curve I concrete stress-strain relation is used in the calculation)

intensity of applied axial load is larger in comparison with applied flexural moment.

(3) The larger strain at peak stress in concrete stress-strain curve increases the value of  $\epsilon_{cu}$  within Region A and B of  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  curve, especially the maximum increase of  $\epsilon_{cu}$  is obtained in case of pure axial force. Also, the increase of negative slope of strain softening region in concrete stress-strain curve reduces the value of  $\epsilon_{cu}$  considerably. These factors have no obvious effects on the ultimate axial load and flexural moment interaction curve of section.

(4) The use of reinforcements having larger yield strength results in considerable increase of  $\epsilon_{cu}$  in region B of  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  curve.

(5) The effects of the factors described in this paper upon the value of  $\epsilon_{cu}$  may be necessary to consider for the exact estimation of ultimate strength as well as corresponding deformation of reinforced concrete member.

#### References

- 1) E. Hognestad, N. W. Hanson & D. McHenry: Concrete Stress Distribution in Ultimate Strength Design, J. of A.C.I., Vol. 52, No. 6, pp. 455~479, Dec. 1955.
- 2) S. Morita & N. Adachi: The Stress-Strain Behaviour of Concrete in the Compression Zone of Flexural Members, Proc. of the International Conference on Mechanical Behavior of Materials, Vol. IV, pp. 162~171, 1972.
- 3) R. F. Warner: Physical-Mathematical Models and Theoretical Considerations, Introductory Report on IABSE Symposium on Design and Safety of Reinforced Concrete Compression Members, pp. 1~21, April 1973.
- 4) F. Watanabe: Complete Stress-Strain Curve for Concrete in Concentral Compression, Proc. of the International Conference on Mechanical Behavior of Materials, Vol. IV, pp. 153~161, 1972.
- 5) H. Muguruma & S. Tanaka: Mechanical Properties of High Strength Concrete, Annual Report of Japan Cement Association, XXVII, 1973, (in Japanese).

ment, etc. upon the compressive fiber strain were investigated. The following conclusions are obtained from the results.

(1) The compressive fiber strain  $\epsilon_{cu}$  varies considerably with the relative intensity of applied flexural moment to axial load.  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  relation obtained in this paper can be divided into four regions in corresponding to the yielding of reinforcement. The value of  $\epsilon_{cu}$  becomes minimum in the case of pure axial loading and the increase of eccentricity results in the gradual increase of  $\epsilon_{cu}$ . Also it decreases with increase of eccentricity after reaching the maximum value near pure flexure.

(2) No obvious effects of the percentage of reinforcement upon the value of  $\epsilon_{cu}$  are recognized within Region A and B of  $\epsilon_{cu}$  -  $P_u(\epsilon_{cu})$  curve, where relative

SUMMARY

Numerical estimations were made on the value of extreme compressive fiber strain of concrete at ultimate strength of reinforced concrete column section subjected to various combinations of axial and flexural loads. The results showed that the extreme compressive fiber strain is much affected by many factors such as the combinations of axial and flexural loads, the characteristics of stress-strain relation of concrete, the yield strength of reinforcement and the percentage of reinforcements, etc.

RESUME

On a estimé la valeur de la tension de compression extrême dans le béton d'une colonne en béton armé soumise à diverses combinaisons de flexions et d'efforts axiaux. Les résultats montrent que l'allongement spécifique dans le béton varie considérablement en fonction de facteurs tels que les combinaisons de flexions et d'efforts axiaux, les caractéristiques de la courbe tension-déformation du béton, la limite d'élasticité des armatures, le pourcentage d'armature, etc.

ZUSAMMENFASSUNG

Zahlenmässige Schätzungen für den Wert der grössten Druckstauchung von Beton bei der Bruchbeanspruchung von Stahlbeton-Stützenquerschnitten unter Einwirkung verschiedener Kombinationen von Normalkraft und Biegemomenten wurden vorgenommen. Die Ergebnisse zeigten, dass die grösste Druckstauchung durch eine Reihe von Faktoren, wie die Kombination von Normalkraft und Biegemoment, den Verlauf des Spannungs-Dehnungs-Diagramms von Beton, die Streckgrenze der Bewehrung, den Bewehrungsgehalt usw. beeinflusst wird.