Zeitschrift: IABSE congress report = Rapport du congrès AIPC = IVBH

Kongressbericht

Band: 9 (1972)

Artikel: Some practical considerations on the postcritical behaviour of structures

Autor: Kollár, Lajos

DOI: https://doi.org/10.5169/seals-9544

Nutzungsbedingungen

Die ETH-Bibliothek ist die Anbieterin der digitalisierten Zeitschriften auf E-Periodica. Sie besitzt keine Urheberrechte an den Zeitschriften und ist nicht verantwortlich für deren Inhalte. Die Rechte liegen in der Regel bei den Herausgebern beziehungsweise den externen Rechteinhabern. Das Veröffentlichen von Bildern in Print- und Online-Publikationen sowie auf Social Media-Kanälen oder Webseiten ist nur mit vorheriger Genehmigung der Rechteinhaber erlaubt. Mehr erfahren

Conditions d'utilisation

L'ETH Library est le fournisseur des revues numérisées. Elle ne détient aucun droit d'auteur sur les revues et n'est pas responsable de leur contenu. En règle générale, les droits sont détenus par les éditeurs ou les détenteurs de droits externes. La reproduction d'images dans des publications imprimées ou en ligne ainsi que sur des canaux de médias sociaux ou des sites web n'est autorisée qu'avec l'accord préalable des détenteurs des droits. En savoir plus

Terms of use

The ETH Library is the provider of the digitised journals. It does not own any copyrights to the journals and is not responsible for their content. The rights usually lie with the publishers or the external rights holders. Publishing images in print and online publications, as well as on social media channels or websites, is only permitted with the prior consent of the rights holders. Find out more

Download PDF: 27.12.2025

ETH-Bibliothek Zürich, E-Periodica, https://www.e-periodica.ch

Some Practical Considerations on the Postcritical Behaviour of Structures

Quelques remarques pratiques sur le comportement des structures dans le domaine post-critique

Praktische Bemerkungen über das Verhalten der Konstruktionen im überkritischen Bereich

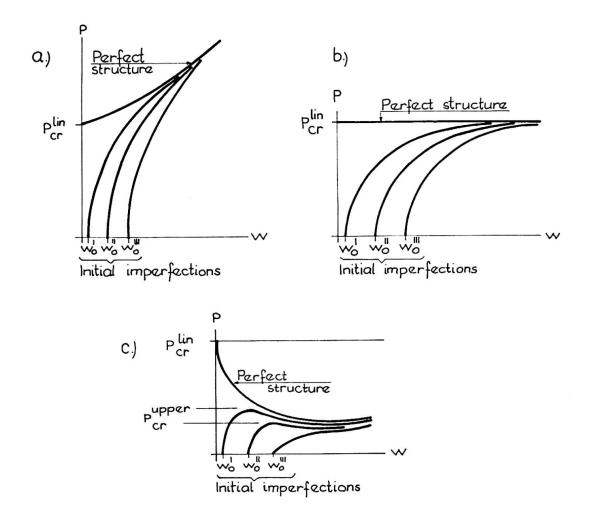
> LAJOS KOLLÁR Dr. techn. Budapest, Hungary

In the following the postcritical behaviour of structures would be dealt with from the viewpoint of their practical applications.

Basically, three different types of postbuckling behaviour can be distinguished. The load-bearing capacity of the structure can be - after exceeding the critical load Plin of the classical /linear/ theory - either increasing, or constant, or decreasing. Plotting the load P against some average value of the buckling deformation w, these three cases can be represented by the diagrams of Figs. la,b,c. Here, in addition to the perfect /centrally compressed/ case, some curves corresponding to initially imperfect structures have been represented too.

Structures with <u>increasing</u> postbuckling load-bearing capacity /Fig. la/ are insensitive to initial imperfections and/or creep because their diagrams have no peak which could be influenced by these two factors. On the other hand, structures with <u>decreasing</u> diagrams /Fig. lc/ are extremely sensitive to initial imperfections and creep as well, for the peak value of their P/w/-curves depend markedly on the magnitude of both. /The influence of creep is similar to that of initial imperfections because creep increases buckling deformation, thus it augments the influence of the imperfection./ We can thus choose a much smaller safety factor for structures corresponding to Fig. la than to those of Fig. lc.

Structures corresponding to Fig. lc form a case of transition between the two other groups. Its importance comes mainly from the fact that it can be treated theoretically in a simple way, but it also describes, at least approximatively, the behaviour of some structures /e.g. buckling of bars/.



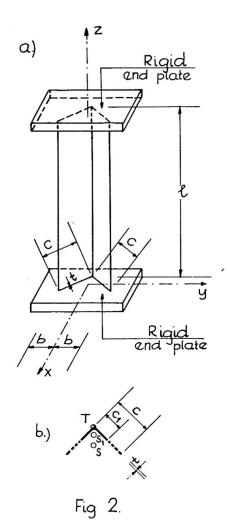
Fiq. 1.

From all that has been said follows that when designing a structure, it is most important to know whether its postbuckling load-bearing capacity increases or decreases. For some structures we know this from theoretical investigations to be found in the literature. But if we have to design a structure the postbuckling analysis of which has not yet been made, some simple criteria to determine the kind of its postbuckling behaviour could be of great value. In the following some such criteria will be shown.

Theoretically it can be said [2], [3] that a structure has an increasing postbuckling load-bearing capacity if the following two conditions are fulfilled:

- a/ The structure must have some parts which can bear more load, even without the other, more buckled /weaker/ parts, than the whole structure.
- b/ The redistribution of stresses that is necessary for con-

dition a/ must be physically possible in the structure itself as well as at the supports.



Let us illustrate this on the pure torsional buckling of a straight bar with the cross section of an angle /Fig. 2a/. When the critical load is exceeded, the angle begins to buckle with the rotation of the cross sections around their shear centre T /Fig. 2b/. We can assume, as an approximation, that the free ends of the cross sections cease to bear any load. Thus, instead of the original flange width c of the angle only a part of it, of width c1, will be effective. This part, however, can carry more load than the original whole structure. This can be seen in the formula for the critical load of torsional buckling for an angle with built-in ends 5:

$$P_{cr} = 2 \frac{G t^3}{c}$$
.

Since P_{cr} is inversely proportional to flange width c, the smaller c, the greater the critical load will be. Condition a/ is thus fulfilled.

In this case the redistribution of stresses means that the point of action of the load must shift from the original centroid S to the centroid S_1 of the smaller cross section. If the end conditions make this possible /e.g. in case of rigid end plates/, then condition b/ is also fulfilled, thus we obtain an increasing postbuckling load-bearing capacity.

Essentially the same considerations can be made in relation to the torsional buckling of shell-arches 1, 3, plate buckling 5 etc., i.e. in all cases where the critical load is inversely proportional to some dimension of the structure, and even in some other cases. Sometimes it is also possible to establish a simple upper bound for the maximum value of the postbuckling load the

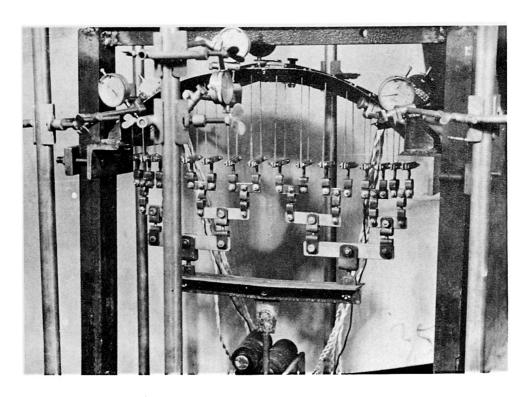


Fig. 3.

load P_{cr}^{lin} = 512 kp, the load-deflection curve has a markedly ascending character, represented in Fig. la.

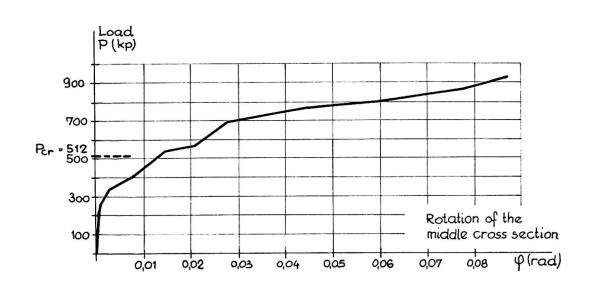


Fig. 4.

structure can carry 2 . For illustration, Fig. 3 shows a steel model of a shell-arch with built-in ends under centrical compression. The rotation of the middle cross section, as characteristic for the torsional buckling, is plotted in Fig. 4. After exceeding the linear critical

> In cases, however. when these theoretical considerations cannot be applied, there is another possibility to predict postbuckling behaviour from nondestructive model tests.

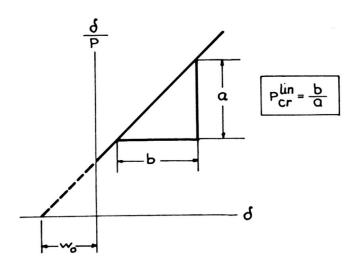
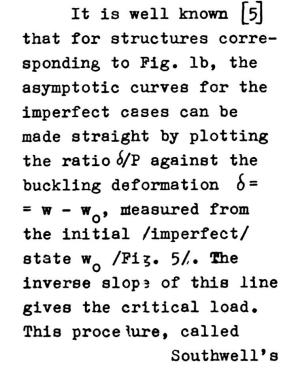
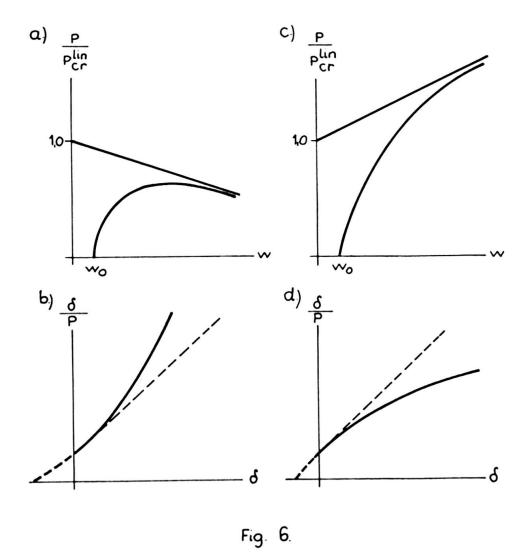


Fig. 5.





be easily shown [2], [4] that in case of increasing or

decreasing

plot, greatly facili-

tates the determination of this latter since

it would be much more

uncertain to

determine the asymptotic value

curves in Fig. 1b by

polation.

It can

of the

extra-

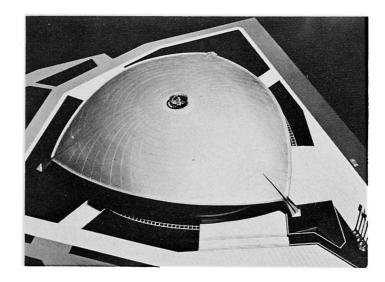


Fig. 7.

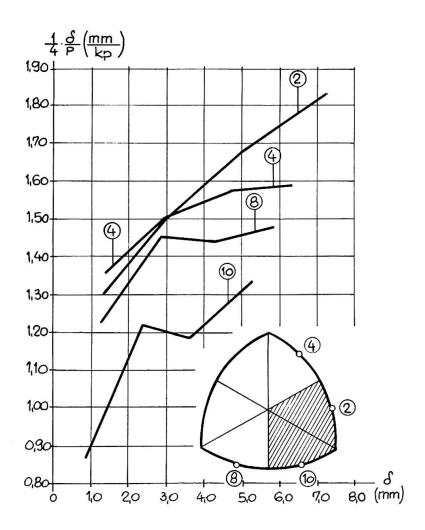


Fig. 8.

postbuckling loadbearing capacities, the Southwell diagram becomes curved downwards or upwards, respectively /Fig. 6/. Thus, measuring the buckling deformations of the model and plotting δ/P against them, we can decide at once and without destructing the model whether it has a constant /Fig. 1b/, an increasing /Fig. la/ or a decreasing /Fig. lc/ postbuckling load-bearing capacity.

For illustration we show some
results of the model
test of the new
Budapest Sports Hall,
designed recently
/Fig. 7/. Its structure is a reticulated steel shell
without stiffening
edge arches, supported by three
points at a distance of 112.80 m.

For the stability of the structure only rough estimates could be made in the course of design. Thus we had to resort to a model test. Since we intended to study its behaviour under several loading cases, it was desirable to clear up postbuckling characteristics by a non-destructive model test in order to avoid costs of several models. Fig. 8 shows the Southwell diagrams of four edge points for the loading indicated by hachure. All diagrams show a definite downward curvature. The ensuing increasing postbuckling load-bearing capacity has been confirmed by the final test when we loaded the model with total load up to failure.

I hope these viewpoints might be of some use for designers.

References

- [1] Kollár, L.: On Postbuckling Behaviour of Shell-arches.

 Bulletin of the International Association for Shell Structures, N. 30, June 1967, 21-32.
- [2] Kollár, L.: On the Behaviour of Shells in the Post-Buckling
 Range
 Bulletin of the International Association for
 Shell Structures, N. 39, Sept. 1969, 41-51.
- [3] Kollár, L.: Statik und Stabilität von Schalenbogen und Schalenbalken.

 W. Ernst und Sohn, Berlin Akadémiai Kiadó, Budapest, 1971.
- [4] Roorda, J.: Some thoughts on the Southwell plot.

 Journ. Eng. Mech. Div. /Proc. ASCE/ 93 EM 6,

 37-48 /Dec. 1967/
- [5] Timoshenko, S. Gere, J.: Theory of Elastic Stability.
 McGraw-Hill, New York, 1971

Summary

After description of the three main types of postbuckling behaviour of structures two conditions, necessary for the increasing postbuckling load-bearing capacity, will be established. For determination of postbuckling behaviour from non-destructive model tests, the generalized Southwell plot will be presented.

Leere Seite Blank page Page vide