Inelastic behavior of steel framed structure subjected to the seismic force

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Inelastic Behavior of the Steel Framed Structure Subjected to the Seismic Force

Comportement inélastique de structures en câdres d'acier soumises à des forces sismiques

Unelastisches Verhalten des Stahlrahmentragwerkes unter Erdbebenkraft

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Introduction

To clear the safety of the structure against earthquake, it is necessary to know the inelastic behavior of beams, columns and entire frames until their collapse state under alternating loading as the author states. This discussion concerns to evaluation of the inelastic behavior of steel structural members.

It is known that the conventional simple plastic theory cannot predict the actual inelastic behavior of the steel structures even in monotonous loading, and it can be said that this mainly comes from the fact that the strain hardening property of the material is not taken into account in that analysis, and the effect of the applied axial load is not evaluated reasonably.

We suggest the solution for the beam-column subjected to axial compression and bending moment which makes allowance for the strain hardening and the effect of the axial compression. The load deflection diagram under alternating loading is shown to be obtained from the load deflection diagram under monotonous loading by the simple definite procedure.

Furthermore, the response analysis of the one mass vibration model of the steel structure is done using the clarified inelastic characteristics, and the difference of the response is shown to be attributed to the difference of evaluation of the effect of the strain hardening upon the structure.

Inelastic Behavior of Steel Members

Monoaxial bending only is treated here, and the effect of shear stress is ignored. Lateral buckling is also out of the matter. Breaking-off and local buckling of the section element of the member are considered to be the most effective origins of the collapse of the member and these origins can be predicted by some material tests.

General feature of the stress strain relation of steel may be expressed by the diagram as shown in Fig.(1).

As the bending deformation is obtained by integration of the

curvature along member axis, to determine the moment curvature relation is the essential procedure.

Moment Curvature Relation --- Case I when the bending moment is applied in monotonous way: The bending moment is to be applied about x-x axis in Fig. (2), and the section of the member is assumed to be symmetric about the axis perpendicular to the bending axis. Axial compression is kept in constant, and the moment increases gradually.

Let the solid line of Fig.(3) be the strain distribution at the arbitrary inelastic state under moment M, and the broken line be that of after infinitecimal increase of the curvature due to the increase of moment. Then the following relation are derived from the equilibrium condition of stress.

 $dH_1 = -\frac{d\phi}{\phi} H_1$, $dH_1' = -\frac{d\phi}{\phi} H_1'$, $dH_2 = -\frac{d\phi}{\phi} H_2$, $dH_2' = -\frac{d\phi}{\phi} H_2'$ $dS_{e} = (dH_{1}B_{1} + dH_{2}B_{2})e_{1} + (dH_{1}'B_{1}' + dH_{2}'B_{2}')e_{2}$ $dI_{e} = (dH_{1}B_{1}H_{1}' + dH_{2}B_{2}H_{2}')e_{1} + (dH_{1}'B_{1}'H_{1}' + dH_{2}'B_{2}'H_{2}')e_{2}$ $dO = \left\{ -(dH_{1}B_{1}H_{1} - dH_{2}B_{2}H_{2})e_{1} - (dH_{1}'B_{1}'H_{1}' - dH_{2}'B_{2}'H_{2}')e_{2} \right\} / S_{e}$ where ϕ : curvature $d\phi$: increment of ϕ

e,: strain at yield point

Est: strain at strain hardening point

 $e_{1}: (E_{1}-E_{2})/E_{1} e_{2}: (E_{2}-E_{3})/E_{1}$

H₁: distance from the transient neutral axis to the compression fibre where the strain is equal to ε_y .

H2: distance from the transient neutral axis to the tension fibre where the strain is equal to- ε_{y} .

Hi: distance from the transient neutral axis to the compression fibre where the strain is equal to $\mathcal{E}_{\mathsf{st}}$.

 H_2 : distance from the transient neutral axis to the tens-

ion fibre where the strain is equal to- ξ_{ℓ} . See effective area, which means the sectional area of the ficticious elastic bar which has the equivalent axial rigidity to the actual bar in the specified inelastic state.

Ie: effective moment of inertia, which means the moment of inertia of the ficticious elastic bar which has the equivalent flexural rigidity to the actual bar in the specified inelastic state.

dO: movement of the transient neutral axis

 B_{i} , B_{i}' : width of the section at H_{i} , H_{i}' respectively. After the increase of the curvature do, these quantities will change as follows.

 $H_1 \rightarrow H_1 + dH_1 + dO$, $H_2 \rightarrow H_2 + dH_2 - dO$ $H_1 \rightarrow H_1 + dH_1 + dO$, $H_2 \rightarrow H_2 + dH_2 - dO$

 $S_e \rightarrow S_e + dS_e$, $I_e \rightarrow I_e + dI_e$, $\phi \rightarrow \phi + d\phi$, $M \rightarrow M + E$, $I_e d\phi$ $exttt{M-}\phi$ relation may be pursued successively using the above relaion throughout the whole strain range. Numerical calculation is performed easily by the aid of the electronic digital computer.

Case II when the bending moment is applied alternatingly: It is very complicated to describe the exact M- ϕ relation under alternating bending. So by the aid of the simplified model given below, an outline of the relation is sought after.

1. Member section is sandwitch type as shown in Fig(4).

2. Stress strain relation of steel under alternating loading is as shown in Fig. (5b). To be more precise, with regard to the stress in definite sign the stress strain relation has the same configuration as that under monotonous loading as shown in Fig. (5a).

On such a model it is easily understood that the M- ϕ relation under alternating loading is obtained as shown in Fig.(6b). Fig.(6a) shows the M- ϕ relation under monotonous bending. Comparing Fig.(6a) and Fig.(6b), it can be seen that in Fig.(6b) with regard to the bending moment in one direction the M- ϕ relation has the same configuration as that shown in Fig.(6a).

The actual shape of section differs from that provided by the condition 1. Hence when the bending moment is removed, the residual stress is introduced over the section. In this paper, however, the effect of such a residual stress is assumed to be negligible, so the M- ϕ relation obtained above becomes applicable to any section.

Load Deflection Curve of Steel Members--- Deflection of the member is readily obtained by integration of the curvature corresponding to the bending moment produced by the external loads. For the exact solution numerical integration technique is effective, but in some cases approximate solution provides facility for engineering purposes. Especially the solution under alternating loading is uselessly troublesome. Hence for this case some devices in approximation are needed.

When the bending stress is determined uniquely by the external loads, the correlation between the load deflection curve under alternating loading and that under monotonous loading is similar to the correlation as exists in M- φ relation. As is shown in Fig.(7), the load deflection diagram under alternating loading is readily obtained from that under monotonous loading. With regard to a definite direction of loading, the load deflection curve in Fig.(7b) has the same configuration as that in Fig.(7a).

But in general, geometry change of the member affects upon the bending moment distribution. In Fig.(8) two cantilever columns are shown for example. When the end load is applied alternatingly under constant axial load P, lateral deflection produces secondary bending. When the end load is removed after some extent of the inelastic deformation in one direction, deflection remains and to remove the residual moment at the fixed end, end loads of $-P\delta/\gamma$ in the case of Fig.(8a) and $-P\delta$ in the case of Fig.(8b) are required respectively. In such a state residual stress still remains along the member axis as shown in Fig. (9). Here, we assume that the residual stress shown in Fig. (9) has no effect upon the load deflection relation under further application of the end load in the opposite direction. Based on the assumption, we can depict the load deflection curve as shown in Fig. (10), that is, the load deflection curve under alternating loading is obtained from that under monotonous loading in the same manner as is shown in Fig.(7). In Fig.(7) the abscissa is the basal line whereas in Fig. (10) the broken line which shows the tentative unloaded state of the member is the basal line, and with regard to the load deflection relation in one side of this line, the curve under alternating loading has the same configuration as that under monotonous loading. From this figure it can be seen that the summation of the plastic deformation in one direction until collapse does not exceed the plastic deformation capacity under monotonous loading.

Comparison with Test Result --- Load deflection curves were obtained using the test specimens as shown in Fig.(11). In specimen(A) the column is subjected to axial thrust and the transverse shear force increasing proportionally according to

the following condition.

 $\text{P=V}\cos \psi$, $\text{Q=V}\sin \psi$ Where V is the applied load.

In specimen(B) the column is subjected to constant axial load and alternating end moment conducted through beams.

Stress strain relation of the material was obtained from the stub column test, and is shown in Fig. (12). The maximum stress was reached by occurence of the local buckling of flanges. M- ϕ relation obtained from the procedure mentioned above

is shown in Fig.(13). Load deflection curve of the specimen(A) is shown in Fig.(14), and the curve of the specimen(B) is shown in Fig. (15) in which the theoretical curve under monotonous bending is shown by the curve ABC.

Collapse of the member was assumed to occur when the stress at the point where the maximum moment grows reachs of over entire section. MB corresponds to such a stress distribution. In Fig. (14) and (15) theoretical curves after collapse are drawn on the assumption that the maximum moment of the specimen is kept to be MB.

In these figures the test results agree with the theoretical prediction fairly well, and the effect of the strain hardening upon the inelastic behavior is very remarkable.

Response Analysis of the Framed Structure

Restoring Force Characteristics --- The cantilever column shown in Fig. (16) represents the fundamental element of the framed structure subjected to seismic force. To see the general feature of resistance of the framed structure to seismic force, a simple outline of the inelastic behavior of the cantilever col-

umn is sought after through the approximate approach.

The M-prelation under the constant thrust obtained above may be approximated by two linear segments ignoring the elastic part of it. The first segment is parallel to the abscissa at Mr.

At first the deflection of the member is evaluated ignoring the effect of the secondary bending caused by the geometry change. In Fig.(17) the part of the column ab is in inelastic range under the given loads P and Q, the the distribution of the curvature along the member is expressed as shown in Fig.(17b). This is reduced to the simplified model as shown in Fig.(17c) in which the curvature of the inelastic part ab is approximated by the mean value of the curvatures at the both ends of ab, then

the mean value ϕ_o may be written as follows.

 $\phi_o = \frac{\Phi_{st} + \Phi_f}{2} = \frac{M_f - M_{PC}}{2D_{st}} + \phi_{st}$ 2D_{st}

Where $\phi_{\rm st}$: the curvature at the starting point of the strain hardening.

> D_{st}: the flexural rigidity in strain hardening range. Namely the slope of the second segment.

 $M_{\text{R}}\colon$ the fully plastic moment under axial force. $M_{\text{f}}\colon$ the fixed end moment

The lateral deflection \mathcal{S}_{b} and the slope \mathcal{G}_{b} at point b are given as follow.

Then the lateral deflection at the top of the member may be given as follows.

 $\mathcal{E}_{l} = \frac{\mathcal{L}_{l} l_{+}(\mathcal{P}_{l} l_{+}^{2})}{2}$ (2) $l_{+}: \text{ the length of the inelastic part of the member.}$ Where \tilde{l}_{2} : the length of the elastic part of the member. As the bending effect of the thrust P is ignored, the following

relation will hold for any shear force Q'.

 $Q'l_2 = M_{PC}$, $Q'l = Q'(l_1 + l_2) = M_L$

These are translated as: $l_1/l_1 = (\alpha-1)/\alpha \ , \quad l_2/l_1 = l/\alpha \ , \quad \alpha = M_f/M_{PC}$ From equation(1) and (2), introducing the expression $M_{PC} = D \ \phi_y$, and $\beta = \phi_{st}/\phi_y$, the lateral deflection is written as follows.

$$S = (\underline{\alpha - 1}_{2} \times \underline{D}_{st} + \beta) (\underline{\alpha^{2} - 1}_{2\alpha^{2}}) \ell^{2} \phi_{y}$$
 (3)

Where D: flexural rigidity in the elastic range As the second step, the effect of the secondary bending must be taken into account. This effect is illustrated in Fig. (18) where the curve ac shows the deflected configuration of the member. Horne*had approximated this configuration by the straight line connecting the both ends of the members as shown in Fig. (18a). Then the equivalent lateral force Q which provide the same bending moment at the fixed end is given as follows.

 $Q = (M_f - PS)/I = (\alpha M_{PC} - PS)/I$

Equation (3) and (4) give the Q-S relation.
This approximation, however, underestimates the secondary bending and the another approximation as shown in Fig.(18b) is proposed, where the point shows the coordinate $(\S, (\alpha-1)l/2\alpha)$. $(\alpha-1)l/2\alpha$ denotes the midheight of the inelastic portion, and the deflected shape of the member is approximated by the straight line also. This choice seems to be rather arbitrary, but it will be shown later that this gives the better approximation to the exact solution. In this approximation the equivalent horizontal shear force is given as follows.

 $Q = \left\{\alpha M_{PC} - \left(\frac{2\alpha}{2}\right)PS\right\} / 1$ (5)

Comparison with the exact solution is made in Fig. (19) with regard to the Q-8 relation using the same section member as shown in Fig.(11), and the same stress strain relation as shown in Fig.(12).

In the case of no axial thrust these two methods coincide, however when the axial force becomes larger, it can be seen that the later method gives better approximation than the former one. In Fig. (20) Q-8 diagram for the same member derived from the conventional theory ignoring the strain hardening is given.
Comparing these two figures, it can be seen that the effect of the strain hardening is very significant.

Besides, from Fig.(19) it can be seen that the inelastic

deflection curve may be approximated by the linear relation without substantial error. Hence the fundamental feature of the restoring force characteristics of the framed structure may be

suggested to be the relation as shown in Fig.(10).

Response Analysis of the 1 Mass System--- Using the restorig force characteristics given in Fig.(21) the response analysis was done . For an example, one mass viburation system as shown in Fig. (21) is chosen.

The ground motion is of N-S component of El Centro 1940, May(the peak value of acceleration is 330 gals)

Governing equation of the sytem is as follows.

 $\mathbf{m}(\mathbf{\hat{y}}+\mathbf{\hat{y}}_{o})+\mathbf{f}(\mathbf{y})=0$

, yo: ground motion y: deflection , yo: ground motion f(y): restoring force characteristics Where

Result of the analysis is given in Fig. (22). Fig. (22a) shows the residual plastic deflection after the ground motion is faded away. Fig. (22b) shows the maximum deflection during the

earthquake and Fig. (22c) shows the summation of the plastic deflection in one direction.

The ordinate of these diagram expresses the yield force coefficient which is given as follows.

Where g: acceleration of gravity The abscissa expresses the plastic deflection divided by the initial elastic limit deflection which corresponds to the initial elastic limit stress Fy.

In these figures, the parameter K denotes the strain hardening effect. When the strain hardening does not exist, the value is equal to the slope of the basal line ff'in Fig. (21) which denotes the effect of the secondary bending by the weight of the

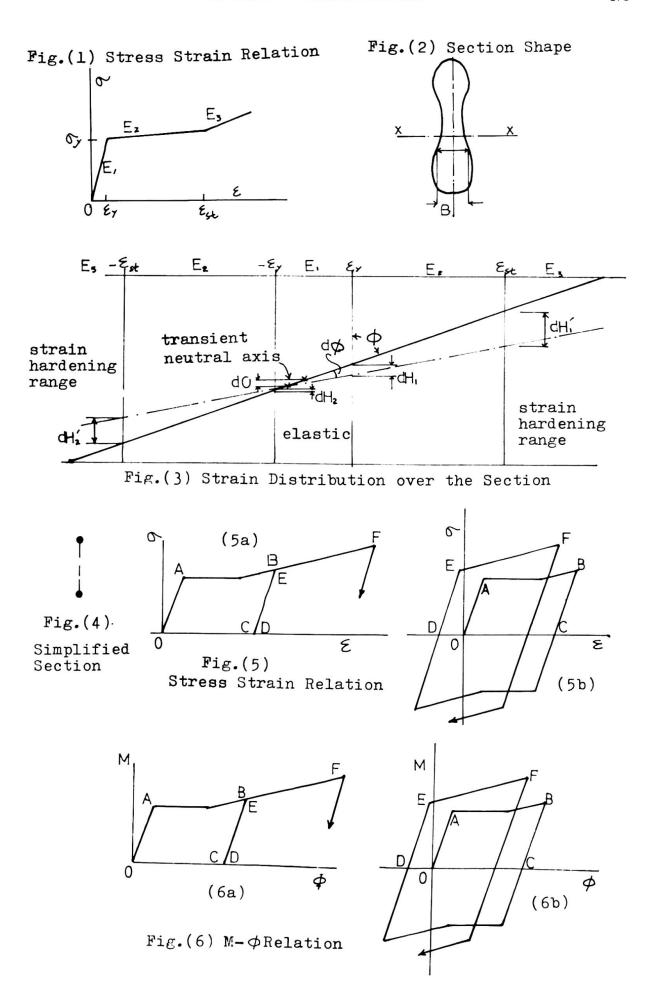
From these figure it can be seen that the plastic deflection is considerably affected by the strain hardening effect and especially development of the residual deflection is moderated by the strain hardening.

Conclusion

The more precise aspect of the inelastic behavior of the steel members has been pursued by the experiment and the analysis which makes allowance for the strain hardening property of steel.

The effect of the strain hardening property upon the deflection response of the steel framed structure to an earthquake was evaluated, and that was shown to be very remarkable.

 $[\]frac{\text{Reference}}{\text{* Horne M.R.}}, \, \frac{\text{Redland I.C.}}{\text{Medland I.C.}}: \, \text{Collapse Loads of Steel Frameworkes} \\ \text{Allowing for the Effect of Strain Hardening.}$ Proc. Institution of Civil Engineers 1966, May



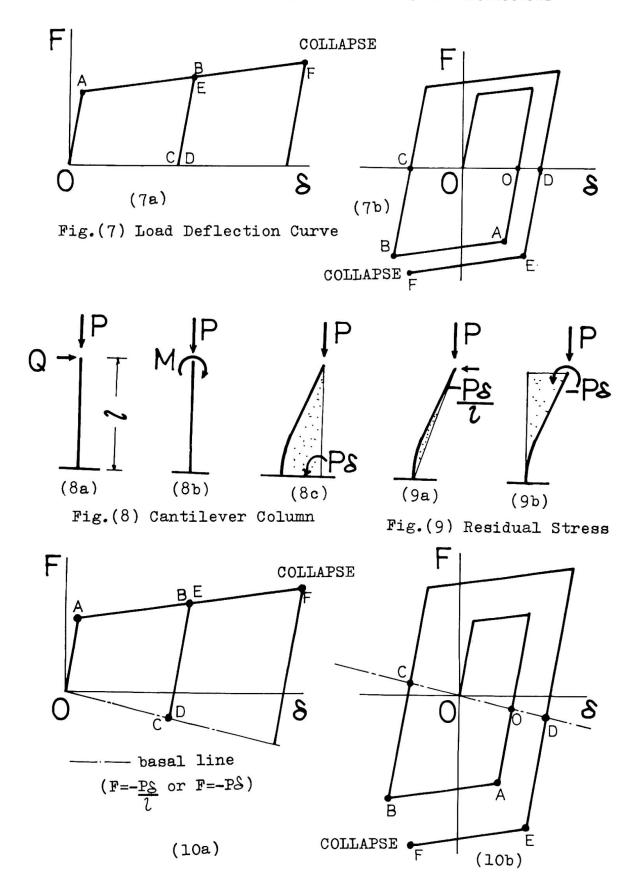
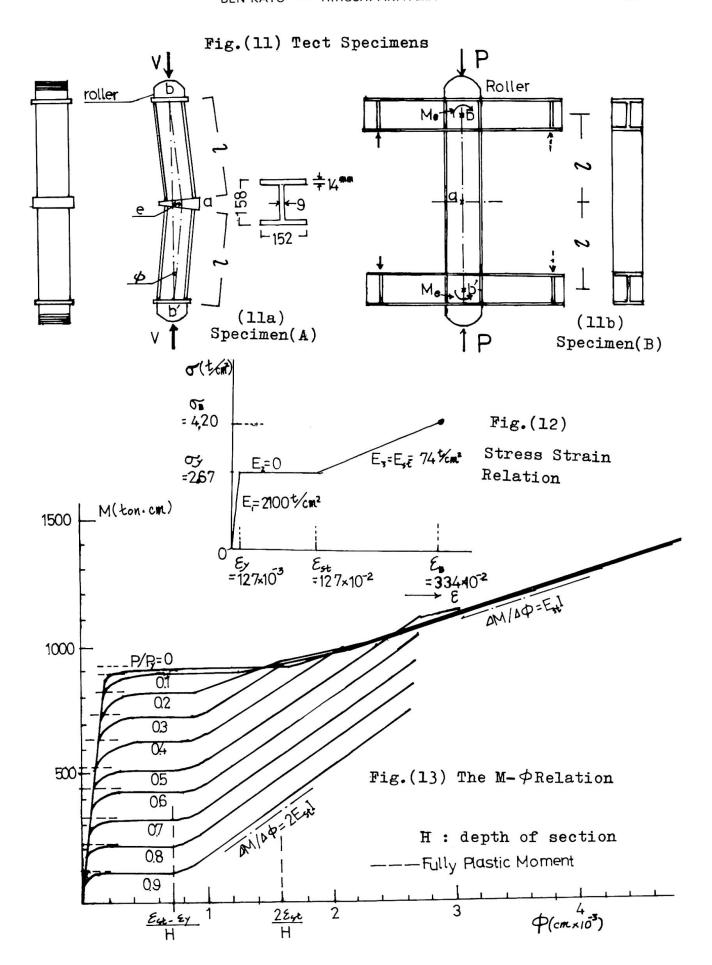
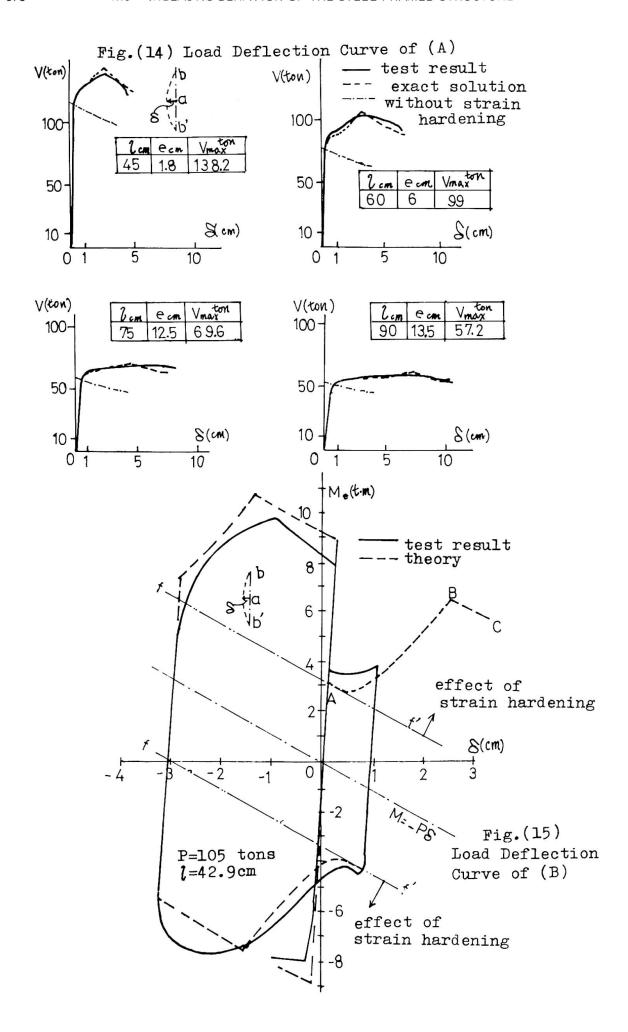
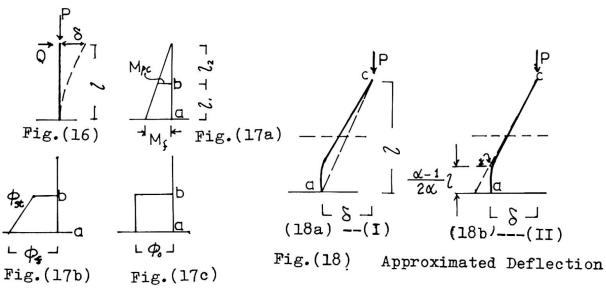
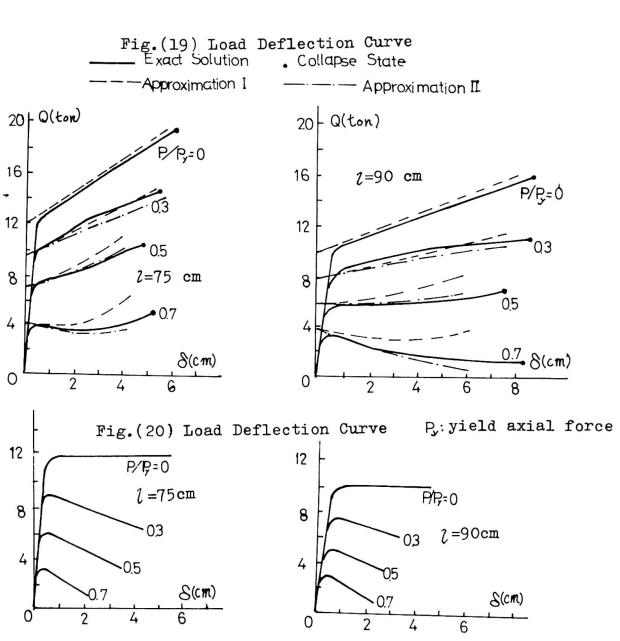


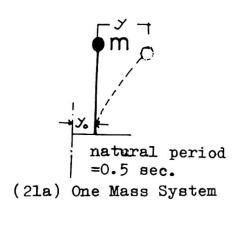
Fig. (10) Load Deflection Curve under Alternating Loading

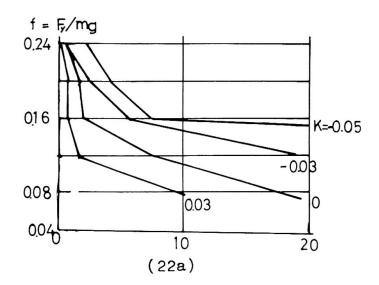


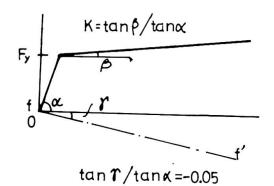












Restoring Force Characteristics

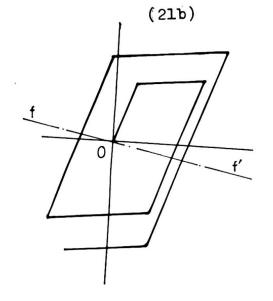
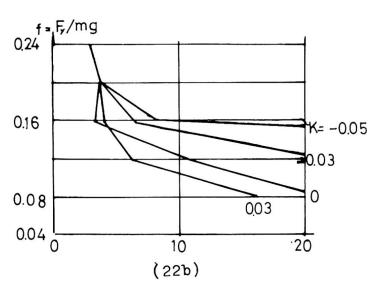


Fig. (21)



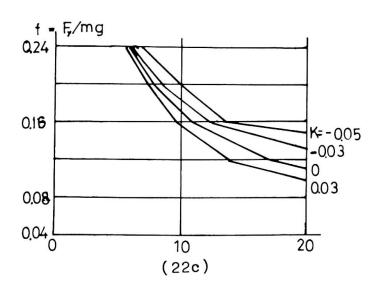


Fig. (22) Deflection Response

SUMMARY

The more precise aspect of the inelastic behaviour of the steel member has been pursued by the analytical method which makes allowance for the strain hardening property of steel.

And the effect of the strain hardening property upon the deflection response of the steel framed structure to an earthquake was evaluated.

RÉSUMÉ

Des connaissances plus précises du comportement plastique de membres en acier ont été obtenues par la méthode analytique, ce qui permet de tenir compte du durcissement de l'acier. Cet effet du durcissement sur la déformation du portique d'acier due à un tremblement de terre a été évalué.

ZUSAMMENFASSUNG

Genaue Kenntnisse des plastischen Verhaltens von Stahlbauteilen wurden mit analytischen Berechnungen angestrebt, wodurch die Verhärtung des Stahls berücksichtigt werden konnte. Die Wirkung der Verhärtung auf die Verformung des Stahlrahmens wurde abgeschätzt.

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